

## Beam Analysis

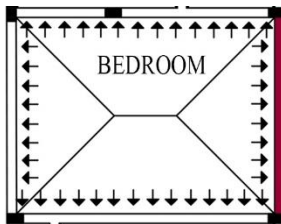
### Load Distribution Diagram

Identify One-Way Slab or Two-Way Slab (to identify the distribution of load from slab to beam).

$L_y$  = longer side of slab     $L_x$  = shorter side of the slab

When  $L_y / L_x > 2$ , it is a one-way slab.

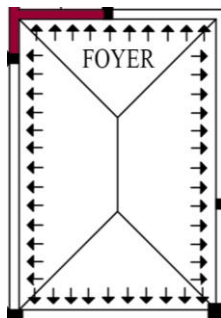
When  $L_y / L_x < 2$  or  $= 2$ , it is a two-way slab.



1. Bedroom (D-E1/ 1-3)  
 $L_y / L_x = 4.785 / 3.6$   
 $= 1.329$  (two-way slab)



2. Staircase (D-F/ 3-4)  
 $L_y / L_x = 5.325 / 1.65$   
 $= 3.227$  (one-way slab)

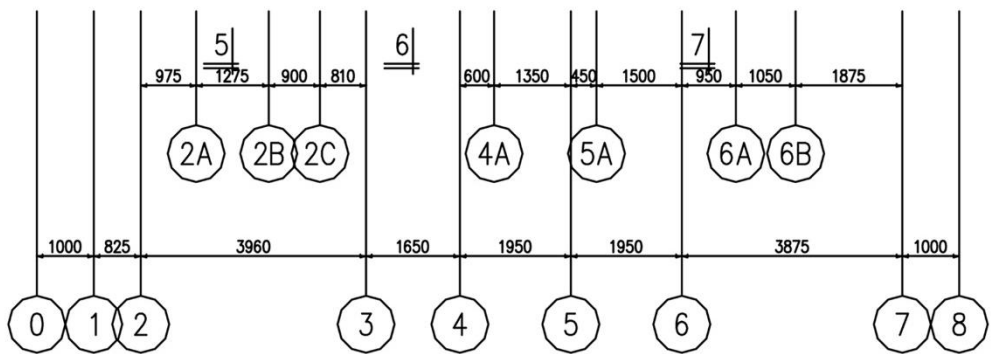
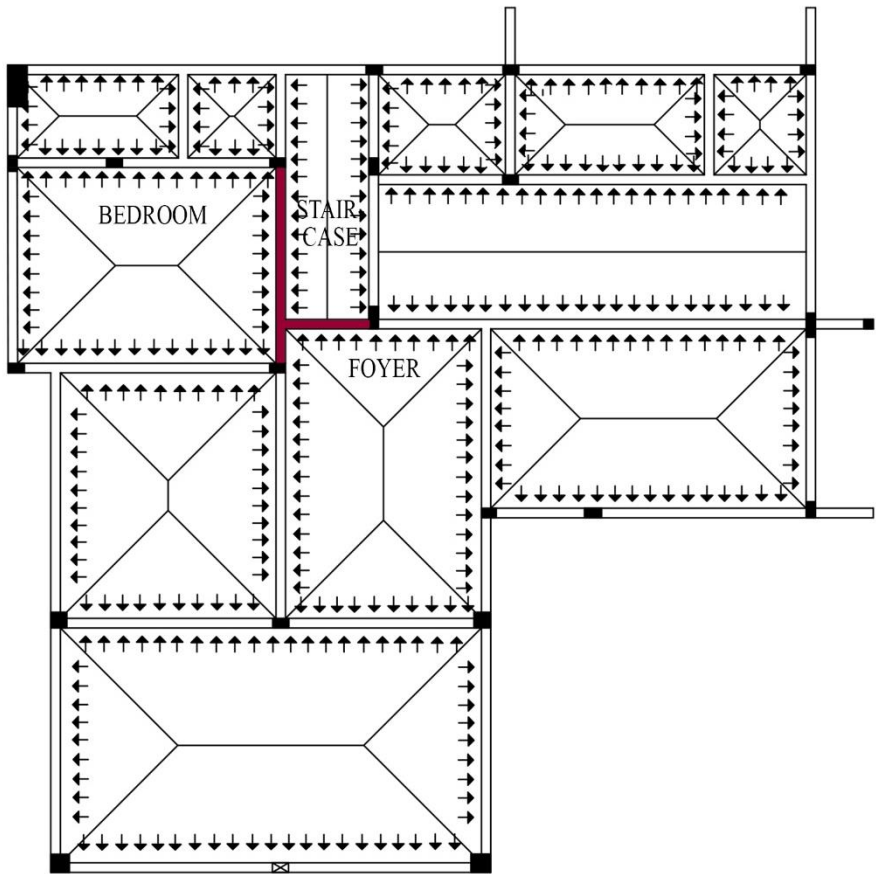
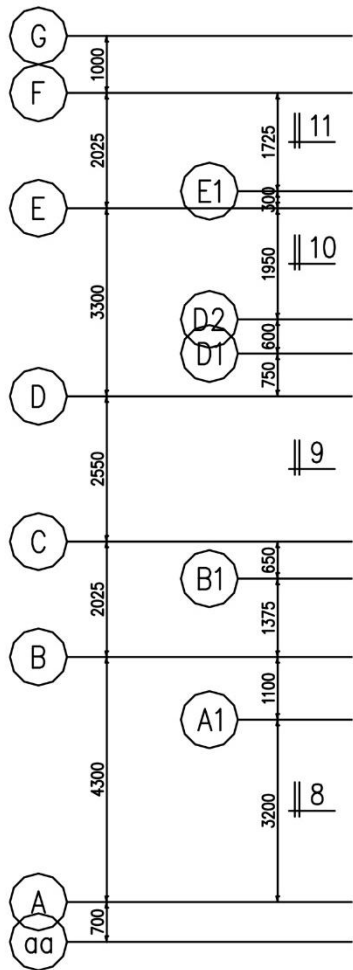


3. Foyer (B-D1/ 3-5)  
 $L_y / L_x = 5.325 / (1.65 + 1.95)$   
 $= 1.479$  (two-way slab)

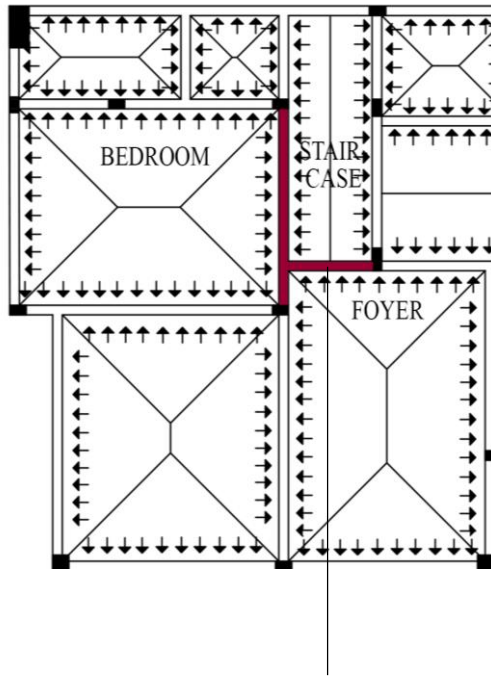
### Live Load of spaces according to UBBL

- A/V Room:  $1.92 \text{ kN/m}^2$
- Balcony:  $1.5 \text{ kN/m}^2$
- Bathroom:  $2.0 \text{ kN/m}^2$
- Bedroom:  $2.0 \text{ kN/m}^2$
- Car porch:  $5.0 \text{ kN/m}^2$
- Dining Room:  $2.0 \text{ kN/m}^2$
- Dressing Room:  $2.0 \text{ kN/m}^2$
- Dry Kitchen:  $3.0 \text{ kN/m}^2$
- Family Room:  $1.92 \text{ kN/m}^2$
- Foyer:  $2.0 \text{ kN/m}^2$
- Living Room:  $2.0 \text{ kN/m}^2$
- Roof:  $0.5 \text{ kN/m}^2$
- Stairs:  $2.0 \text{ kN/m}^2$
- Study Room:  $2.0 \text{ kN/m}^2$
- Utility Room:  $2.0 \text{ kN/m}^2$
- Passage: Based on the room passage is leading to.

Analysis on beam **D1/ 3-4**



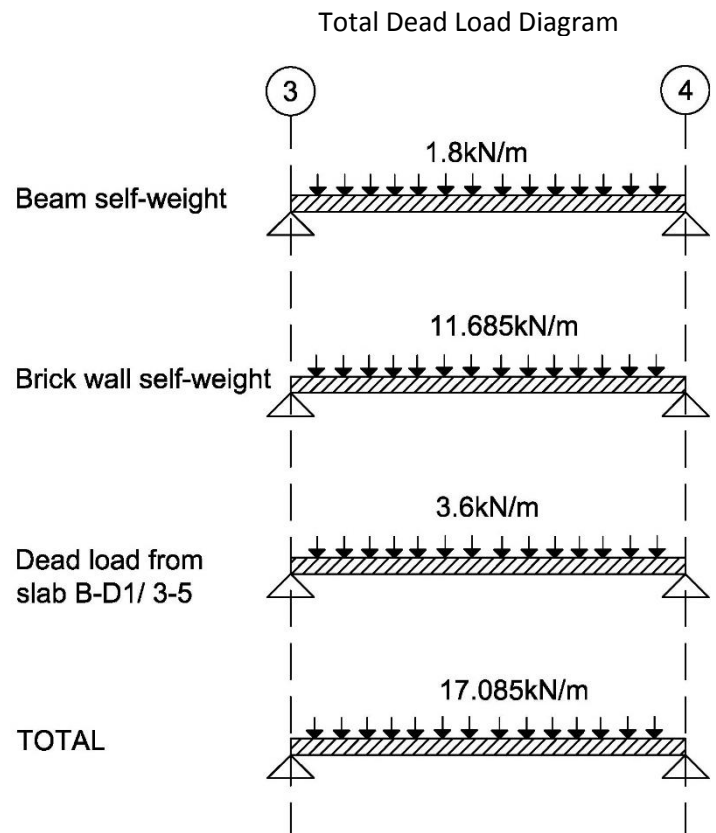
LOAD DISTRIBUTION DIAGRAM- GROUND FLOOR  
(NTS)



Beam D1/ 3-4 (only loads from foyer is acting on it)

#### Dead loads acting on beam D1/ 3-4

1. Slab self-weight  
 $= \text{Slab thickness} \times \text{concrete density}$   
 $= 0.125\text{m} \times 24\text{kN/m}^3$   
 $= 3\text{kN/m}^2$
2. Beam self-weight  
 $= \text{Beam size} \times \text{concrete density}$   
 $= (0.15\text{m} \times 0.5\text{m}) \times 24\text{kN/m}^3$   
 $= 1.8\text{kN/m}$
3. Brick wall self-weight  
 $= \text{Wall height} \times \text{thickness} \times \text{density}$   
 $= 4.1\text{m} \times 0.15\text{m} \times 19\text{kN/m}^3$   
 $= 11.685\text{kN/m}$
4. Dead load from the slab B-D1/ 3-5  
 $= 3\text{kN/m}^2 \times (L_x/2) \times (2/3)$   
 $= 3\text{kN/m}^2 \times (3.6/2) \times (2/3)$   
 $= 3.6\text{kN/m}$
5. Total dead load  
 $= 1.8 + 11.685 + 3.6$   
 $= 17.085 \text{ kN/m}$



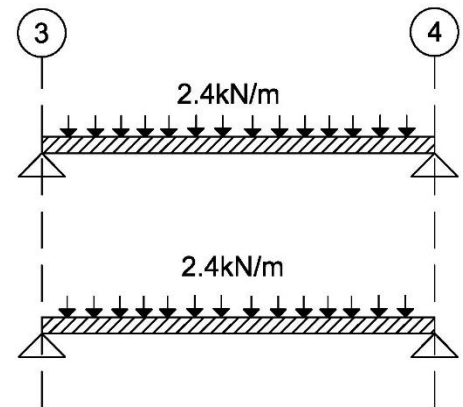
### Live loads acting on beam D1/ 3-4

1. Live load on beam D1/ 3-4  
= live load from foyer x  
 $(L_x/2) \times (2/3)$   
=  $2\text{kN/m}^2 \times (3.6\text{m}/2) \times (2/3)$   
=  $2.4\text{kN/m}$
2. Total live load  
=  $2.4\text{kN/m}$

Live load from  
slab B-D1/ 3-5

TOTAL

Total Live Load Diagram



### Ultimate Load

Dead load factor= 1.4

Live load factor= 1.6

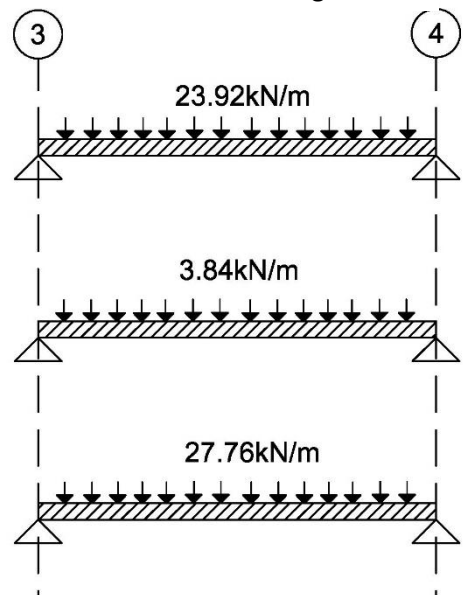
1. Ultimate dead load  
=  $17.085\text{kN/m} \times 1.4$   
=  $23.92\text{kN/m}$
2. Ultimate live load  
=  $2.4\text{kN/m} \times 1.6$   
=  $3.84\text{kN/m}$
3. Ultimate load  
=  $23.92\text{kN/m} + 3.84\text{kN/m}$   
=  $27.76\text{kN/m}$

Ultimate dead load

Ultimate live load

Ultimate load

Ultimate Load Diagram



### Reaction

The ultimate load (UDL) is converted into point load before

resolving the reaction forces of the beam D1/ 3-4.

$$27.76\text{kN/m} \times 1.65\text{m} = 45.8\text{kN}$$

Assuming  $\sum M = 0$ ,

$$[45.8\text{kN} \times (1.65\text{m}/2)] - (R_b \times 1.65\text{m}) = 0$$

$$(45.8\text{kN} \times 0.825\text{m}) - 1.65R_b = 0$$

$$37.785\text{kNm} - 1.65R_b = 0$$

$$-1.65R_b = -37.785\text{kNm}$$

$$R_b = 37.785\text{kNm} / 1.65\text{m}$$

$$R_b = 22.9\text{kN}$$

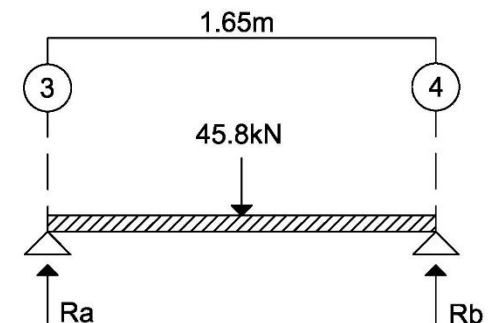
Assuming  $\sum F = 0$ ,

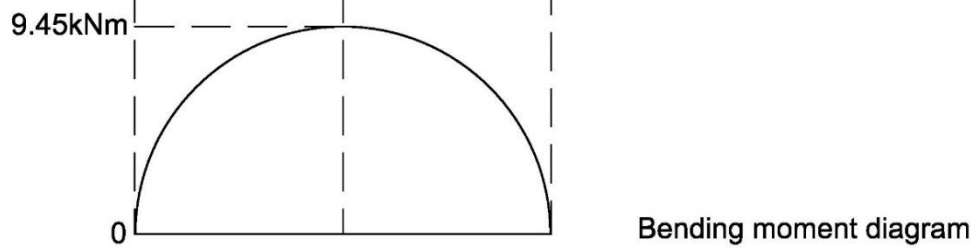
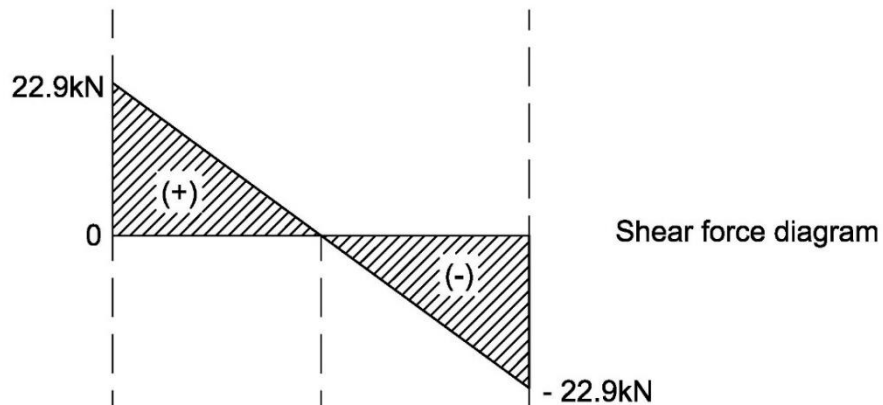
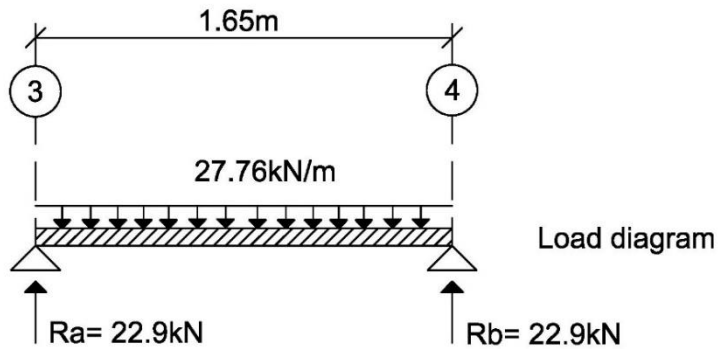
$$45.8\text{kN} - R_a - R_b = 0$$

$$45.8\text{kN} - 22.9\text{kN} - R_a = 0$$

$$R_a = 45.8\text{kN} - 22.9\text{kN}$$

$$R_a = 22.9\text{kN}$$





#### Shear force diagram

At point 3, 22.9kN of  $R_a$  is acting upwards.

From 3 to 4, there is a UDL of 27.76kN/m acting downwards, therefore

$$27.76\text{kN/m} \times 1.65\text{m} = 45.8\text{kN}$$

$$22.9\text{kN} - 45.8\text{kN} = -22.9\text{kN}$$

At point 4, another 22.9kN of  $R_b$  acting upwards, making the beam balance.

#### Bending moment diagram

Positive area – negative area in shear force diagram

(+ve)

$$= (1/2) \times 22.9 \times 0.825$$

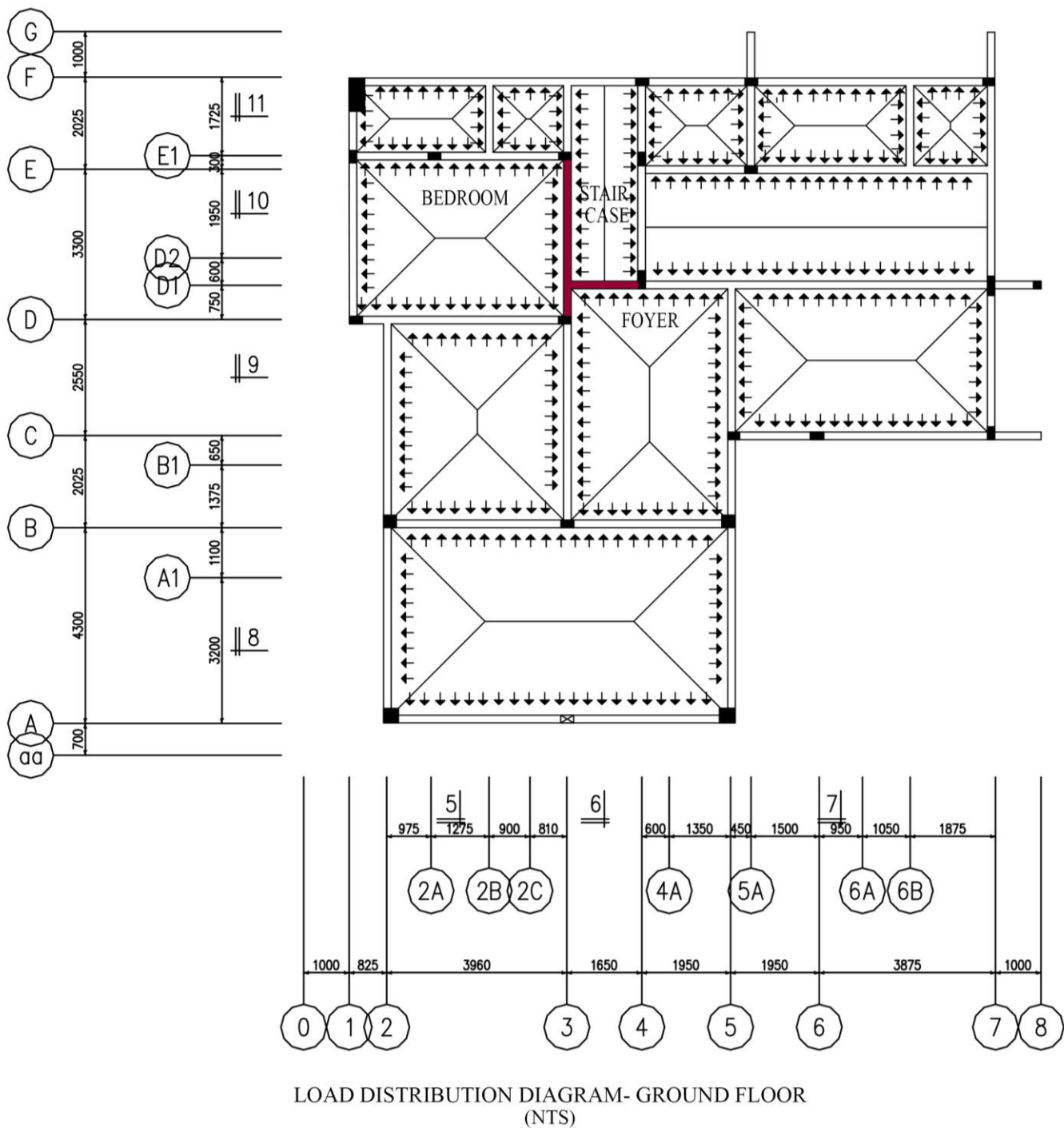
$$= 9.45$$

(-ve)

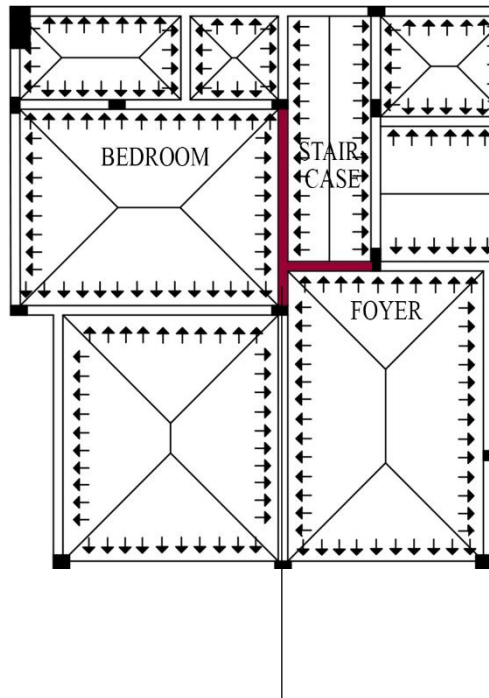
$$= (1/2) \times (-22.9) \times 0.825$$

$$= -9.45$$

Analysis on beam **3/ D- E1**



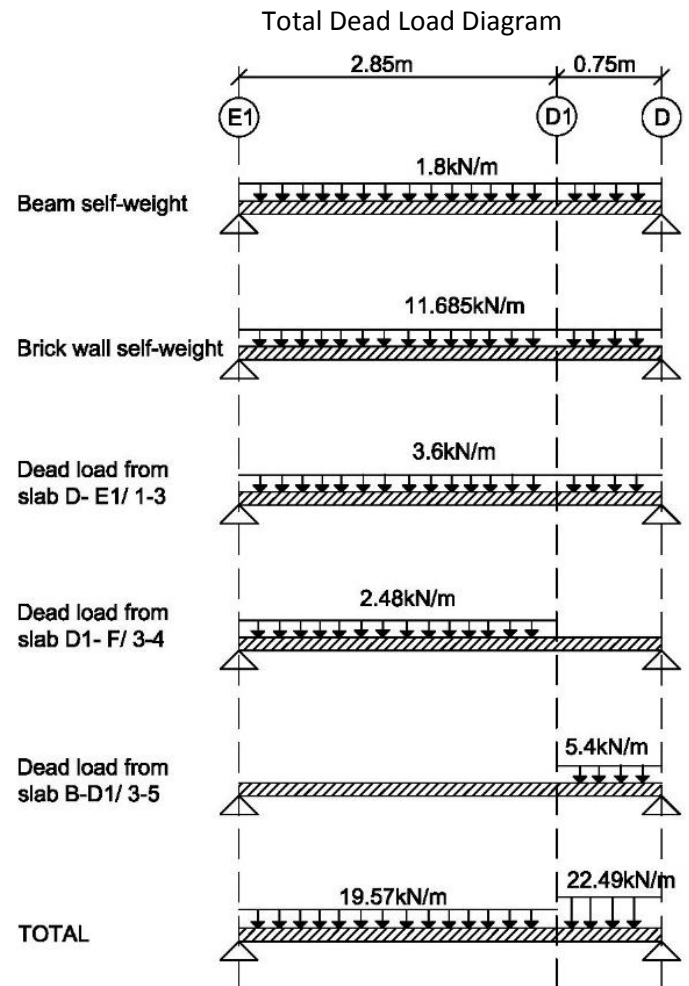
LOAD DISTRIBUTION DIAGRAM- GROUND FLOOR  
(NTS)



Beam 3/ D- E1 (loads from bedroom, staircase and foyer are acting on it)

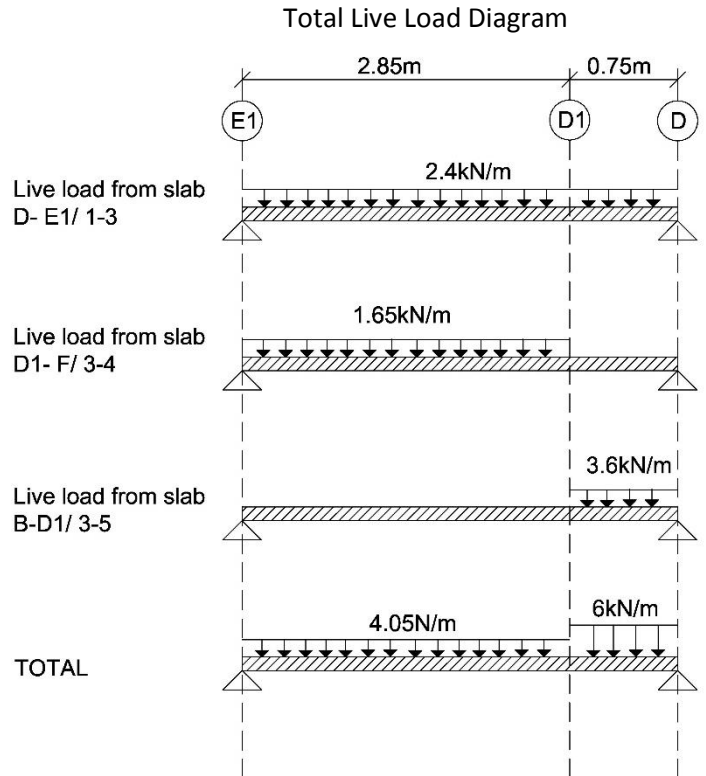
#### Dead loads acting on beam 3/ D- E1

1. Slab self-weight  
 $= \text{Slab thickness} \times \text{concrete density}$   
 $= 0.125\text{m} \times 24\text{kN/m}^3$   
 $= 3\text{kN/m}^2$
2. Beam self-weight  
 $= \text{Beam size} \times \text{concrete density}$   
 $= (0.15\text{m} \times 0.5\text{m}) \times 24\text{kN/m}^3$   
 $= 1.8\text{kN/m}$
3. Brick wall self-weight  
 $= \text{Wall height} \times \text{thickness} \times \text{density}$   
 $= 4.1\text{m} \times 0.15\text{m} \times 19\text{kN/m}^3$   
 $= 11.685\text{kN/m}$
4. Dead load from the slab D- E1/ 1-3  
 $= 3\text{kN/m}^2 \times (L_x/2) \times (2/3)$   
 $= 3\text{kN/m}^2 \times (3.6/2) \times (2/3)$   
 $= 3.6\text{kN/m}$
5. Dead load from the slab D1- F/ 3-4  
 $= 3\text{kN/m}^2 \times (L_x/2)$   
 $= 3\text{kN/m}^2 \times (1.65/2)$   
 $= 2.48\text{kN/m}$
6. Dead load from the slab B- D1/ 3-5  
 $= 3\text{kN/m}^2 \times (L_x/2)$   
 $= 3\text{kN/m}^2 \times (3.6/2)$   
 $= 5.4\text{kN/m}$



### Live loads acting on beam 3/ D- E1

1. Live load from slab D- E1/ 1-3  
= live load of bedroom  $\times (L_x/2) \times (2/3)$   
=  $2\text{kN/m}^2 \times (3.6\text{m}/2) \times (2/3)$   
=  $2.4\text{kN/m}$
2. Live load from slab D1- F/ 3-4  
= live load of staircase  $\times (L_x/2)$   
=  $2\text{kN/m}^2 \times (1.65\text{m}/2)$   
=  $1.65\text{kN/m}$
3. Live load from slab B- D1/ 3-5  
= live load of foyer  $\times (L_x/2)$   
=  $2\text{kN/m}^2 \times (3.6\text{m}/2)$   
=  $3.6\text{kN/m}$

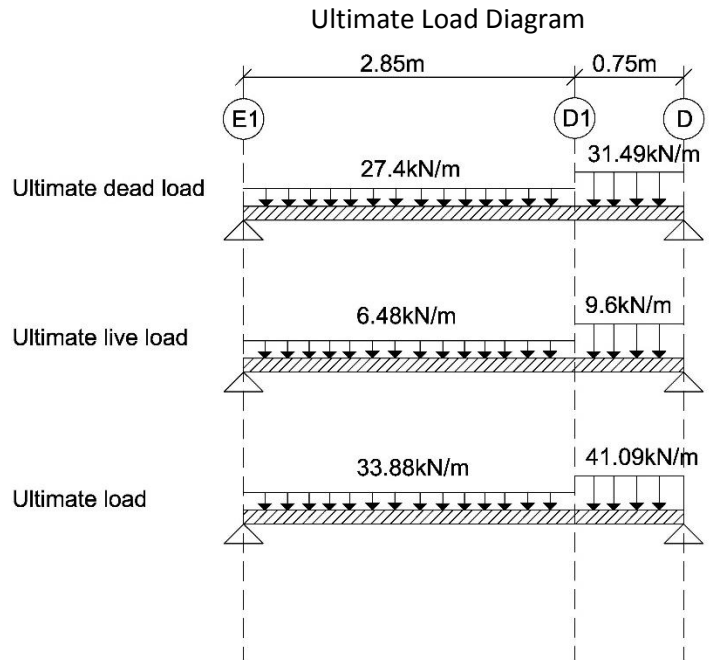


### Ultimate Load

Dead load factor= 1.4

Live load factor= 1.6

1. Ultimate dead load at D1- E1  
=  $19.57\text{kN/m} \times 1.4$   
=  $27.4\text{kN/m}$   
Ultimate dead load at D- D1  
=  $22.49\text{kN/m} \times 1.4$   
=  $31.49\text{kN/m}$
2. Ultimate live load at D1- E1  
=  $4.05\text{kN/m} \times 1.6$   
=  $6.48\text{kN/m}$   
Ultimate live load at D- D1  
=  $6\text{kN/m} \times 1.6$   
=  $9.6\text{kN/m}$
3. Ultimate load at D1- E1  
=  $27.4\text{kN/m} + 6.48\text{kN/m}$   
=  $33.88\text{kN/m}$   
Ultimate load at D- D1  
=  $31.49\text{kN/m} + 9.6\text{kN/m}$   
=  $41.09\text{kN/m}$



### Reaction

The ultimate load (UDL) is converted into point load before resolving the reaction forces of the beam 3/ D- E1.

Ultimate load at D1- E1

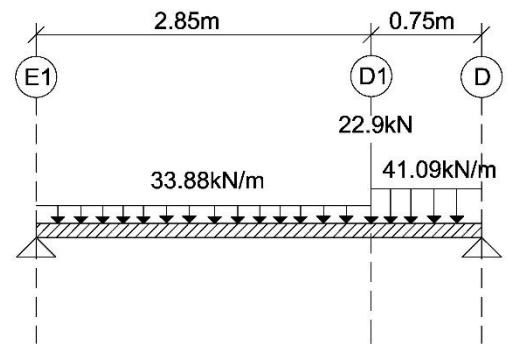
$$= 33.88 \text{ kN/m} \times 2.85 \text{ m} = 96.56 \text{ kN}$$

Ultimate load at D- D1

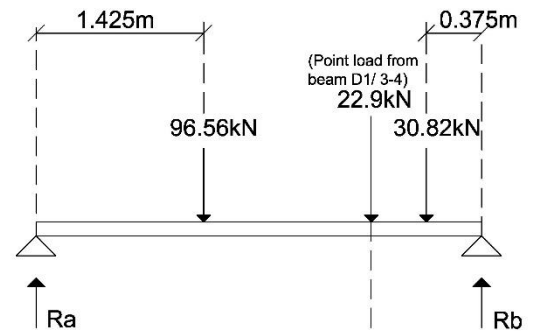
$$= 41.09 \text{ kN/m} \times 0.75 \text{ m} = 30.82 \text{ kN}$$

Reaction force,  $R_a$  of beam D1/ 3-4 acting on this beam is taken as the point load which is 22.9kN.

Ultimate load



Reaction



Assuming  $\sum M = 0$ ,

$$(96.56 \text{ kN} \times 1.425 \text{ m}) + (22.9 \text{ kN} \times 2.85 \text{ m}) + (30.82 \text{ kN} \times 3.225 \text{ m}) - (R_b \times 3.6 \text{ m}) = 0$$

$$137.598 \text{ kNm} + 65.265 \text{ kNm} + 99.39 \text{ kNm} - 3.6 R_b = 0$$

$$302.253 \text{ kNm} - 3.6 R_b = 0$$

$$-3.6 R_b = -302.253 \text{ kNm}$$

$$R_b = 302.253 \text{ kNm} / 3.6 \text{ m}$$

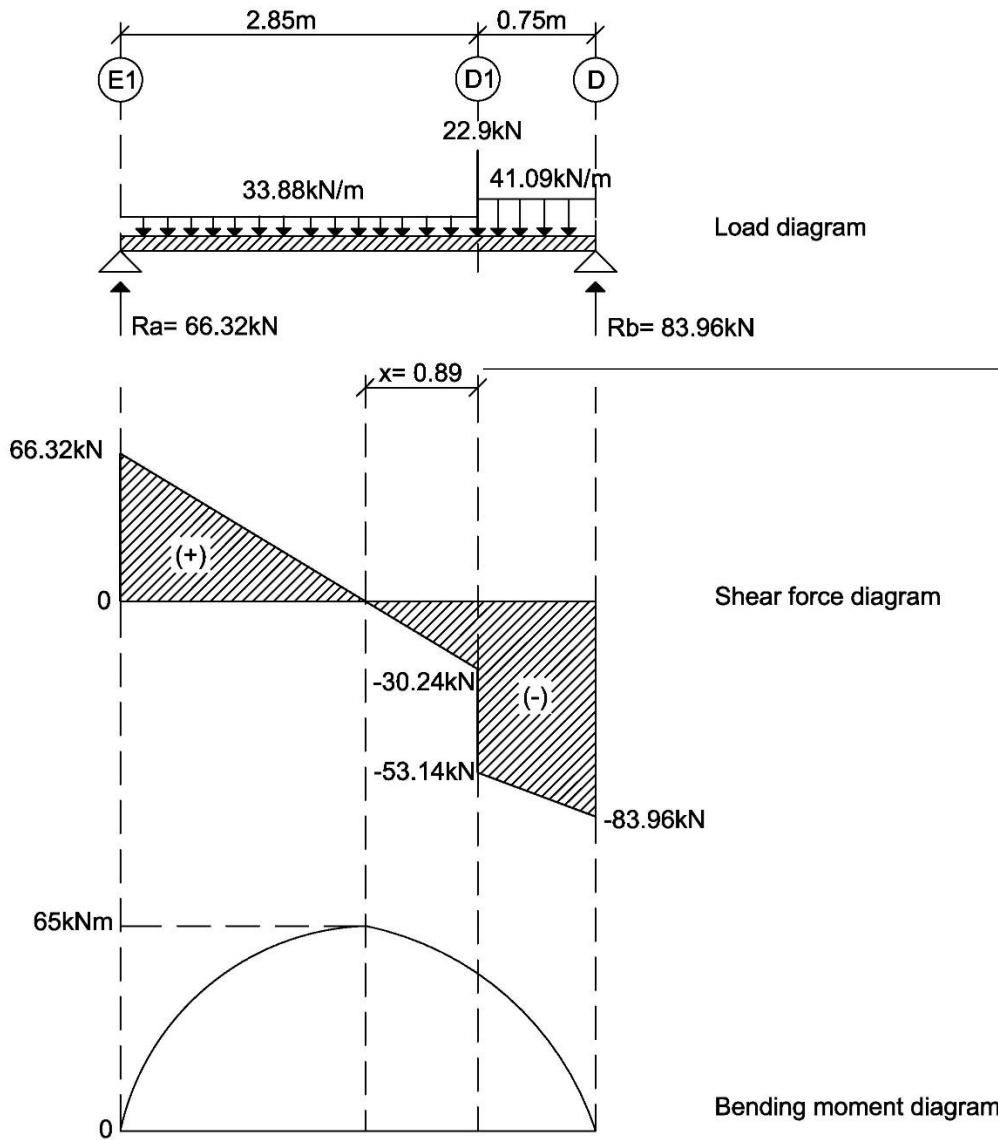
$$R_b = 83.96 \text{ kN}$$

Assuming  $\sum F = 0$ ,

$$96.56 \text{ kN} + 22.9 \text{ kN} + 30.82 \text{ kN} - R_a - R_b = 0$$

$$150.28 \text{ kN} - 83.96 \text{ kN} - R_a = 0$$

$$R_a = 66.32 \text{ kN}$$



$$\begin{aligned} (x / 2.85) &= [30.24 / (30.24 + 66.32)] \\ (x / 2.85) &= 0.31317 \\ X &= 0.31317 \times 2.85 \\ X &= 0.89 \end{aligned}$$

#### Shear force diagram

At point E1,  $66.32 \text{ kN}$  of  $R_a$  is acting upwards.

From E1 to D1, there is a UDL of  $33.88 \text{ kN/m}$  acting downwards, therefore

$$33.88 \text{ kN/m} \times 2.85 \text{ m} = 96.558 \text{ kN}$$

$$66.32 \text{ kN} - 96.558 \text{ kN} = -30.24 \text{ kN}$$

At point D1, there is a point load of  $22.9 \text{ kN}$  ( $R_a$  of beam D1/ 3-4) acting downwards, therefore

$$-30.24 \text{ kN} - 22.9 \text{ kN} = -53.14 \text{ kN}$$

From D1 to D, there is a UDL of  $41.09 \text{ kN/m}$  acting downwards, therefore

$$41.09 \text{ kN/m} \times 0.75 \text{ m} = 30.8175 \text{ kN}$$

$$-53.14 \text{ kN} - 30.8175 \text{ kN} = -83.96 \text{ kN}$$

Which is then resolved by  $R_b$  of  $83.96 \text{ kN}$  that is acting upwards.

#### Bending moment diagram

Positive area – negative area in shear force diagram

(+ve)

$$= (1/2) \times 66.32 \times (2.85 - 0.89)$$

$$= (1/2) \times 66.32 \times 1.96$$

$$= 64.99 \approx 65$$

(-ve)

$$= [(1/2) \times -30.24 \times 0.89] + [(1/2) \times [(-53.14) + (-83.96)] \times 0.75]$$

$$= -13.46 + 51.41$$

$$= -64.87 \approx -65$$

## Load Distribution Diagram

Identify One-Way Slab or Two-Way Slab (to identify the distribution of load from slab to beam).

$L_y$  = longer side of slab     $L_x$  = shorter side of the slab

When  $L_y / L_x > 2$ , it is a one-way slab.

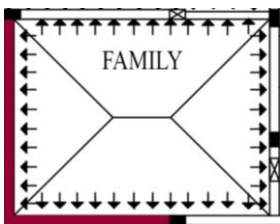
When  $L_y / L_x < 2$  or  $= 2$ , it is a two-way slab.



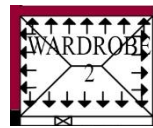
1. Staircase (D-E1/ 1-2A)  
 $L_y / L_x$   
 $= 3.7 / 1.8$   
 $= 2.1$  (one-way slab)



5. Wardrobe 1 (C-D/ 2C-4A)  
 $L_y / L_x$   
 $= 3.06 / 2.55$   
 $= 1.2$  (two-way slab)



2. Family (D-E1/ 2A-4)  
 $L_y / L_x$   
 $= 4.635 / 3.6$   
 $= 1.2875$  (two-way slab)



6. Wardrobe 2 (B-C/ 2C-4)  
 $L_y / L_x$   
 $= 2.46 / 2.025$   
 $= 1.215$  (two-way slab)

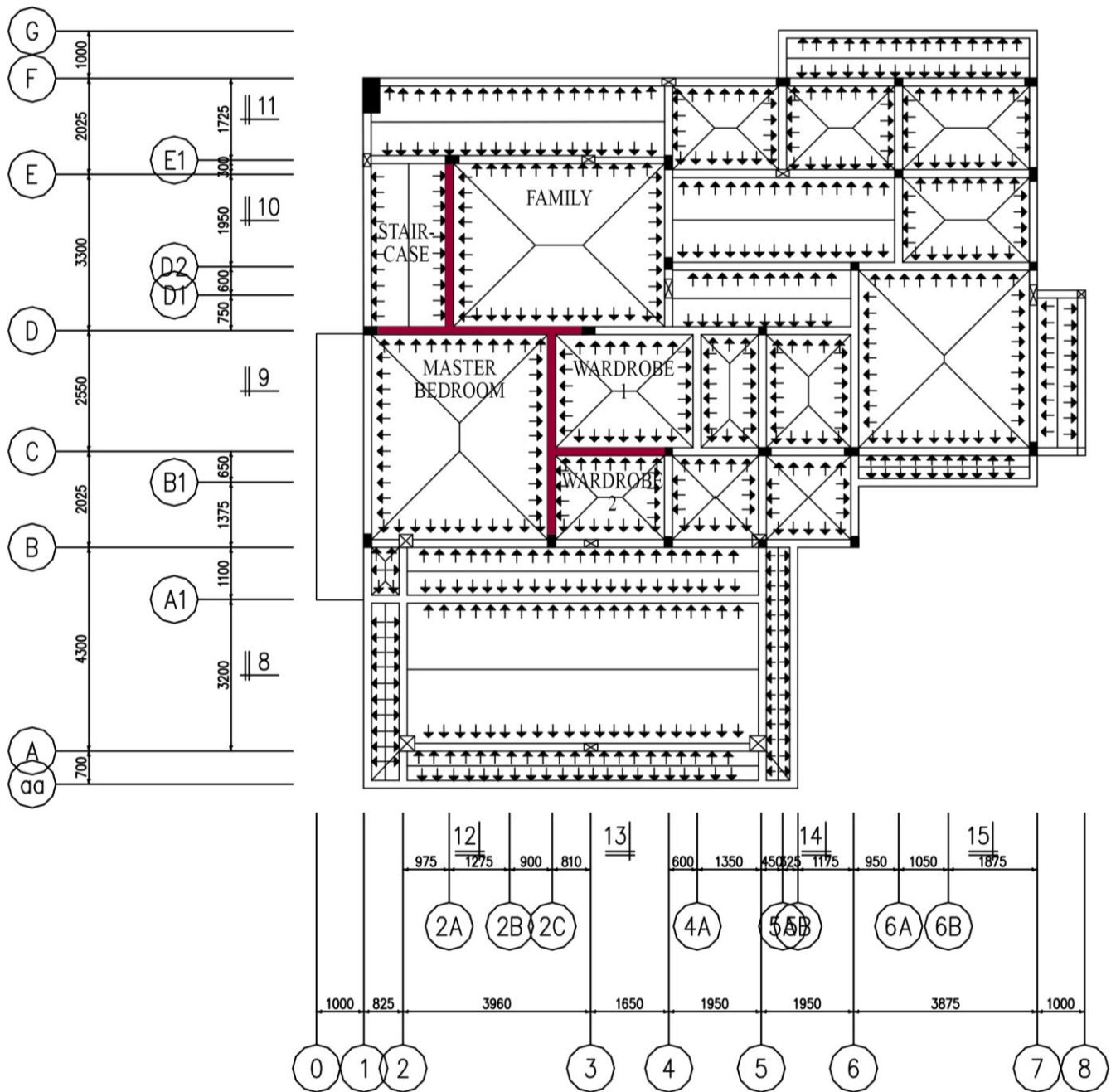


3. Master Bedroom (B-D/ 1-2C)  
 $L_y / L_x$   
 $= 4.575 / 3.975$   
 $= 1.15$  (two-way slab)

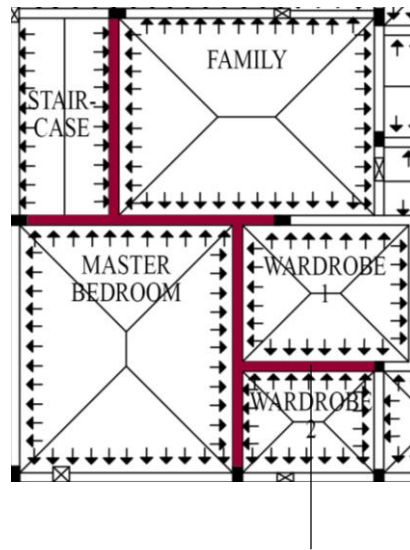
## Live Load of spaces according to UBBL

- A/V Room: 1.92kN/m
- Balcony: 1.5kN/m
- Bathroom: 2.0 kN/m
- Bedroom: 2.0 kN/m
- Car porch: 5.0kN/m
- Dining Room: 2.0 kN/m
- Dressing Room: 2.0kN/m
- Dry Kitchen: 3.0 kN/m
- Family Room: 1.92kN/m
- Foyer: 2.0kN/m
- Living Room: 2.0kN/m
- Roof: 0.5kN/m
- Stairs: 2.0kN/m
- Study Room: 2.0kN/m
- Utility Room: 2.0kN/m
- Passage: Based on the room passage is leading to.

## Analysis on beam **C/ 2C-4**



LOAD DISTRIBUTION DIAGRA- FIRST FLOOR  
(NTS)



Beam C/ 2C- 4 (loads from wardrobe 1 and wardrobe 2 are acting on it)

#### Dead loads acting on beam C/ 2C- 4

1. Slab self-weight  
 $= \text{Slab thickness} \times \text{concrete density}$   
 $= 0.125\text{m} \times 24\text{kN/m}^3$   
 $= 3\text{kN/m}^2$
2. Beam self-weight  
 $= \text{Beam size} \times \text{concrete density}$   
 $= (0.15\text{m} \times 0.6\text{m}) \times 24\text{kN/m}^3$   
 $= 2.16\text{kN/m}$
3. Dead load from the slab B- C/ 2C-4  
 $= 3\text{kN/m}^2 \times (L_x/2)$   
 $= 3\text{kN/m}^2 \times (2.025/2)$   
 $= 3.0375\text{kN/m}$
4. Dead load from the slab C- D/ 2C-4A  
 $= 3\text{kN/m}^2 \times (L_x/2)$   
 $= 3\text{kN/m}^2 \times (2.55/2)$   
 $= 3.825\text{kN/m}$
5. Total dead load  
 $= 2.16\text{kN/m} + 3.0375\text{kN/m} + 3.825\text{kN/m}$   
 $= 9.02\text{kN/m}$

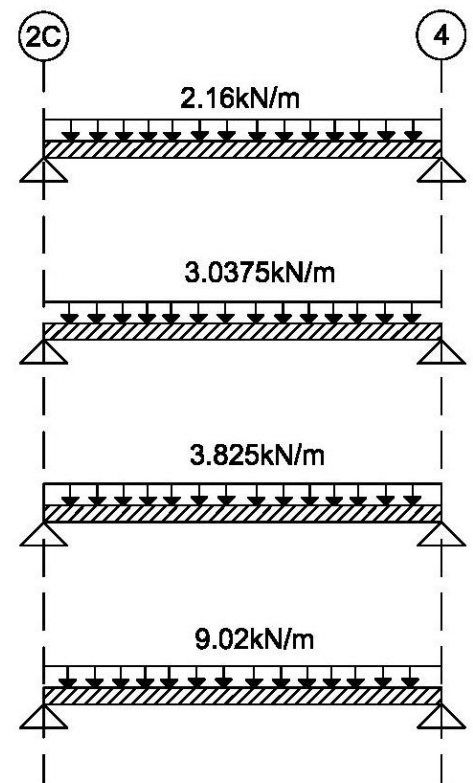
Beam self-weight

Dead load from  
slab B-C/ 2C-4

Dead load from  
slab C-D/ 2C-4A

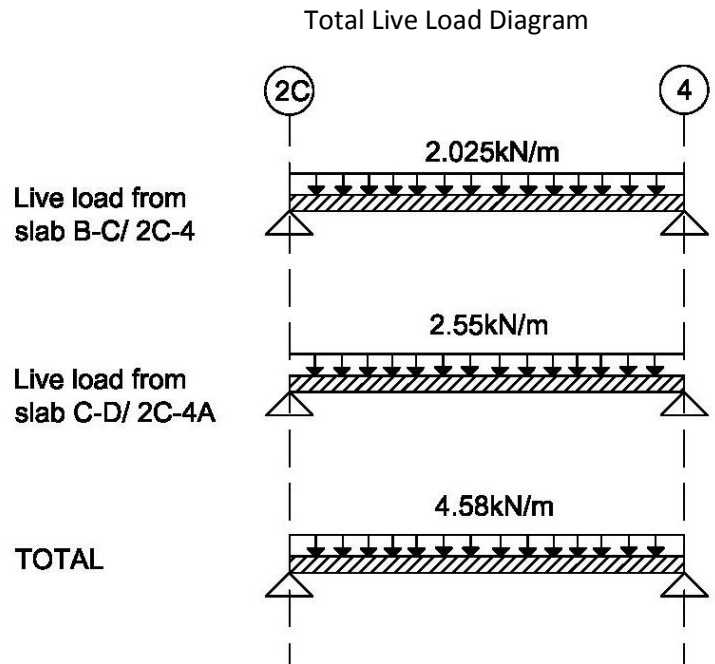
TOTAL

#### Total Dead Load Diagram



### Live loads acting on beam C/ 2C- 4

1. Live load from slab B- C/ 2C-4  
= live load of wardrobe  $\times (L_x/ 2)$   
=  $2\text{kN/m}^2 \times (2.025\text{m}/ 2)$   
=  $2.025\text{kN/m}$
2. Live load from slab C- D/ 2C-4A  
= live load of wardrobe  $\times (L_x/ 2)$   
=  $2\text{kN/m}^2 \times (2.55\text{m}/ 2)$   
=  $2.55\text{kN/m}$
3. Total live load  
=  $2.025\text{kN/m} + 2.55\text{kN/m}$   
=  $4.58\text{kN/m}$

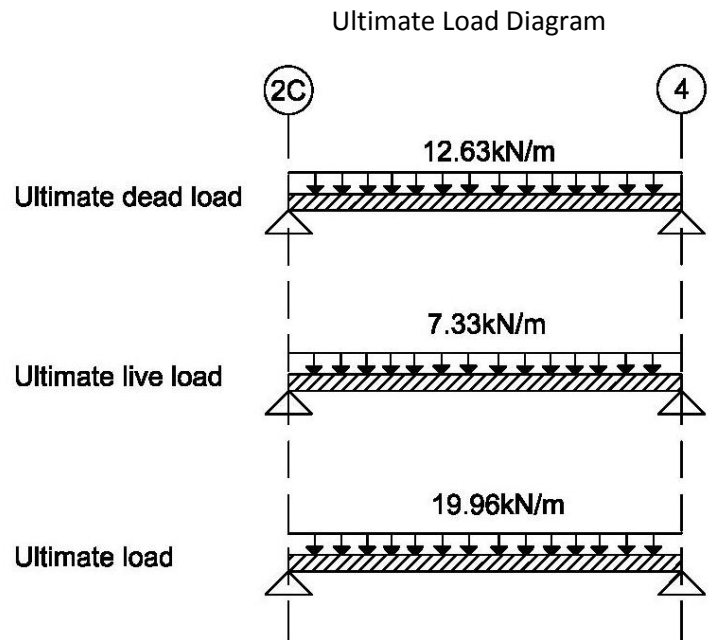


### Ultimate Load

Dead load factor= 1.4

Live load factor= 1.6

1. Ultimate dead load  
=  $9.02\text{kN/m} \times 1.4$   
=  $12.63\text{kN/m}$
2. Ultimate live load  
=  $4.58\text{kN/m} \times 1.6$   
=  $7.33\text{kN/m}$
3. Ultimate load  
=  $12.63\text{kN/m} + 7.33\text{kN/m}$   
=  $19.96\text{kN/m}$



### Reaction

The ultimate load (UDL) is converted into point load before resolving the reaction forces of the beam C/ 2C- 4.

Ultimate load

$$= 19.96\text{kN/m} \times 2.46\text{m} = 49.10\text{kN}$$

Assuming  $\sum M = 0$ ,

$$(49.1\text{kN} \times 1.23\text{m}) - (R_b \times 2.46\text{m}) = 0$$

$$60.393\text{kNm} - 2.46R_b = 0$$

$$-2.46R_b = -60.393\text{kNm}$$

$$R_b = 60.393\text{kNm} / 2.46\text{m}$$

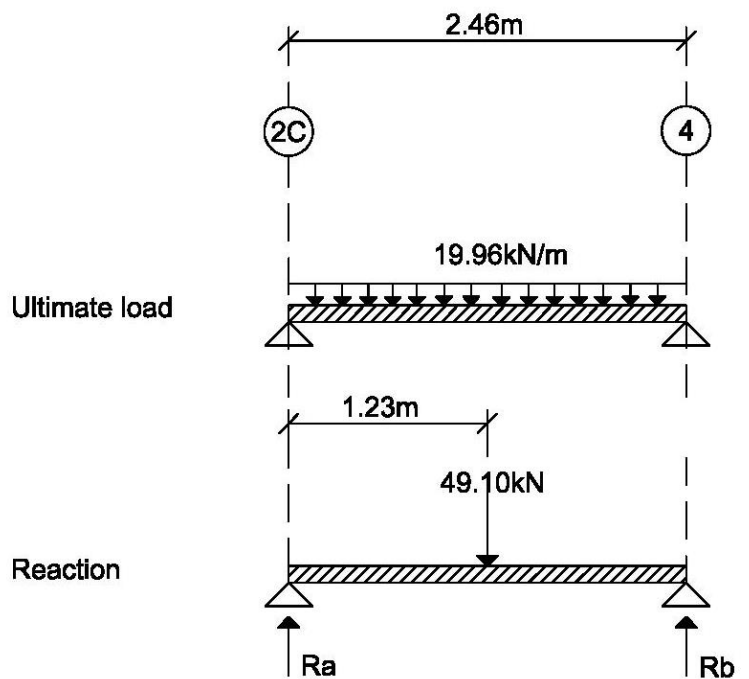
$$R_b = 24.55\text{kN}$$

Assuming  $\sum F = 0$ ,

$$49.1\text{kN} - R_a - R_b = 0$$

$$49.1\text{kN} - 24.55\text{kN} - R_a = 0$$

$$R_a = 24.55\text{kN}$$



### Shear force diagram

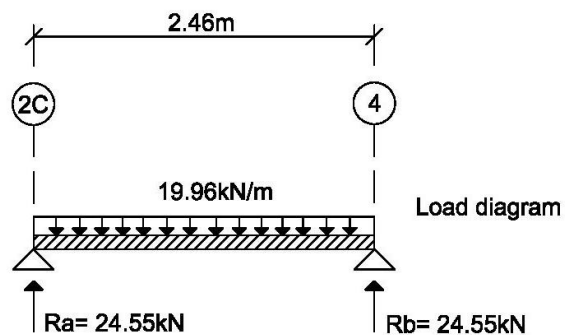
At point 2C, 24.55kN of  $R_a$  is acting upwards.

From 2C to 4, there is a UDL of 19.96kN/m acting downwards, therefore

$$19.96\text{kN/m} \times 2.46\text{m} = 49.1016\text{kN}$$

$$24.55\text{kN} - 49.1016\text{kN} = -24.55\text{kN}$$

At point 4, another 24.55kN of  $R_b$  acting upwards, thus making the beam balance.



### Bending moment diagram

Positive area – negative area in shear force diagram

(+ve)

$$= (1/2) \times 24.55 \times (2.46/2)$$

$$= (1/2) \times 24.55 \times 1.23$$

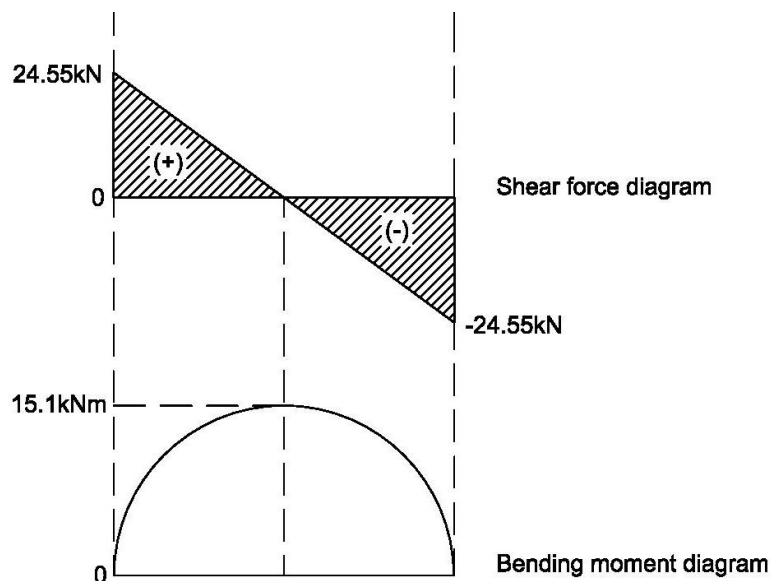
$$= 15.1$$

(-ve)

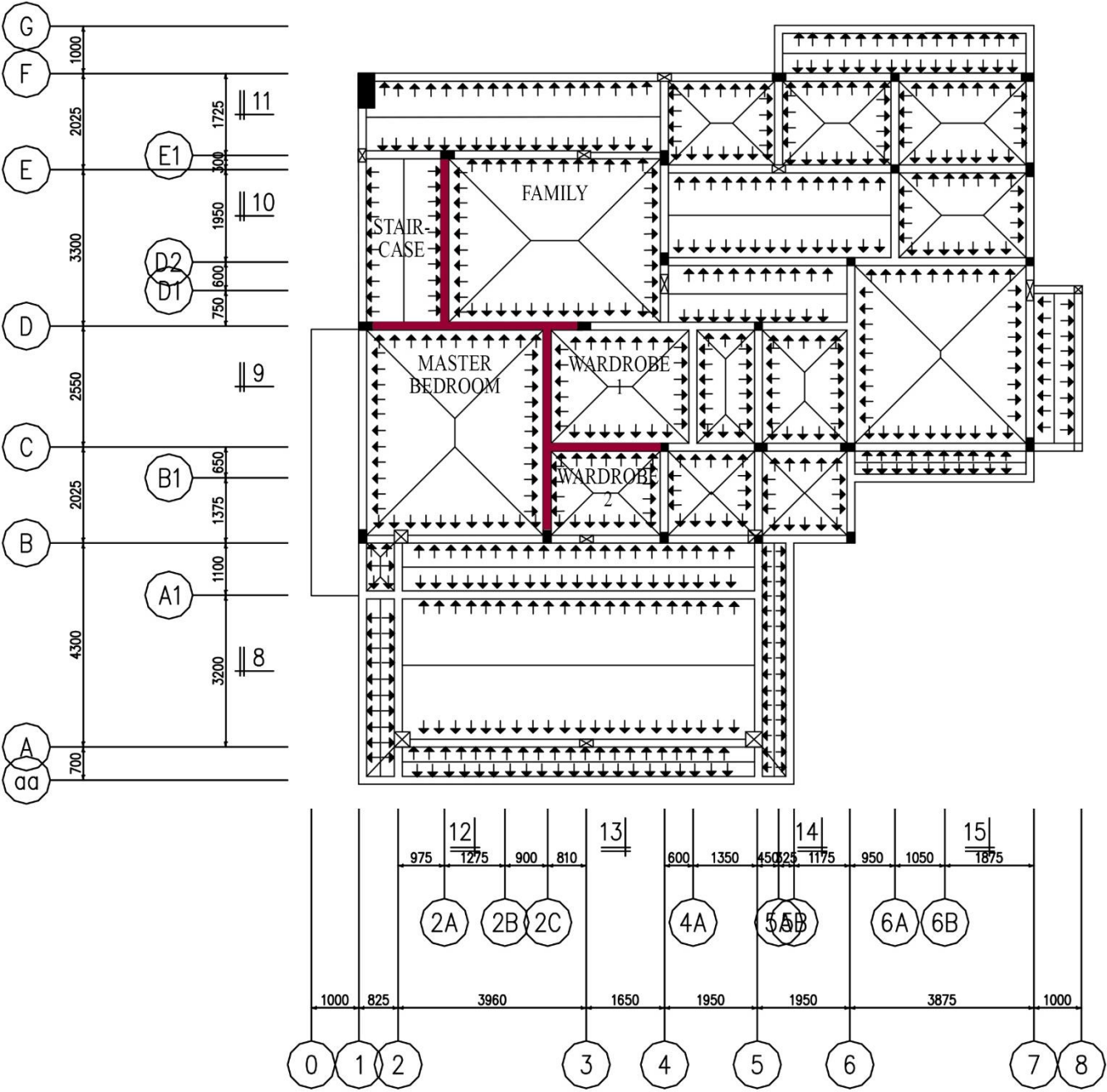
$$= (1/2) \times (-24.55) \times (2.46/2)$$

$$= (1/2) \times (-24.55) \times 1.23$$

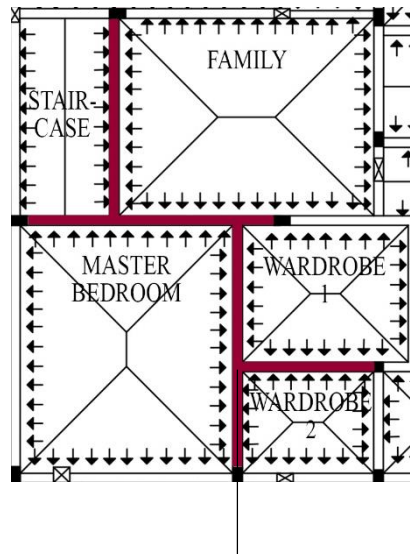
$$= -15.1$$



Analysis on beam **2C/ B-D**



LOAD DISTRIBUTION DIAGRA- FIRST FLOOR  
(NTS)

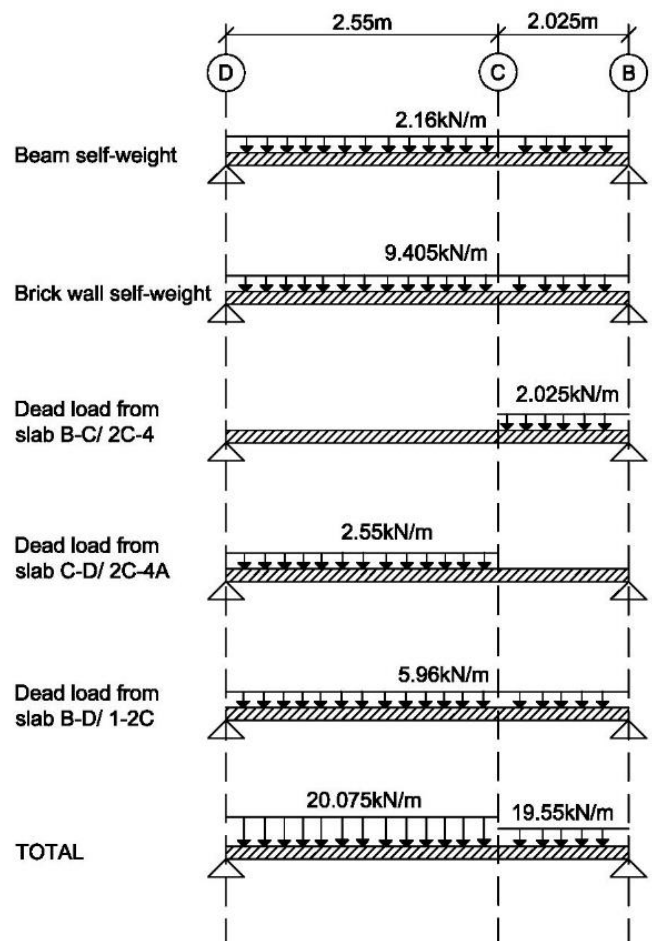


Beam 2C/ B- D (loads from wardrobe 1, wardrobe 2 and master bedroom are acting on it)

#### Dead loads acting on beam 2C/ B- D

1. Slab self-weight  
 $= \text{Slab thickness} \times \text{concrete density}$   
 $= 0.125\text{m} \times 24\text{kN/m}^3$   
 $= 3\text{kN/m}^2$
2. Beam self-weight  
 $= \text{Beam size} \times \text{concrete density}$   
 $= (0.15\text{m} \times 0.6\text{m}) \times 24\text{kN/m}^3$   
 $= 2.16\text{kN/m}$
3. Brick wall self-weight  
 $= \text{Wall height} \times \text{thickness} \times \text{density}$   
 $= 3.3\text{m} \times 0.15\text{m} \times 19\text{kN/m}^3$   
 $= 9.405\text{kN/m}$
4. Dead load from the slab B- C/ 2C-4  
 $= 3\text{kN/m}^2 \times (L_x/2) \times (2/3)$   
 $= 3\text{kN/m}^2 \times (2.025/2) \times (2/3)$   
 $= 2.025\text{kN/m}$
5. Dead load from the slab C- D/ 2C-4A  
 $= 3\text{kN/m}^2 \times (L_x/2) \times (2/3)$   
 $= 3\text{kN/m}^2 \times (2.55/2) \times (2/3)$   
 $= 2.55\text{kN/m}$
6. Dead load from the slab B- D/ 1-2C  
 $= 3\text{kN/m}^2 \times (L_x/2)$   
 $= 3\text{kN/m}^2 \times (3.975/2)$   
 $= 5.96\text{kN/m}$

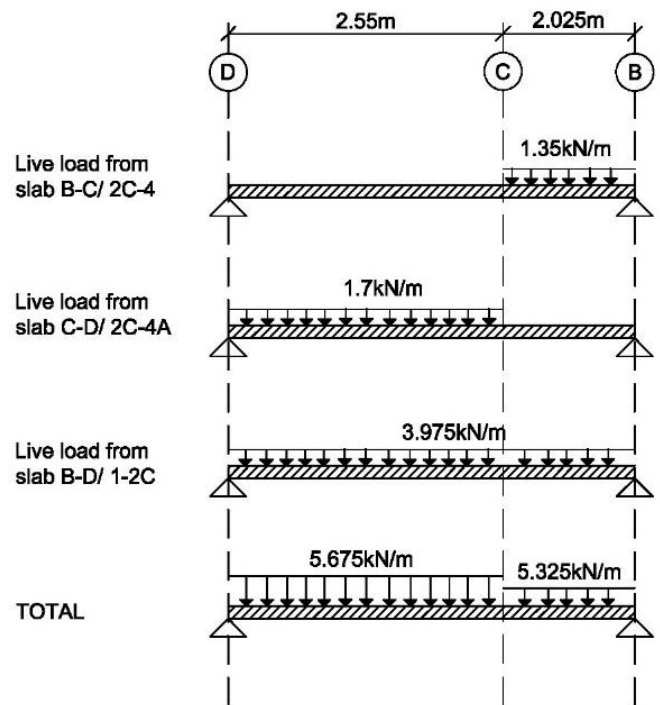
#### Total Dead Load Diagram



### Live loads acting on beam 2C/ B- D

1. Live load from slab B- C/ 2C-4  
= live load of wardrobe  $2 \times (L_x/2) \times (2/3)$   
=  $2\text{kN/m}^2 \times (2.025\text{m}/2) \times (2/3)$   
=  $1.35\text{kN/m}$
2. Live load from slab C- D/ 2C-4A  
= live load of wardrobe  $1 \times (L_x/2) \times (2/3)$   
=  $2\text{kN/m}^2 \times (2.55\text{m}/2) \times (2/3)$   
=  $1.7\text{kN/m}$
3. Live load from slab B- D/ 1-2C  
= live load of master bedroom  $\times (L_x/2)$   
=  $2\text{kN/m}^2 \times (3.975\text{m}/2)$   
=  $3.975\text{kN/m}$

Total Live Load Diagram



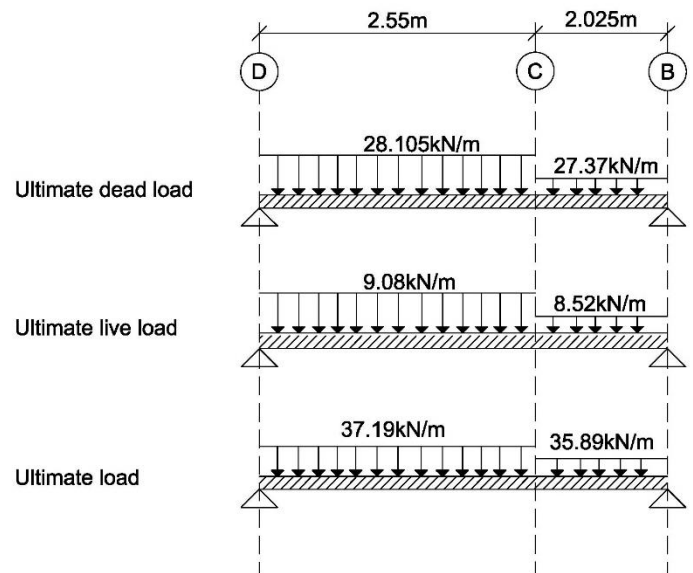
### Ultimate Load

Dead load factor= 1.4

Live load factor= 1.6

1. Ultimate dead load at B- C  
=  $19.55\text{kN/m} \times 1.4$   
=  $27.37\text{kN/m}$   
Ultimate dead load at C- D  
=  $20.075\text{kN/m} \times 1.4$   
=  $28.105\text{kN/m}$
2. Ultimate live load at B- C  
=  $5.325\text{kN/m} \times 1.6$   
=  $8.52\text{kN/m}$   
Ultimate live load at C- D  
=  $5.675\text{kN/m} \times 1.6$   
=  $9.08\text{kN/m}$
3. Ultimate load at B- C  
=  $27.37\text{kN/m} + 8.52\text{kN/m}$   
=  $35.89\text{kN/m}$   
Ultimate load at C- D  
=  $28.105\text{kN/m} + 9.08\text{kN/m}$   
=  $37.19\text{kN/m}$

Ultimate Load Diagram



## Reaction

The ultimate load (UDL) is converted into point load before resolving the reaction forces of the beam 2C/ B- D.

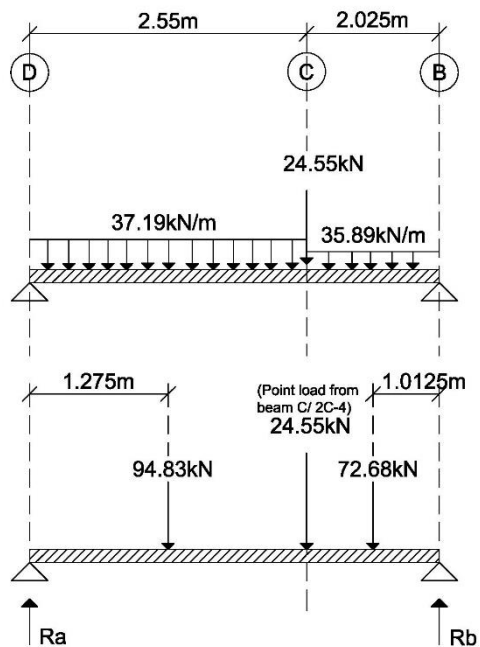
Ultimate load at B- C

$$= 35.89\text{kN/m} \times 2.025\text{m} = 72.68\text{kN}$$

Ultimate load at C- D

$$= 37.19\text{kN/m} \times 2.55\text{m} = 94.83\text{kN}$$

Reaction force,  $R_a$  of beam C/ 2C-4 acting on this beam is taken as the point load which is 24.55kN.



Assuming  $\sum M = 0$ ,

$$(94.83\text{kN} \times 1.275\text{m}) + (24.55\text{kN} \times 2.55\text{m}) + (72.68\text{kN} \times 3.5625\text{m}) - (R_b \times 4.575\text{m}) = 0$$

$$120.91\text{kNm} + 65.60\text{kNm} + 258.92\text{kNm} - 4.575R_b = 0$$

$$442.43\text{kNm} - 4.575R_b = 0$$

$$-4.575R_b = -442.43\text{kNm}$$

$$R_b = 442.43\text{kNm} / 4.575\text{m}$$

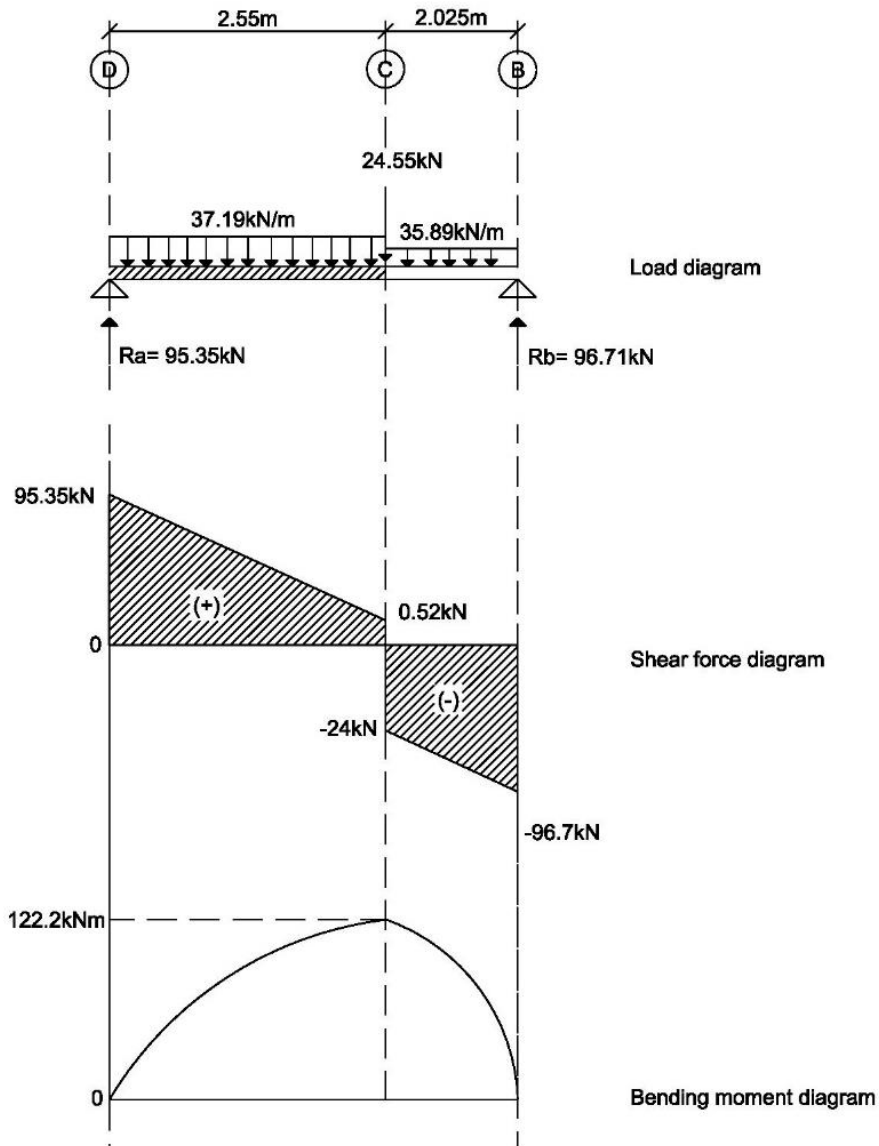
$$R_b = 96.71\text{kN}$$

Assuming  $\sum F = 0$ ,

$$94.83\text{kN} + 24.55\text{kN} + 72.68\text{kN} - R_a - R_b = 0$$

$$192.06\text{kN} - 96.71\text{kN} - R_a = 0$$

$$R_a = 95.35\text{kN}$$



#### Shear force diagram

At point D, 95.35kN of  $R_a$  is acting upwards.

From D to C, there is a UDL of 37.19kN/m acting downwards, therefore

$$37.19\text{kN/m} \times 2.55\text{m} = 94.8345\text{kN}$$

$$95.35\text{kN} - 94.8345\text{kN} = 0.52\text{kN}$$

At point C, there is a point load of 24.55kN ( $R_a$  of beam C/ 2C-4) acting downwards, therefore

$$0.52\text{kN} - 24.55\text{kN} = -24\text{kN}$$

From C to B, there is a UDL of 35.89kN/m acting downwards, therefore

$$35.89\text{kN/m} \times 2.025\text{m} = 76.677\text{kN}$$

$$-24\text{kN} - 76.677\text{kN} = -96.68\text{kN} \approx -96.7\text{kN}$$

Which is then resolved by  $R_b$  of 96.71kN that is acting upwards.

#### Bending moment diagram

Positive area – negative area in shear force diagram

(+ve)

$$= (1/2) \times (95.35 + 0.52) \times 2.55$$

$$= (1/2) \times 95.87 \times 2.55$$

$$= 122.23 \approx 122.2$$

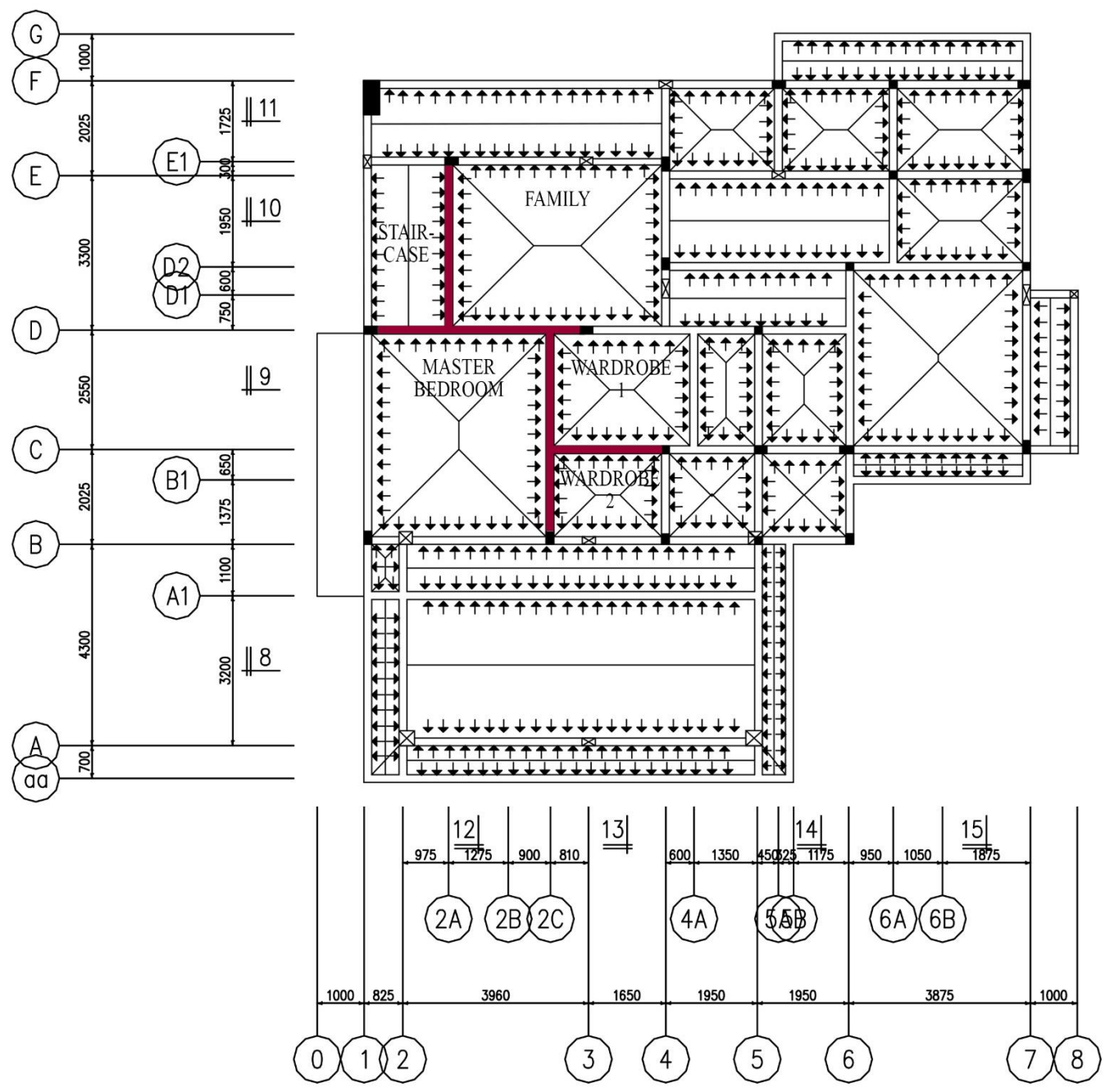
(-ve)

$$= (1/2) \times [(-24) + (-96.7)] \times 2.025$$

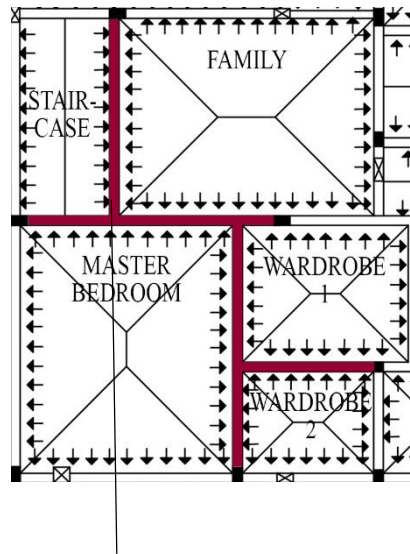
$$= (1/2) \times 120.7 \times 2.025$$

$$= 122.21 \approx -122.2$$

Analysis on beam **2A/ D-E1**



LOAD DISTRIBUTION DIAGRA- FIRST FLOOR  
(NTS)



Beam 2A/ D- E1 (loads from staircase and family room are acting on it).

#### Dead loads acting on beam 2A/ D- E1

1. Slab self-weight  
 $= \text{Slab thickness} \times \text{concrete density}$   
 $= 0.125\text{m} \times 24\text{kN/m}^3$   
 $= 3\text{kN/m}^2$
2. Beam self-weight  
 $= \text{Beam size} \times \text{concrete density}$   
 $= (0.15\text{m} \times 0.6\text{m}) \times 24\text{kN/m}^3$   
 $= 2.16\text{kN/m}$
3. Brick wall self-weight  
 $= \text{Wall height} \times \text{thickness} \times \text{density}$   
 $= 3.3\text{m} \times 0.15\text{m} \times 19\text{kN/m}^3$   
 $= 9.405\text{kN/m}$
4. Dead load from the slab D- E1/ 1-2A  
 $= 3\text{kN/m}^2 \times (L_x/2)$   
 $= 3\text{kN/m}^2 \times (1.8/2)$   
 $= 2.7\text{kN/m}$
5. Dead load from the slab D- E1/ 2A-4  
 $= 3\text{kN/m}^2 \times (L_x/2) \times (2/3)$   
 $= 3\text{kN/m}^2 \times (3.6/2) \times (2/3)$   
 $= 3.6\text{kN/m}$
6. Total dead load  
 $= 2.16\text{kN/m} + 9.405\text{kN/m} + 2.7\text{kN/m}$   
 $+ 3.6\text{kN/m}$   
 $= 17.865\text{kN/m}$

#### Total Dead Load Diagram

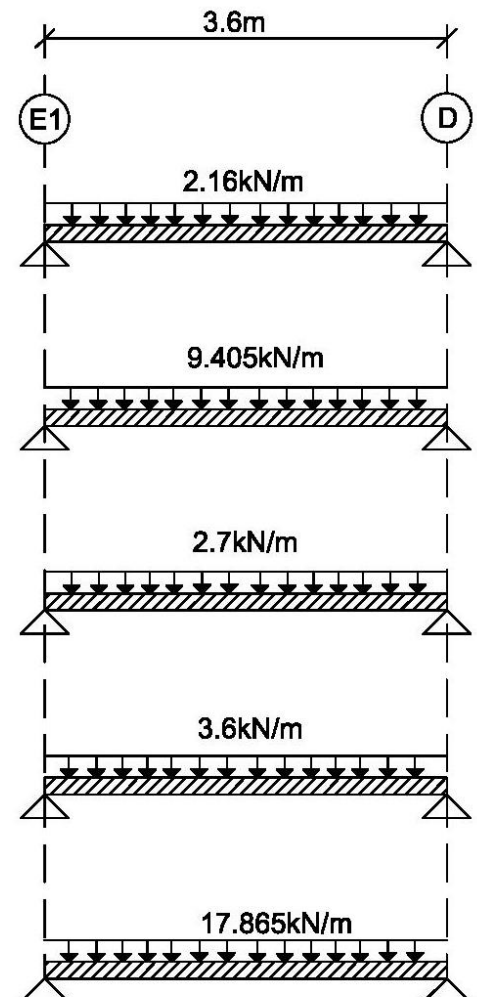
Beam self-weight

Brick wall self-weight

Dead load from slab D-E1/ 1-2A

Dead load from slab D-E1/ 2A-4

TOTAL



### Live loads acting on beam 2A/ D- E1

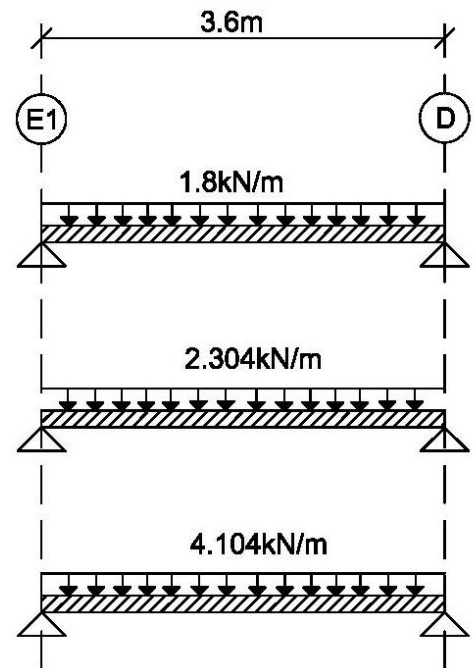
1. Live load from slab D- E1/ 1-2A  
= live load of staircase  $\times (L_x / 2)$   
=  $2\text{kN/m}^2 \times (1.8\text{m} / 2)$   
=  $1.8\text{kN/m}$
2. Live load from slab D- E1/ 2A-4  
= live load of family room  $\times (L_x / 2) \times (2/3)$   
=  $1.92\text{kN/m}^2 \times (3.6\text{m} / 2) \times (2/3)$   
=  $2.304\text{kN/m}$
3. Total live load  
=  $1.8\text{kN/m} + 2.304\text{kN/m}$   
=  $4.104\text{kN/m}$

Live load from  
slab D-E1/ 1-2A

Live load from  
slab D-E1/ 2A-4

TOTAL

Total Live Load Diagram



### Ultimate Load

Dead load factor= 1.4

Live load factor= 1.6

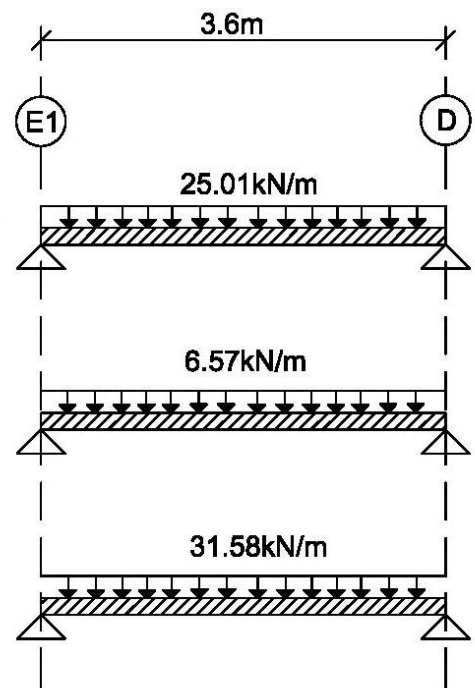
4. Ultimate dead load  
=  $17.865\text{kN/m} \times 1.4$   
=  $25.01\text{kN/m}$
5. Ultimate live load  
=  $4.104\text{kN/m} \times 1.6$   
=  $6.57\text{kN/m}$
6. Ultimate load  
=  $25.01\text{kN/m} + 6.57\text{kN/m}$   
=  $31.58\text{kN/m}$

Ultimate dead load

Ultimate live load

Ultimate load

Ultimate Load Diagram



### Reaction

The ultimate load (UDL) is converted into point load before resolving the reaction forces of the beam 2A/ D- E1.

Ultimate load

$$= 31.58\text{kN/m} \times 3.6\text{m} = 113.69\text{kN}$$

Assuming  $\sum M = 0$ ,

$$(113.69\text{kN} \times 1.8\text{m}) - (R_b \times 3.6\text{m}) = 0$$

$$204.64\text{kNm} - 3.6R_b = 0$$

$$-3.6R_b = -204.64\text{kNm}$$

$$R_b = 204.64\text{kNm} / 3.6\text{m}$$

$$R_b = 56.85\text{kN}$$

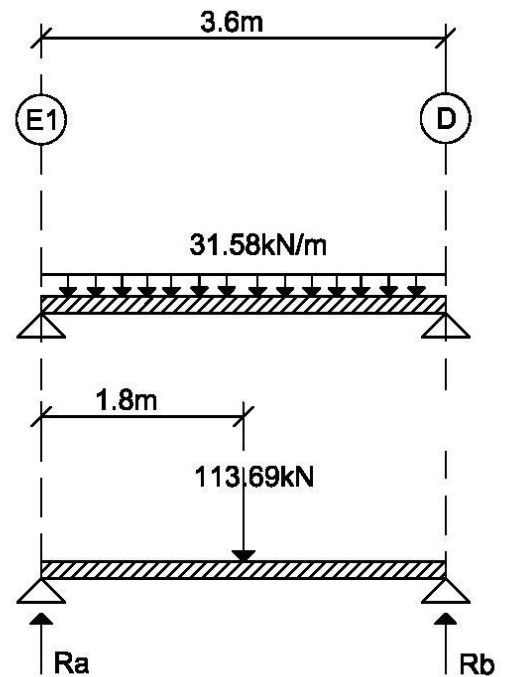
Assuming  $\sum F = 0$ ,

$$113.69\text{kN} - R_a - R_b = 0$$

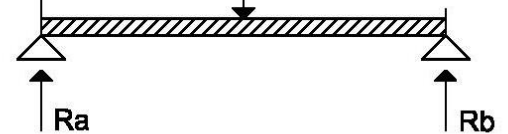
$$113.69\text{kN} - 56.85\text{kN} - R_a = 0$$

$$R_a = 56.84\text{kN}$$

Ultimate load



Reaction



### Shear force diagram

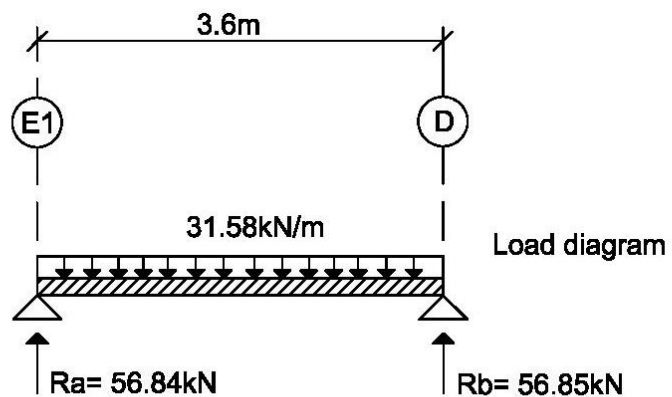
At point E1, 56.84kN of Ra is acting upwards.

From E1 to D, there is a UDL of 31.58kN/m acting downwards, therefore

$$31.58\text{kN/m} \times 3.6\text{m} = 113.688\text{kN}$$

$$56.84\text{kN} - 113.688\text{kN} = -56.848\text{kN}$$

At point D, another 56.85kN of Rb acting upwards,  
thus making the beam balance.



Load diagram

### Bending moment diagram

Positive area – negative area in shear force diagram

(+ve)

$$= (1/2) \times 56.84 \times (3.6/2)$$

$$= (1/2) \times 56.84 \times 1.8$$

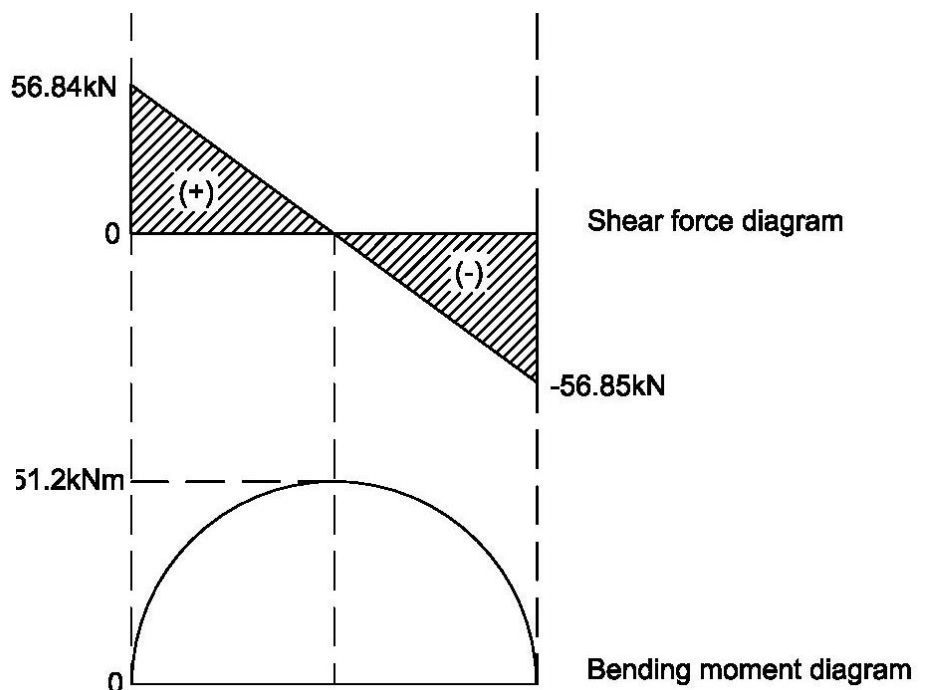
$$= 51.156 \approx 51.2$$

(-ve)

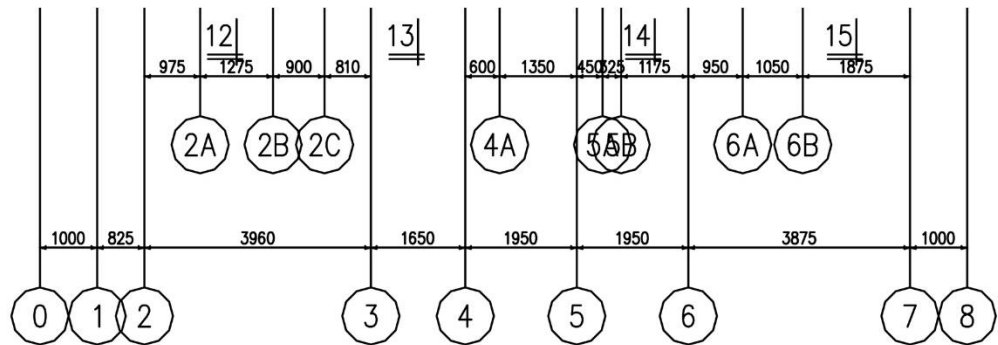
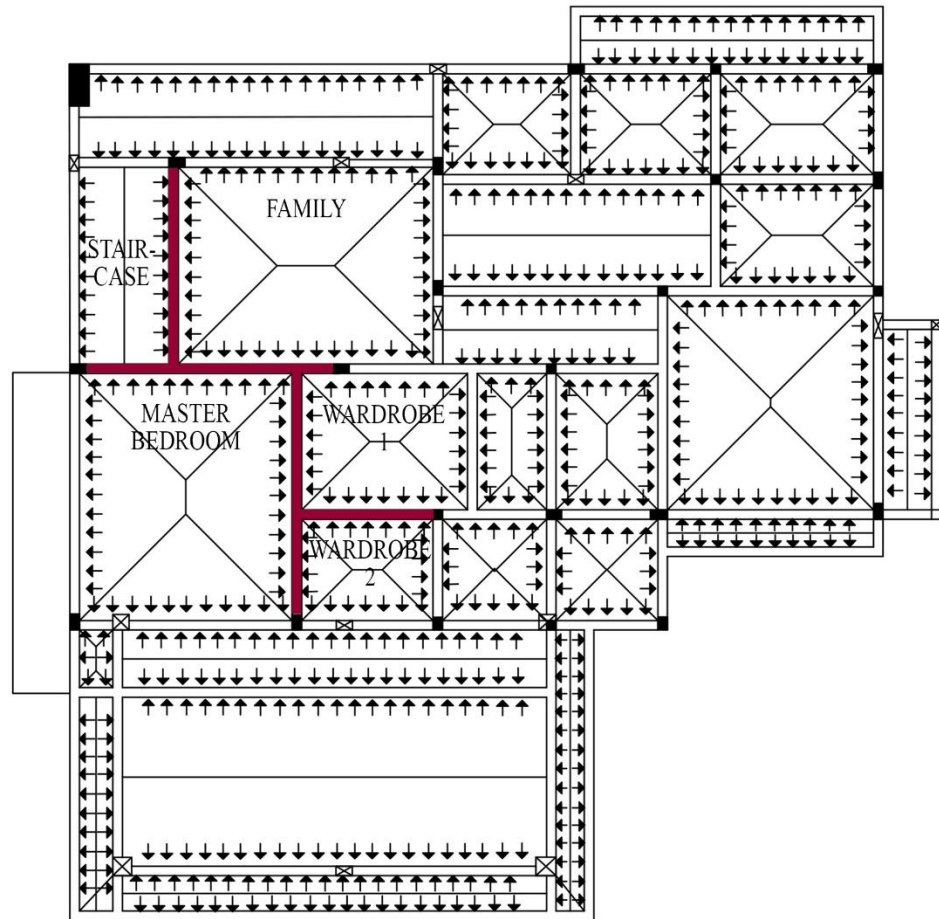
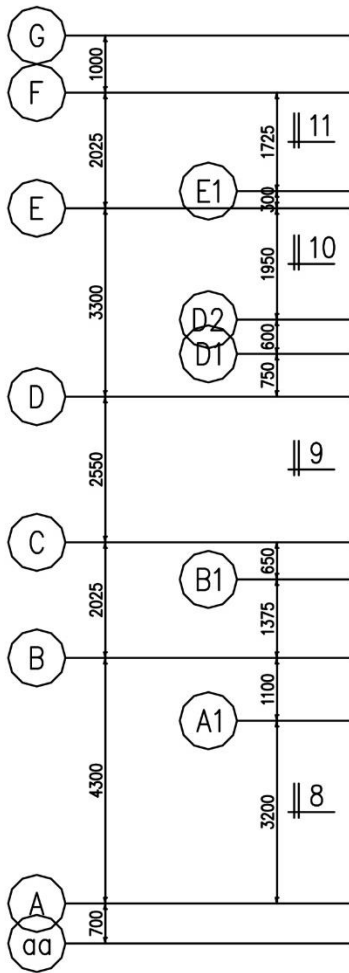
$$= (1/2) \times (-56.85) \times (3.6/2)$$

$$= (1/2) \times (-56.85) \times 1.8$$

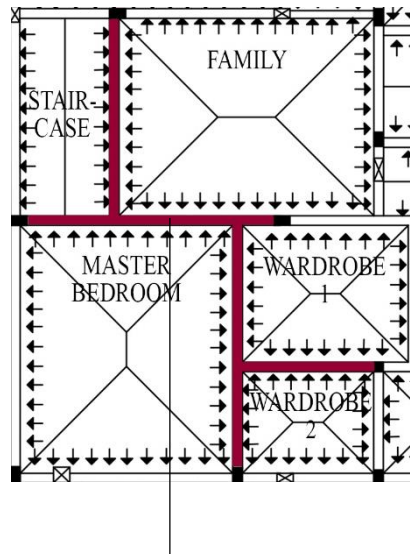
$$= -51.165 \approx -51.2$$



## Analysis on beam **D/ 1-3**



LOAD DISTRIBUTION DIAGRA- FIRST FLOOR  
(NTS)

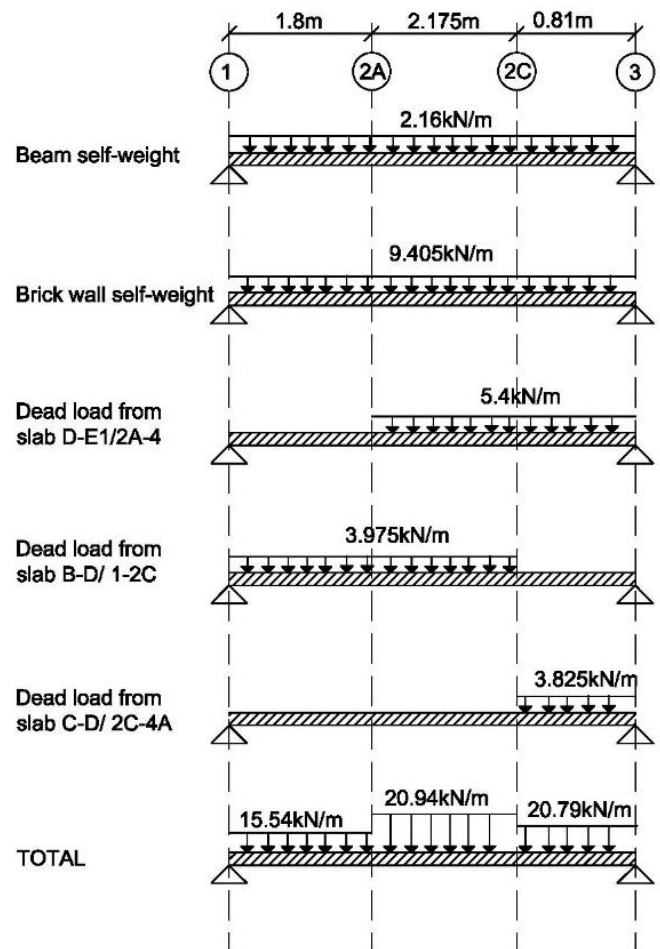


Beam D/ 1-3 (loads from wardrobe 1, family room and master bedroom are acting on it)

#### Dead loads acting on beam D/ 1-3

- Slab self-weight  
 $= \text{Slab thickness} \times \text{concrete density}$   
 $= 0.125\text{m} \times 24\text{kN/m}^3$   
 $= 3\text{kN/m}^2$
- Beam self-weight  
 $= \text{Beam size} \times \text{concrete density}$   
 $= (0.15\text{m} \times 0.6\text{m}) \times 24\text{kN/m}^3$   
 $= 2.16\text{kN/m}$
- Brick wall self-weight  
 $= \text{Wall height} \times \text{thickness} \times \text{density}$   
 $= 3.3\text{m} \times 0.15\text{m} \times 19\text{kN/m}^3$   
 $= 9.405\text{kN/m}$
- Dead load from the slab D- E1/ 2A-4  
 $= 3\text{kN/m}^2 \times (L_x/2)$   
 $= 3\text{kN/m}^2 \times (3.6/2)$   
 $= 5.4\text{kN/m}$
- Dead load from the slab B- D/ 1-2C  
 $= 3\text{kN/m}^2 \times (L_x/2) \times (2/3)$   
 $= 3\text{kN/m}^2 \times (3.975/2) \times (2/3)$   
 $= 3.975\text{kN/m}$
- Dead load from the slab C- D/ 2C-4A  
 $= 3\text{kN/m}^2 \times (L_x/2)$   
 $= 3\text{kN/m}^2 \times (2.55/2)$   
 $= 3.825\text{kN/m}$

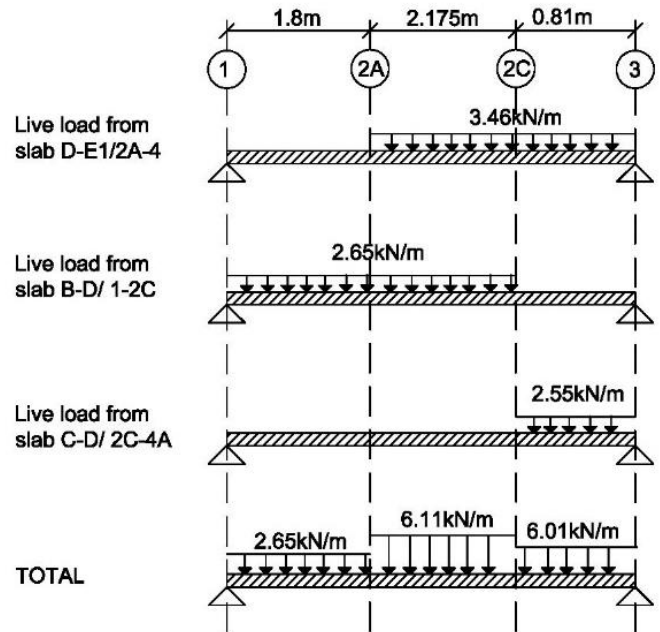
#### Total Dead Load Diagram



### Live loads acting on beam D/ 1-3

1. Live load from slab D- E1/ 2A-4  
 $= \text{live load of family room} \times (L_x / 2)$   
 $= 1.92 \text{ kN/m}^2 \times (3.6 \text{ m} / 2)$   
 $= 3.46 \text{ kN/m}$
2. Live load from slab B- D/ 1-2C  
 $= \text{live load of master bedroom} \times (L_x / 2) \times (2/3)$   
 $= 2 \text{ kN/m}^2 \times (3.975 \text{ m} / 2) \times (2/3)$   
 $= 2.65 \text{ kN/m}$
3. Live load from slab C- D/ 2C-4A  
 $= \text{live load of wardrobe 1} \times (L_x / 2)$   
 $= 2 \text{ kN/m}^2 \times (2.55 \text{ m} / 2)$   
 $= 2.55 \text{ kN/m}$

Total Live Load Diagram



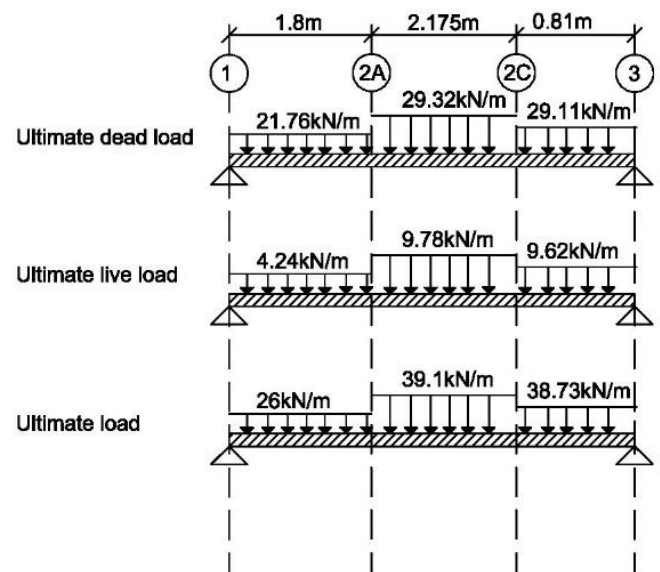
### Ultimate Load

Dead load factor= 1.4

Live load factor= 1.6

1. Ultimate dead load at 1- 2A  
 $= 15.54 \text{ kN/m} \times 1.4$   
 $= 21.76 \text{ kN/m}$   
 Ultimate dead load at 2A- 2C  
 $= 20.94 \text{ kN/m} \times 1.4$   
 $= 29.32 \text{ kN/m}$   
 Ultimate dead load at 2C- 3  
 $= 20.79 \text{ kN/m} \times 1.4$   
 $= 29.11 \text{ kN/m}$
2. Ultimate live load at 1- 2A  
 $= 2.65 \text{ kN/m} \times 1.6$   
 $= 4.24 \text{ kN/m}$   
 Ultimate live load at 2A- 2C  
 $= 6.11 \text{ kN/m} \times 1.6$   
 $= 9.78 \text{ kN/m}$   
 Ultimate live load at 2C- 3  
 $= 6.01 \text{ kN/m} \times 1.6$   
 $= 9.62 \text{ kN/m}$
3. Ultimate load at 1- 2A  
 $= 21.76 \text{ kN/m} + 4.24 \text{ kN/m}$   
 $= 26 \text{ kN/m}$   
 Ultimate load at 2A- 2C  
 $= 29.32 \text{ kN/m} + 9.78 \text{ kN/m}$   
 $= 39.1 \text{ kN/m}$   
 Ultimate load at 2C- 3  
 $= 29.11 \text{ kN/m} + 9.62 \text{ kN/m}$   
 $= 38.73 \text{ kN/m}$

Ultimate Load Diagram



## Reaction

The ultimate load (UDL) is converted into point load before resolving the reaction forces of the beam D/1-3.

Ultimate load at 1- 2A

$$= 26\text{kN/m} \times 1.8\text{m} = 46.8\text{kN}$$

Ultimate load at 2A- 2C

$$= 39.1\text{kN/m} \times 2.175\text{m} = 85.04\text{kN}$$

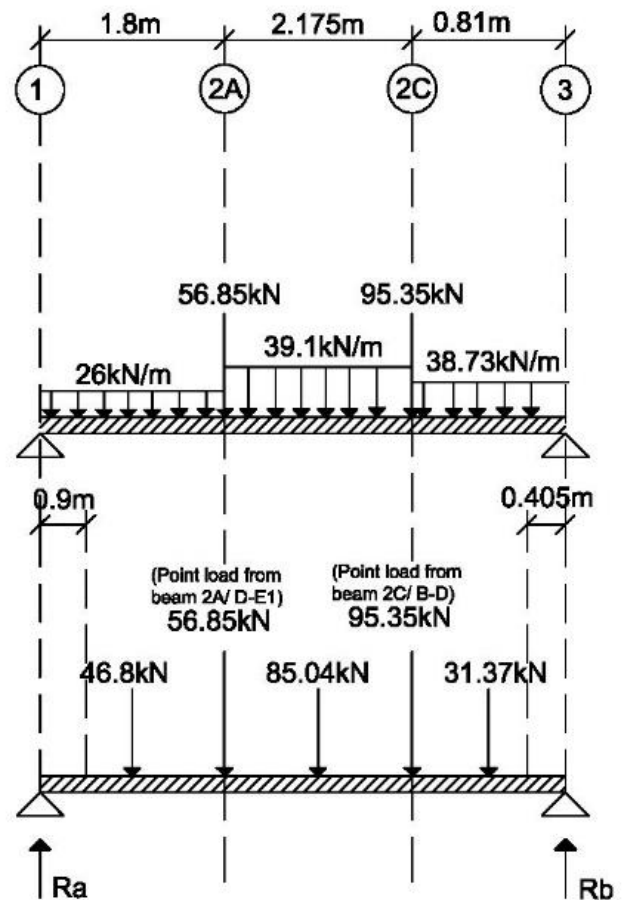
Ultimate load at 2C- 3

$$= 38.73\text{kN/m} \times 0.81\text{m} = 31.37\text{kN}$$

Reaction force,  $R_b$  of beam 2A/D- E1 acting on this beam is taken as the point load which is 56.85kN, and also reaction force,  $R_a$  of beam 2C/B- D which is 95.35kN.

Ultimate load

Reaction



Assuming  $\sum M = 0$ ,

$$(46.8\text{kN} \times 0.9\text{m}) + (56.85\text{kN} \times 1.8\text{m}) + (85.04\text{kN} \times 2.8875\text{m}) + (95.35\text{kN} \times 3.975\text{m}) + (31.37\text{kN} \times 4.38\text{m}) - (R_b \times 4.785\text{m}) = 0$$

$$42.12\text{kNm} + 102.33\text{kNm} + 245.553\text{kNm} + 379.02\text{kNm} + 137.40\text{kNm} - 4.785R_b = 0$$

$$906.423\text{kNm} - 4.785R_b = 0$$

$$-4.785R_b = -906.423\text{kNm}$$

$$R_b = 906.423\text{kNm} / 4.785\text{m}$$

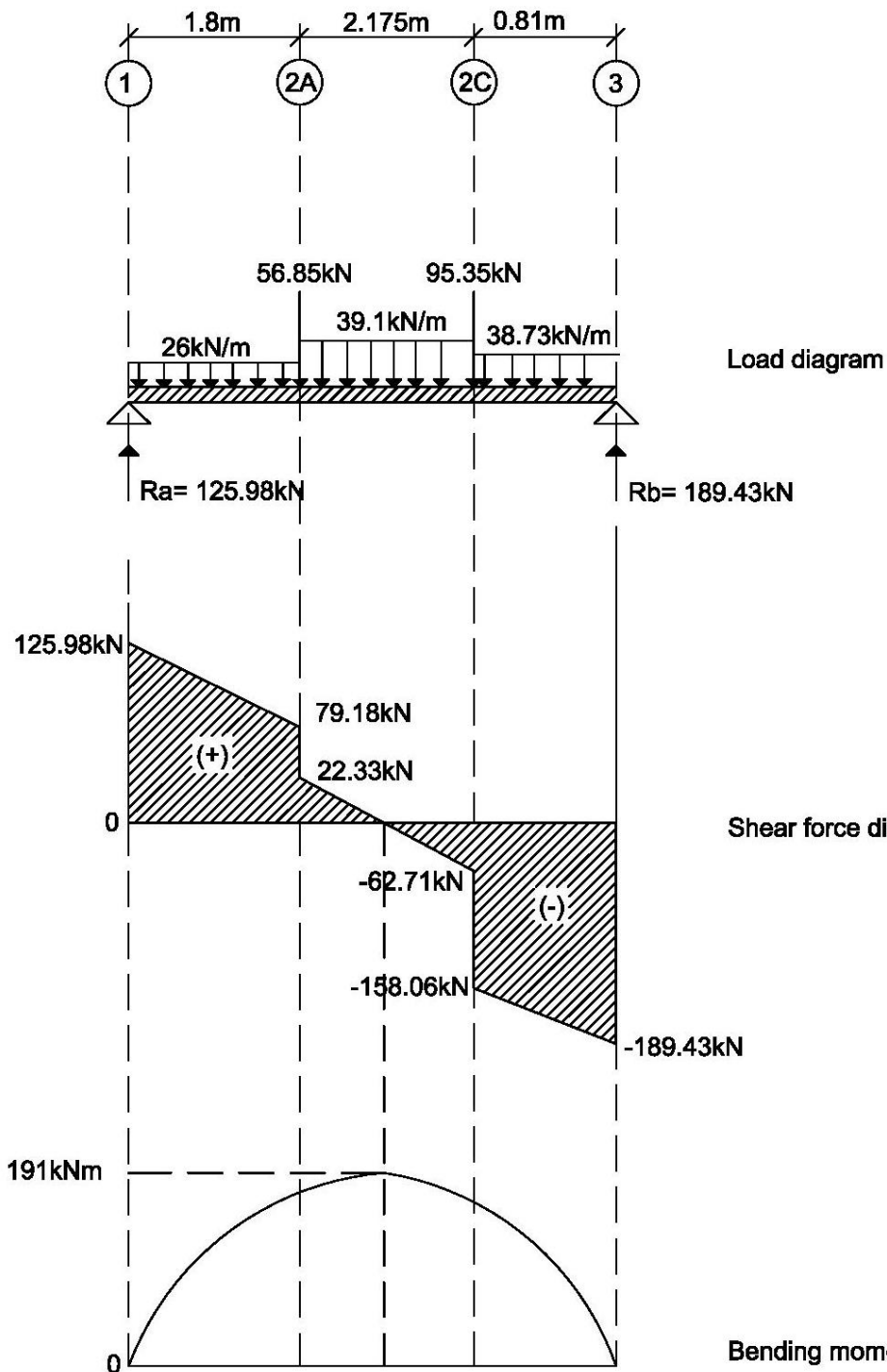
$$R_b = 189.43\text{kN}$$

Assuming  $\sum F = 0$ ,

$$46.8\text{kN} + 56.85\text{kN} + 85.04\text{kN} + 95.35\text{kN} + 31.37\text{kN} - R_a - R_b = 0$$

$$315.41\text{kN} - 189.43\text{kN} - R_a = 0$$

$$R_a = 125.98\text{kN}$$



### Shear force diagram

At point 1,  $125.98\text{kN}$  of  $R_a$  is acting upwards.

From 1 to 2A, there is a UDL of  $26\text{kN/m}$  acting downwards, therefore

$$26\text{kN/m} \times 1.8\text{m} = 46.8\text{kN}$$

$$125.98\text{kN} - 46.8\text{kN} = 79.18\text{kN}$$

At point 2A, there is a point load of  $56.85\text{kN}$  ( $R_b$  of beam 2A/D-E1) acting downwards, therefore

$$79.18\text{kN} - 56.85\text{kN} = 22.33\text{kN}$$

From 2A to 2C, there is a UDL of  $39.1\text{kN/m}$  acting downwards, therefore

$$39.1\text{kN/m} \times 2.175\text{m} =$$

$$85.0425\text{kN}$$

$$22.33\text{kN} - 85.0425\text{kN} =$$

$$-62.7125\text{kN}$$

At point 2C, there is another point load of  $95.35\text{kN}$  ( $R_a$  of beam 2C/ B- D) acting downwards, therefore,

$$-62.71\text{kN} - 95.35\text{kN} = -158.0625$$

From 2C to 3, there is a UDL of  $38.73\text{kN/m}$  acting downwards, therefore

$$38.73\text{kN/m} \times 0.81\text{m} = 31.3713$$

$$-158.0625 - 31.3713 = -189.43$$

Which is then resolved by  $R_b$  of  $189.43\text{kN}$  that is acting upwards.

### Bending moment diagram

Positive area – negative area in shear force diagram

(+ve)

$$= [(1/2) \times (125.98 + 79.18) \times 1.8] + [(1/2) \times 0.57 \times 22.33]$$

$$= 184.644 + 6.36$$

$$= 191.04 \approx 191$$

(-ve)

$$= [(1/2) \times (-62.71) \times (2.175 - 0.57)] + [(1/2) \times (158.06 + 189.43) \times 0.81]$$

$$= 50.32 + 140.73$$

$$= 191.05 \approx 191$$