

Beam Analysis

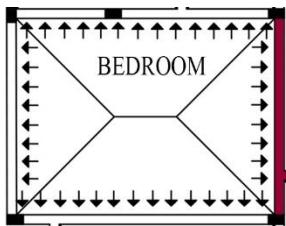
Load Distribution Diagram

Identify One-Way Slab or Two-Way Slab (to identify the distribution of load from slab to beam).

L_y = longer side of slab L_x = shorter side of the slab

When $L_y/ L_x > 2$, it is a one-way slab.

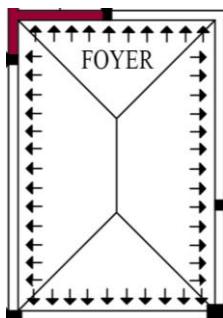
When $L_y/ L_x < 2$ or $= 2$, it is a two-way slab.



1. Bedroom (D-E1/ 1-3)
 $L_y/ L_x = 4.785/ 3.6$
 $= 1.329$ (two-way slab)



2. Staircase (D-F/ 3-4)
 $L_y/ L_x = 5.325/ 1.65$
 $= 3.227$ (one-way slab)

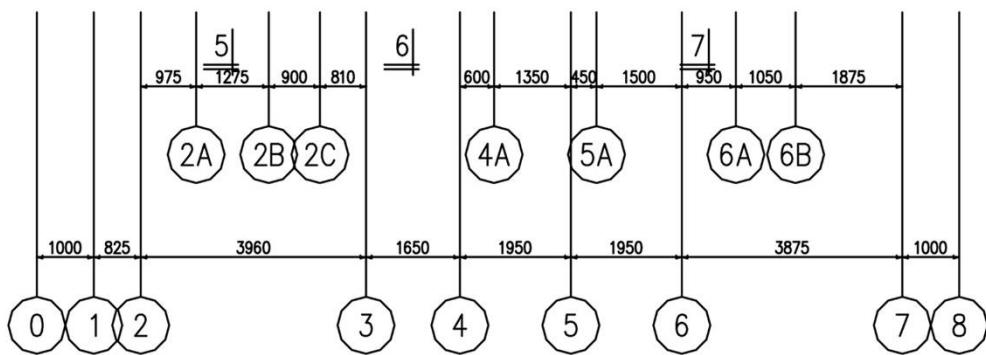
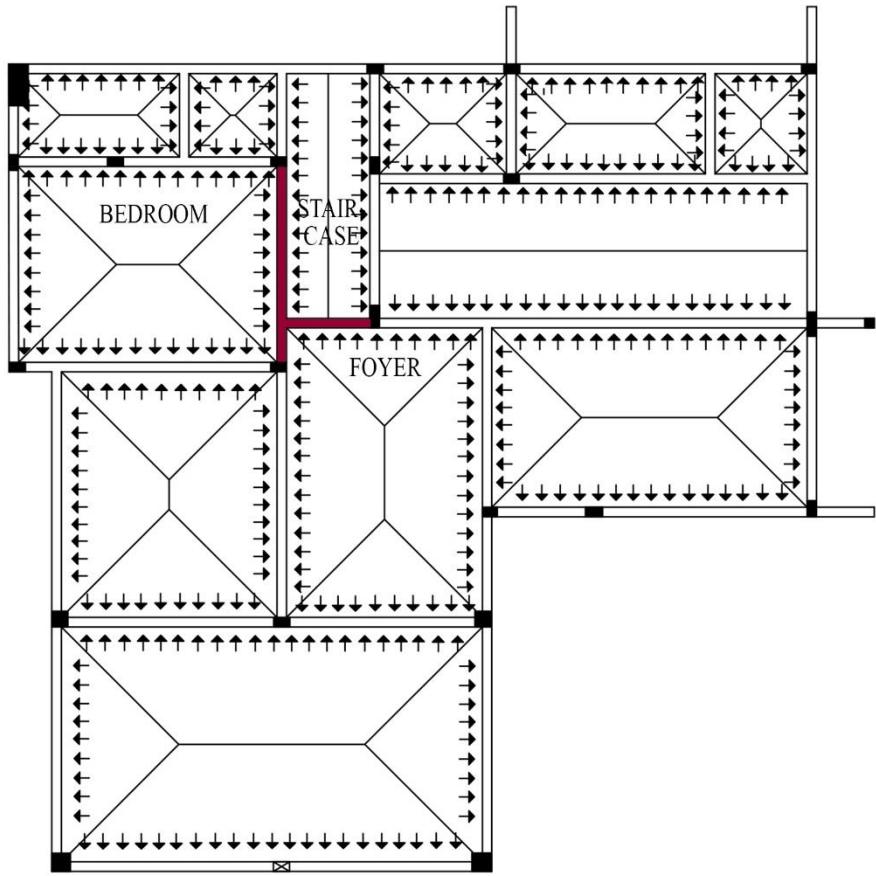
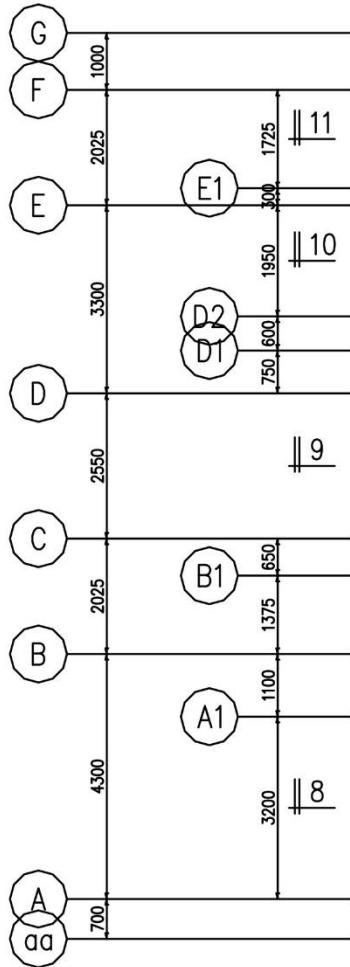


3. Foyer (B-D1/ 3-5)
 $L_y/ L_x = 5.325/ (1.65 + 1.95)$
 $= 1.479$ (two-way slab)

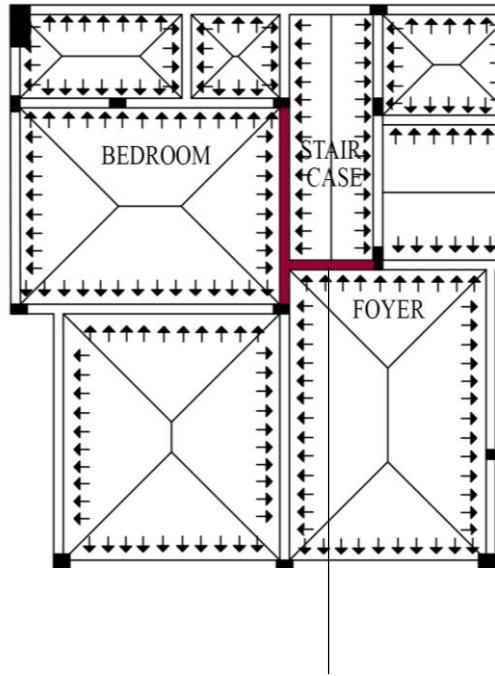
Live Load of spaces according to UBBL

- A/V Room: 1.92kN/m²
- Balcony: 1.5 kN/m²
- Bathroom: 2.0 kN/m²
- Bedroom: 2.0 kN/m²
- Car porch: 5.0 kN/m²
- Dining Room: 2.0 kN/m²
- Dressing Room: 2.0 kN/m²
- Dry Kitchen: 3.0 kN/m²
- Family Room: 1.92 kN/m²
- Foyer: 2.0 kN/m²
- Living Room: 2.0 kN/m²
- Roof: 0.5 kN/m²
- Stairs: 2.0 kN/m²
- Study Room: 2.0 kN/m²
- Utility Room: 2.0 kN/m²
- Passage: Based on the room passage is leading to.

Analysis on beam D1/ 3-4



LOAD DISTRIBUTION DIAGRAM- GROUND FLOOR
(NTS)

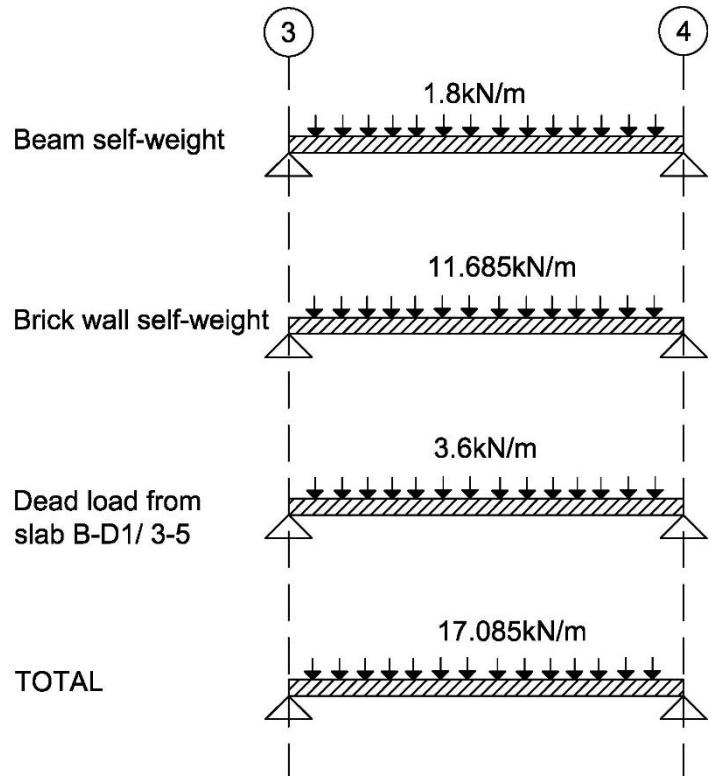


Beam D1/ 3-4 (only loads from foyer is acting on it)

Dead loads acting on beam D1/ 3-4

1. Slab self-weight
 $= \text{Slab thickness} \times \text{concrete density}$
 $= 0.125\text{m} \times 24\text{kN/m}^3$
 $= 3\text{kN/m}^2$
2. Beam self-weight
 $= \text{Beam size} \times \text{concrete density}$
 $= (0.15\text{m} \times 0.5\text{m}) \times 24\text{kN/m}^3$
 $= 1.8\text{kN/m}$
3. Brick wall self-weight
 $= \text{Wall height} \times \text{thickness} \times \text{density}$
 $= 4.1\text{m} \times 0.15\text{m} \times 19\text{kN/m}^3$
 $= 11.685\text{kN/m}$
4. Dead load from the slab B-D1/ 3-5
 $= 3\text{kN/m}^2 \times (L_x/2) \times (2/3)$
 $= 3\text{kN/m}^2 \times (3.6/2) \times (2/3)$
 $= 3.6\text{kN/m}$
5. Total dead load
 $= 1.8 + 11.685 + 3.6$
 $= 17.085 \text{ kN/m}$

Total Dead Load Diagram



Live loads acting on beam D1/ 3-4

1. Live load on beam D1/ 3-4

$$= \text{live load from foyer } x$$

$$= (L_x/ 2) \times (2/3)$$

$$= 2\text{kN/m}^2 \times (3.6\text{m}/ 2) \times (2/3)$$

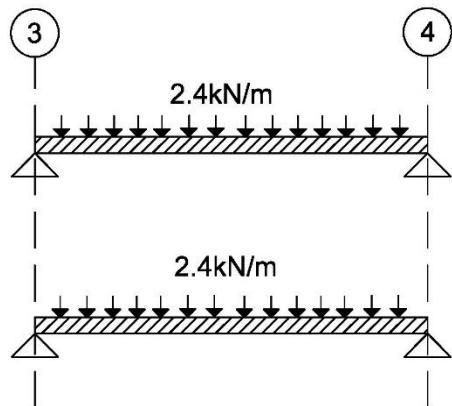
$$= 2.4\text{kN/m}$$
2. Total live load

$$= 2.4\text{kN/m}$$

Live load from slab B-D1/ 3-5

TOTAL

Total Live Load Diagram



Ultimate Load

Dead load factor= 1.4

Live load factor= 1.6

1. Ultimate dead load

$$= 17.085\text{kN/m} \times 1.4$$

$$= 23.92\text{kN/m}$$
2. Ultimate live load

$$= 2.4\text{kN/m} \times 1.6$$

$$= 3.84\text{kN/m}$$
3. Ultimate load

$$= 23.92\text{kN/m} + 3.84\text{kN/m}$$

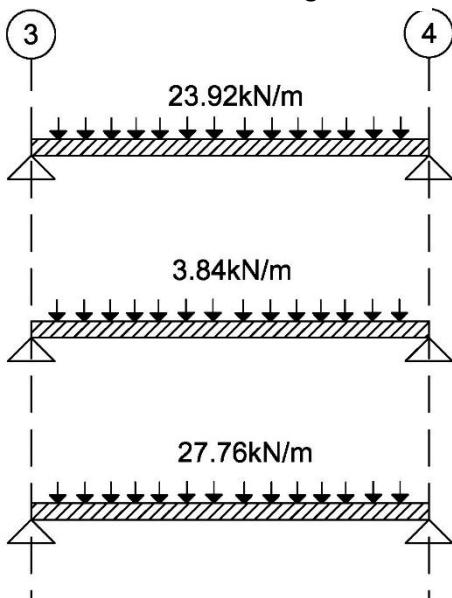
$$= 27.76\text{kN/m}$$

Ultimate dead load

Ultimate live load

Ultimate load

Ultimate Load Diagram



Reaction

The ultimate load (UDL) is converted into point load before resolving the reaction forces of the beam D1/ 3-4.

$$27.76\text{kN/m} \times 1.65\text{m} = 45.8\text{kN}$$

Assuming $\sum M = 0$,

$$[45.8\text{kN} \times (1.65\text{m}/ 2)] - (R_b \times 1.65\text{m}) = 0$$

$$(45.8\text{kN} \times 0.825\text{m}) - 1.65R_b = 0$$

$$37.785\text{kNm} - 1.65R_b = 0$$

$$-1.65R_b = -37.785\text{kNm}$$

$$R_b = 37.785\text{kNm} / 1.65\text{m}$$

$$R_b = 22.9\text{kN}$$

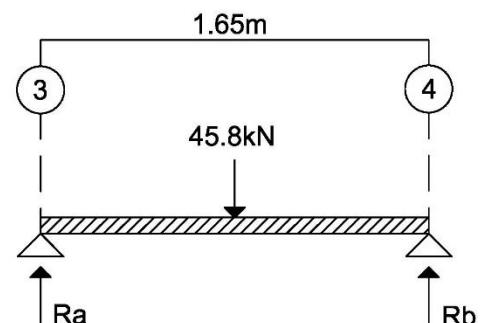
Assuming $\sum F = 0$,

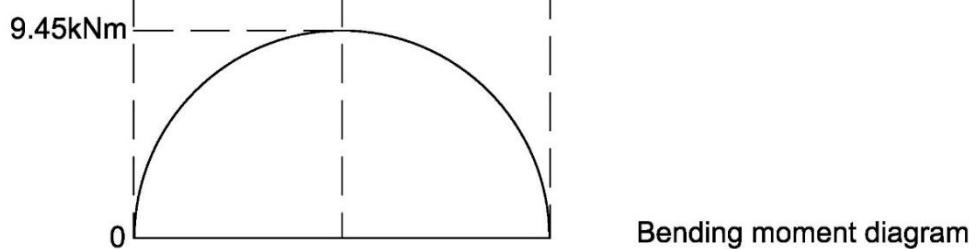
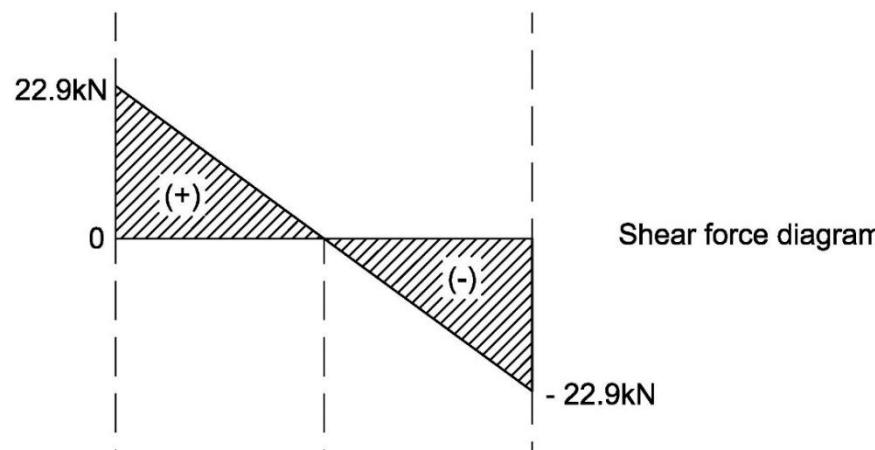
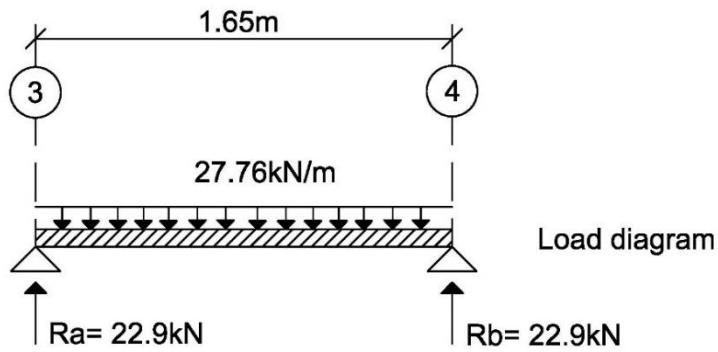
$$45.8\text{kN} - R_a - R_b = 0$$

$$45.8\text{kN} - 22.9\text{kN} - R_a = 0$$

$$R_a = 45.8\text{kN} - 22.9\text{kN}$$

$$R_a = 22.9\text{kN}$$





Shear force diagram

At point 3, 22.9kN of R_a is acting upwards.

From 3 to 4, there is a UDL of 27.76kN/m acting downwards, therefore

$$27.76\text{kN/m} \times 1.65\text{m} = 45.8\text{kN}$$

$$22.9\text{kN} - 45.8\text{kN} = -22.9\text{kN}$$

At point 4, another 22.9kN of R_b acting upwards, making the beam balance.

Bending moment diagram

Positive area – negative area in shear force diagram

(+ve)

$$= (1/2) \times 22.9 \times 0.825$$

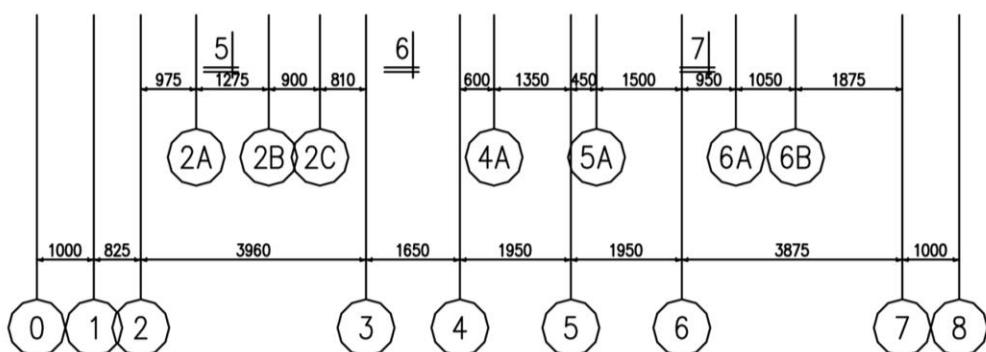
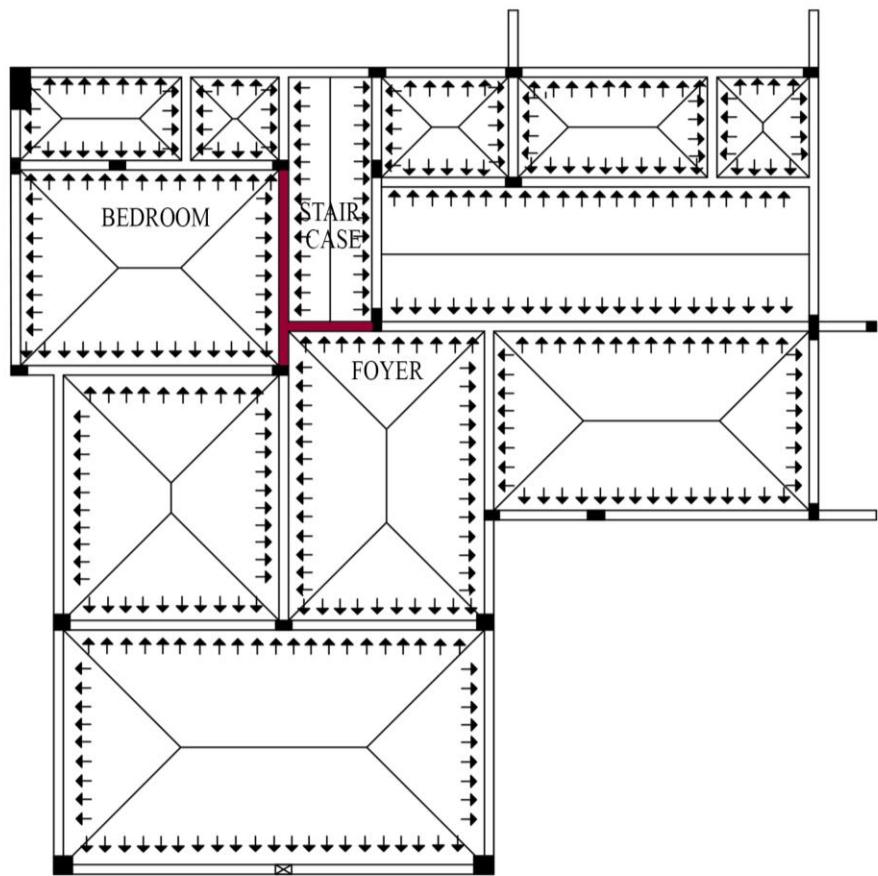
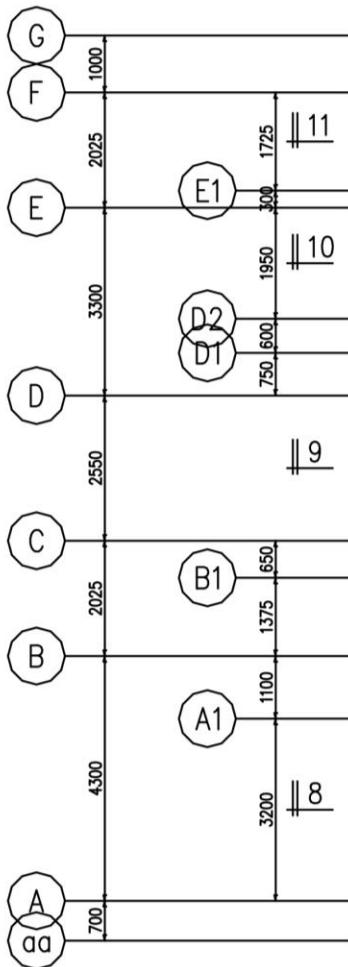
$$= 9.45$$

(-ve)

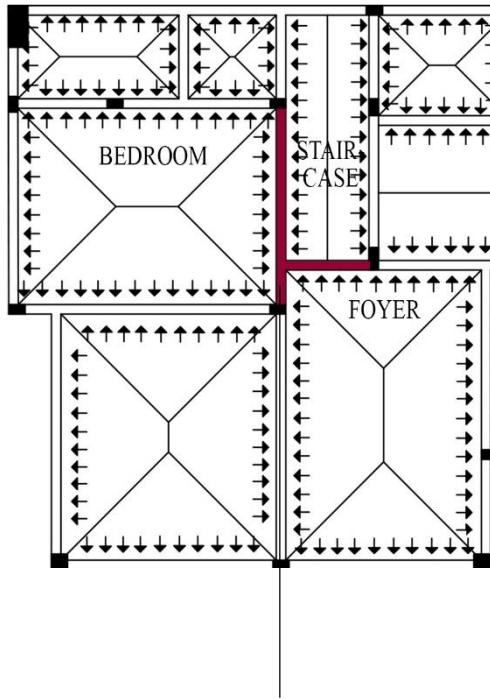
$$= (1/2) \times (-22.9) \times 0.825$$

$$= -9.45$$

Analysis on beam 3/ D- E1



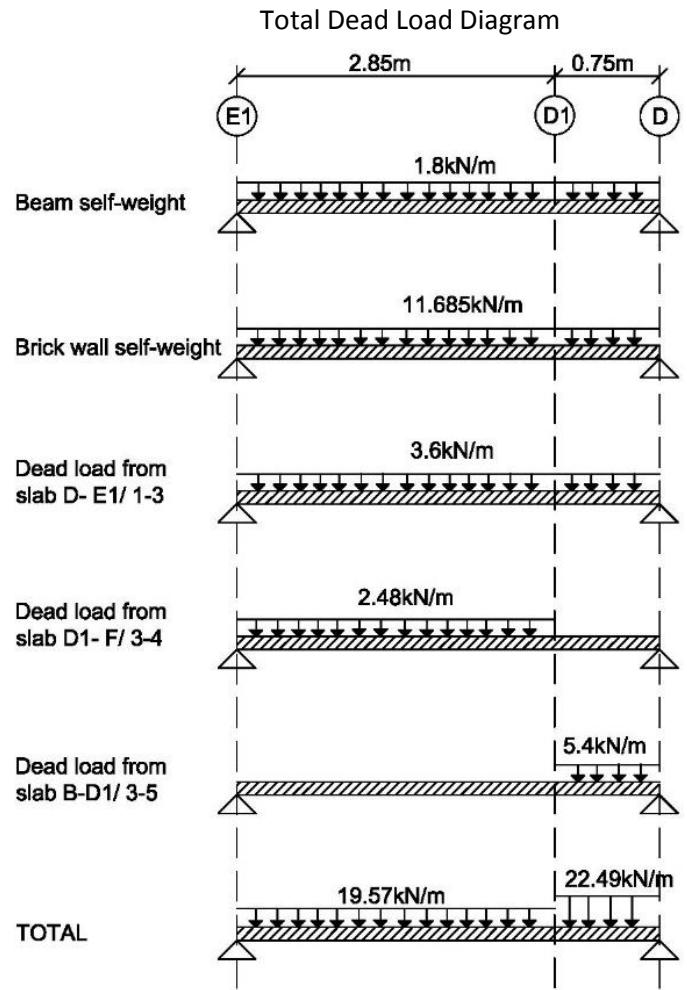
LOAD DISTRIBUTION DIAGRAM- GROUND FLOOR
(NTS)



Beam 3/ D- E1 (loads from bedroom, staircase and foyer are acting on it)

Dead loads acting on beam 3/ D- E1

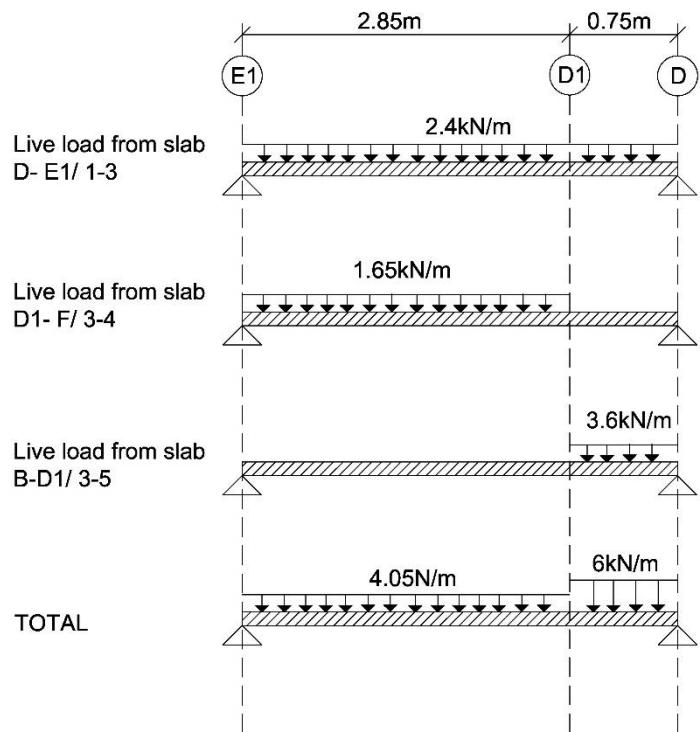
1. Slab self-weight
= Slab thickness x concrete density
= $0.125\text{m} \times 24\text{Kn/m}^3$
= 3kN/m^2
2. Beam self-weight
= Beam size x concrete density
= $(0.15\text{m} \times 0.5\text{m}) \times 24\text{kn/m}^3$
= 1.8kN/m
3. Brick wall self-weight
= Wall height x thickness x density
= $4.1\text{m} \times 0.15\text{m} \times 19\text{Kn/m}^3$
= 11.685kN/m
4. Dead load from the slab D- E1/ 1-3
= $3\text{kN/m}^2 \times (L_x/2) \times (2/3)$
= $3\text{kN/m}^2 \times (3.6/2) \times (2/3)$
= 3.6kN/m
5. Dead load from the slab D1- F/ 3-4
= $3\text{kN/m}^2 \times (L_x/2)$
= $3\text{kN/m}^2 \times (1.65/2)$
= 2.48kN/m
6. Dead load from the slab B- D1/ 3-5
= $3\text{kN/m}^2 \times (L_x/2)$
= $3\text{kN/m}^2 \times (3.6/2)$
= 5.4kN/m



Live loads acting on beam 3/ D- E1

1. Live load from slab D- E1/ 1-3
 $= \text{live load of bedroom} \times (L_x/ 2) \times (2/3)$
 $= 2\text{kN/m}^2 \times (3.6\text{m}/ 2) \times (2/3)$
 $= 2.4\text{kN/m}$
2. Live load from slab D1- F/ 3-4
 $= \text{live load of staircase} \times (L_x/ 2)$
 $= 2\text{kN/m}^2 \times (1.65\text{m}/ 2)$
 $= 1.65\text{kN/m}$
3. Live load from slab B- D1/ 3-5
 $= \text{live load of foyer} \times (L_x/ 2)$
 $= 2\text{kN/m}^2 \times (3.6\text{m}/ 2)$
 $= 3.6\text{kN/m}$

Total Live Load Diagram



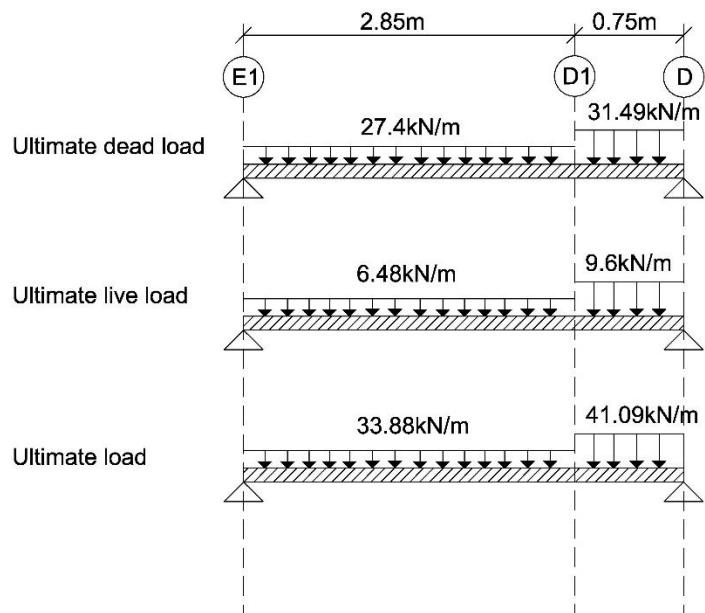
Ultimate Load

Dead load factor= 1.4

Live load factor= 1.6

1. Ultimate dead load at D1- E1
 $= 19.57\text{kN/m} \times 1.4$
 $= 27.4\text{kN/m}$
 Ultimate dead load at D- D1
 $= 22.49\text{kN/m} \times 1.4$
 $= 31.49\text{kN/m}$
2. Ultimate live load at D1- E1
 $= 4.05\text{kN/m} \times 1.6$
 $= 6.48\text{kN/m}$
 Ultimate live load at D- D1
 $= 6\text{kN/m} \times 1.6$
 $= 9.6\text{kN/m}$
3. Ultimate load at D1- E1
 $= 27.4\text{kN/m} + 6.48\text{kN/m}$
 $= 33.88\text{kN/m}$
 Ultimate load at D- D1
 $= 31.49\text{kN/m} + 9.6\text{kN/m}$
 $= 41.09\text{kN/m}$

Ultimate Load Diagram



Reaction

The ultimate load (UDL) is converted into point load before resolving the reaction forces of the beam 3/ D- E1.

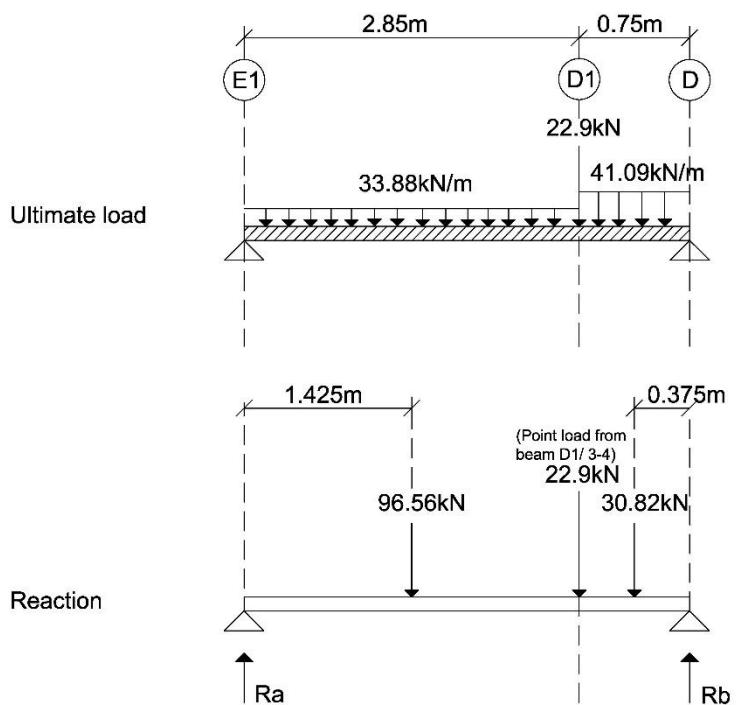
Ultimate load at D1- E1

$$= 33.88 \text{ kN/m} \times 2.85 \text{ m} = 96.56 \text{ kN}$$

Ultimate load at D- D1

$$= 41.09 \text{ kN/m} \times 0.75 \text{ m} = 30.82 \text{ kN}$$

Reaction force, R_a of beam D1/ 3-4 acting on this beam is taken as the point load which is 22.9kN.



Assuming $\sum M = 0$,

$$(96.56 \text{ kN} \times 1.425 \text{ m}) + (22.9 \text{ kN} \times 2.85 \text{ m}) + (30.82 \text{ kN} \times 3.225 \text{ m}) - (R_b \times 3.6 \text{ m}) = 0$$

$$137.598 \text{ kNm} + 65.265 \text{ kNm} + 99.39 \text{ kNm} - 3.6R_b = 0$$

$$302.253 \text{ kNm} - 3.6R_b = 0$$

$$-3.6R_b = -302.253 \text{ kNm}$$

$$R_b = 302.253 \text{ kNm} / 3.6 \text{ m}$$

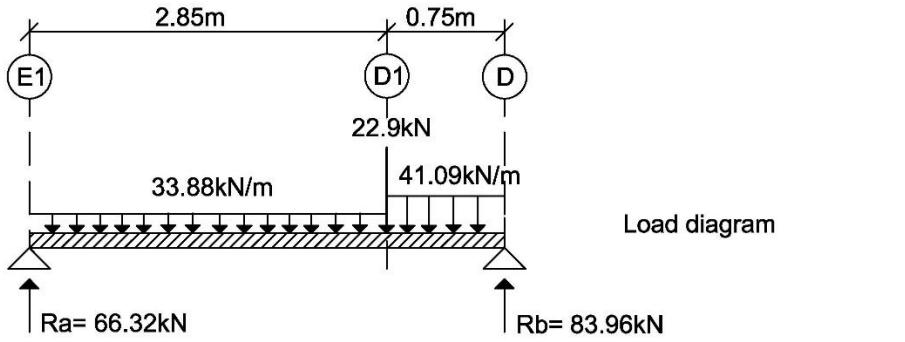
$$R_b = 83.96 \text{ kN}$$

Assuming $\sum F = 0$,

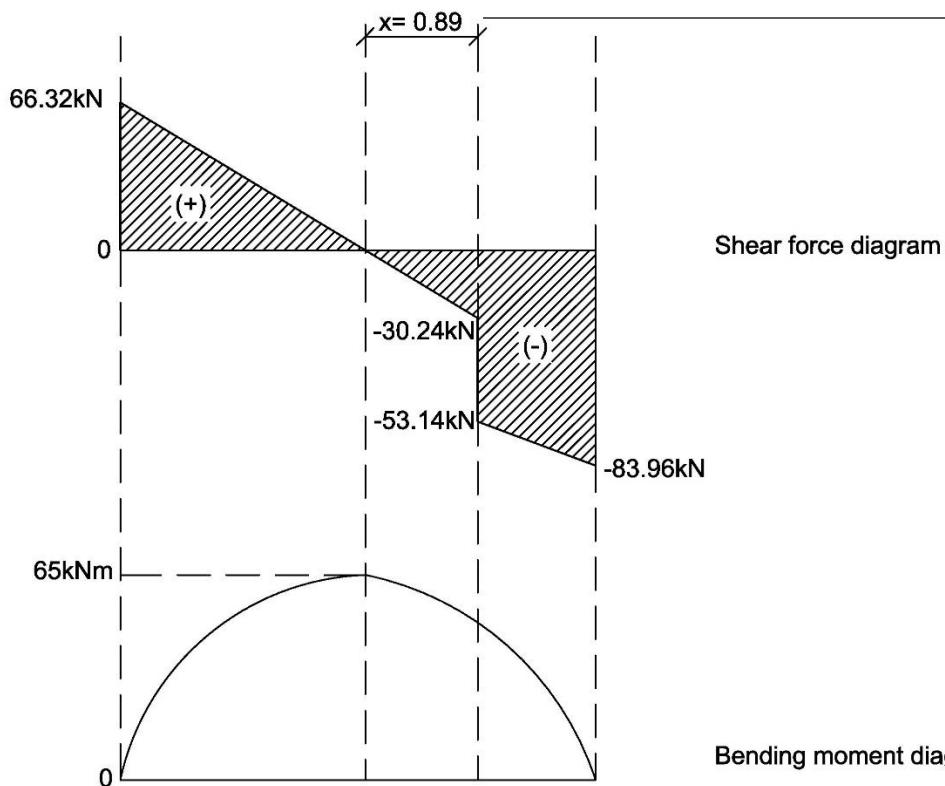
$$96.56 \text{ kN} + 22.9 \text{ kN} + 30.82 \text{ kN} - R_a - R_b = 0$$

$$150.28 \text{ kN} - 83.96 \text{ kN} - R_a = 0$$

$$R_a = 66.32 \text{ kN}$$



$$\begin{aligned}
 \frac{x}{2.85} &= [30.24 \\
 &\quad (30.24 + 66.32)] \\
 \frac{x}{2.85} &= 0.31317 \\
 X &= 0.31317 \times 2.85 \\
 X &= 0.89
 \end{aligned}$$



Bending moment diagram

Shear force diagram

At point E1, 66.32kN of R_a is acting upwards.

From E1 to D1, there is a UDL of 33.88kN/m acting downwards, therefore

$$33.88\text{kN/m} \times 2.85\text{m} = 96.558\text{kN}$$

$$66.32\text{kN} - 96.558\text{kN} = -30.24\text{kN}$$

At point D1, there is a point load of 22.9kN (R_a of beam D1/ 3-4) acting downwards, therefore

$$-30.24\text{kN} - 22.9\text{kN} = -53.14\text{kN}$$

From D1 to D, there is a UDL of 41.09kN/m acting downwards, therefore

$$41.09\text{kN/m} \times 0.75\text{m} = 30.8175\text{kN}$$

$$-53.14\text{kN} - 30.8175\text{kN} = -83.96\text{kN}$$

Which is then resolved by R_b of 83.96kN that is acting upwards.

Bending moment diagram

Positive area – negative area in shear force diagram

(+ve)

$$= (1/2) \times 66.32 \times (2.85 - 0.89)$$

$$= (1/2) \times 66.32 \times 1.96$$

$$= 64.99 \approx 65$$

(-ve)

$$= [(1/2) \times -30.24 \times 0.89] + [(1/2) \times$$

$$[-53.14] + [-83.96] \times 0.75]$$

$$= -13.46 + 51.41$$

$$= -64.87 \approx -65$$

Load Distribution Diagram

Identify One-Way Slab or Two-Way Slab (to identify the distribution of load from slab to beam).

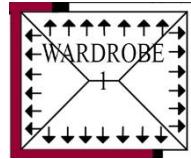
L_y = longer side of slab L_x = shorter side of the slab

When $L_y/ L_x > 2$, it is a one-way slab.

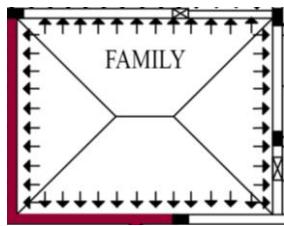
When $L_y/ L_x < 2$ or $= 2$, it is a two-way slab.



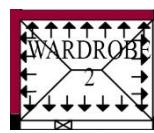
1. Staircase (D-E1/ 1-2A)
 L_y/ L_x
 $= 3.7/ 1.8$
 $= 2.1$ (one-way slab)



5. Wardrobe 1 (C-D/ 2C-4A)
 L_y/ L_x
 $= 3.06/ 2.55$
 $= 1.2$ (two-way slab)



2. Family (D-E1/ 2A-4)
 L_y/ L_x
 $= 4.635/ 3.6$
 $= 1.2875$ (two-way slab)



6. Wardrobe 2 (B-C/ 2C-4)
 L_y/ L_x
 $= 2.46/ 2.025$
 $= 1.215$ (two-way slab)

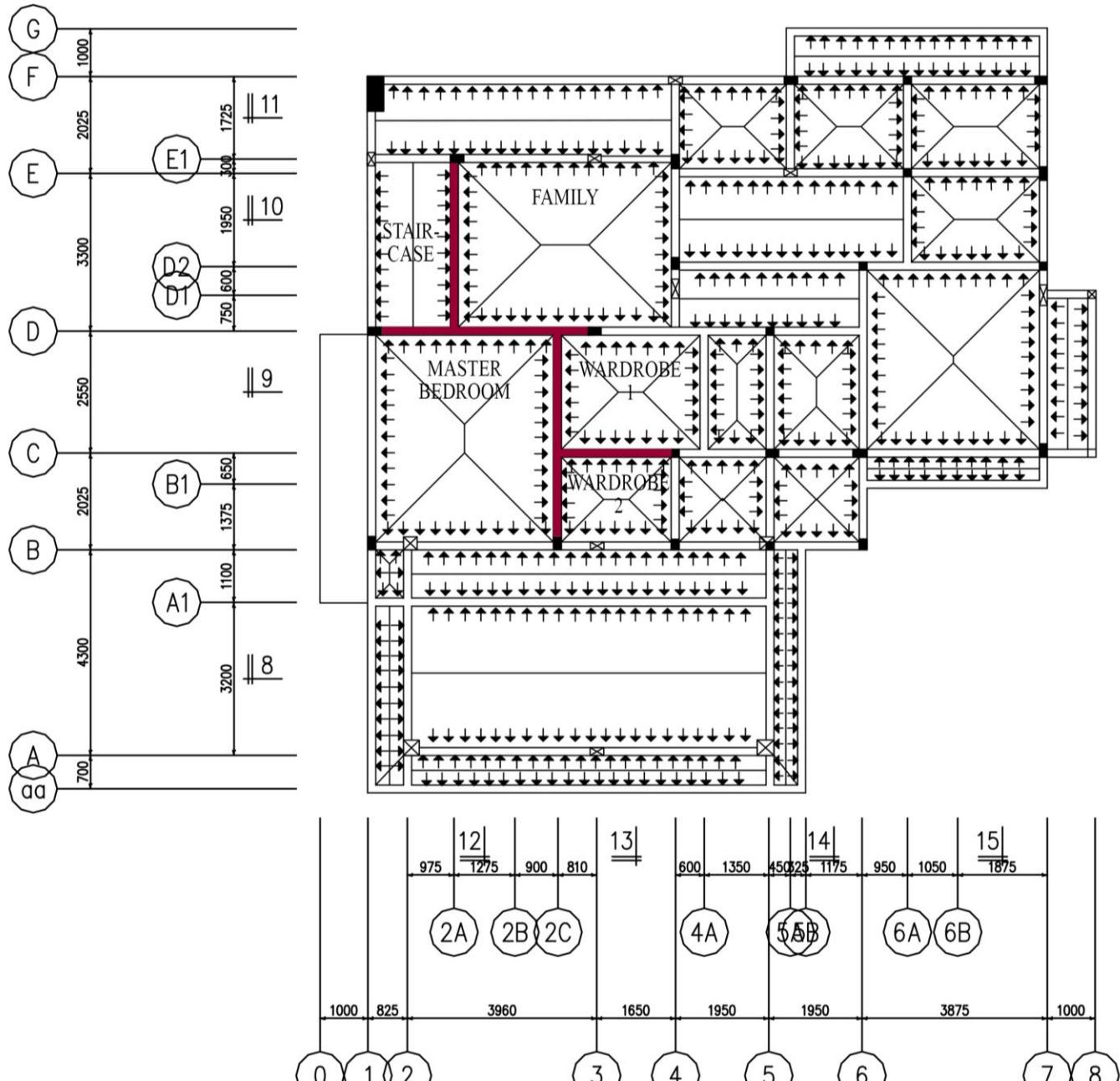


3. Master Bedroom (B-D/ 1-2C)
 L_y/ L_x
 $= 4.575/ 3.975$
 $= 1.15$ (two-way slab)

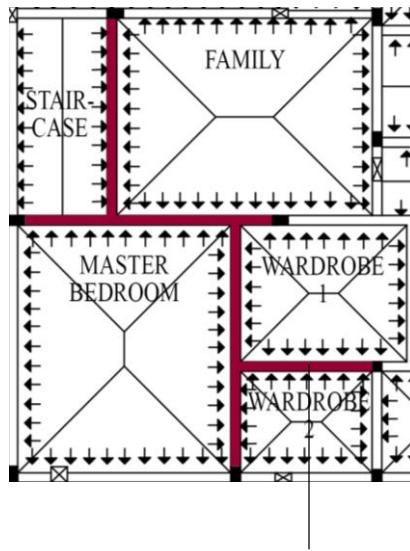
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- Bedroom: 2.0 kN/m
- Car porch: 5.0kN/m
- Dining Room: 2.0 kN/m
- Dressing Room: 2.0kN/m
- Dry Kitchen: 3.0 kN/m
- Family Room: 1.92kN/m
- Foyer: 2.0kN/m
- Living Room: 2.0kN/m
- Roof: 0.5kN/m
- Stairs: 2.0kN/m
- Study Room: 2.0kN/m
- Utility Room: 2.0kN/m
- Passage: Based on the room passage is leading to.

Analysis on beam C/ 2C-4



LOAD DISTRIBUTION DIAGRAM- FIRST FLOOR
(NTS)



Beam C/ 2C- 4 (loads from wardrobe 1 and wardrobe 2 are acting on it)

Dead loads acting on beam C/ 2C- 4

1. Slab self-weight

$$= \text{Slab thickness} \times \text{concrete density}$$

$$= 0.125\text{m} \times 24\text{Kn/m}^3$$

$$= 3\text{kN/ m}^2$$
2. Beam self-weight

$$= \text{Beam size} \times \text{concrete density}$$

$$= (0.15\text{m} \times 0.6\text{m}) \times 24\text{Kn/m}^3$$

$$= 2.16\text{kN/m}$$
3. Dead load from the slab B- C/ 2C-4

$$= 3\text{kN/m}^2 \times (L_x/2)$$

$$= 3\text{kN/m}^2 \times (2.025/2)$$

$$= 3.0375\text{kN/m}$$
4. Dead load from the slab C- D/ 2C-4A

$$= 3\text{kN/m}^2 \times (L_x/2)$$

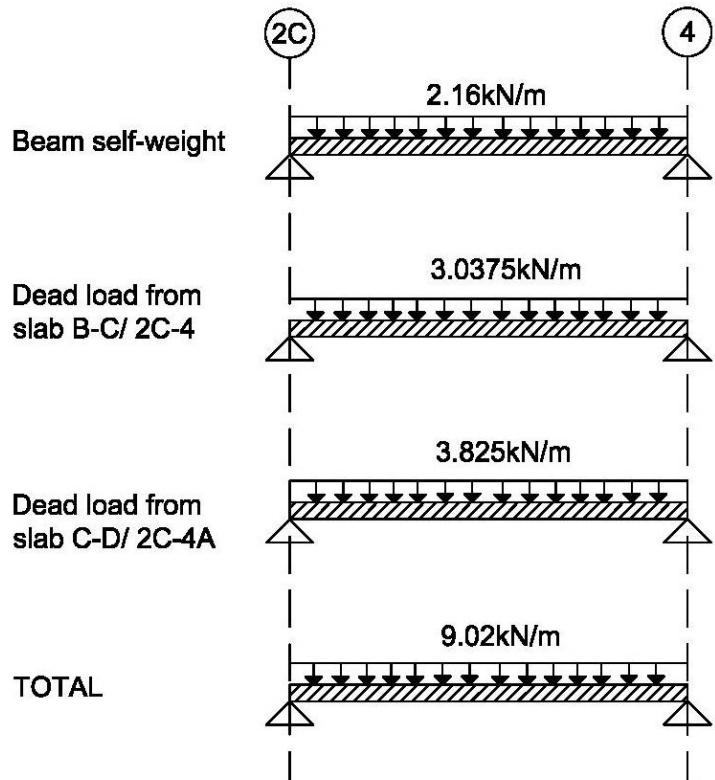
$$= 3\text{kN/m}^2 \times (2.55/2)$$

$$= 3.825\text{kN/m}$$
5. Total dead load

$$= 2.16\text{kN/m} + 3.0375\text{kN/m} + 3.825\text{kN/m}$$

$$= 9.02\text{kN/m}$$

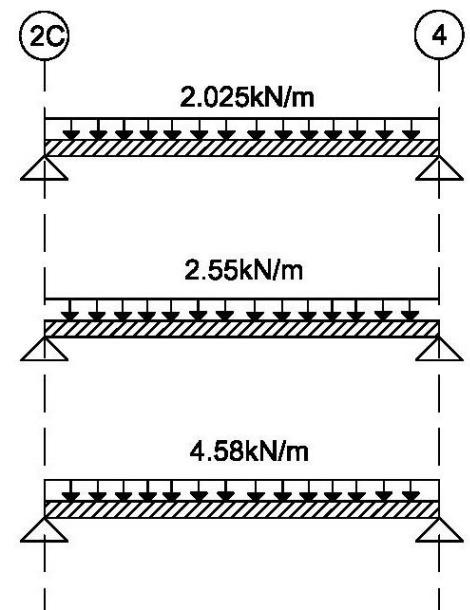
Total Dead Load Diagram



Live loads acting on beam C/ 2C- 4

1. Live load from slab B- C/ 2C-4
 $= \text{live load of wardrobe} \times (L_x/ 2)$
 $= 2\text{kN/m}^2 \times (2.025\text{m}/ 2)$
 $= 2.025\text{kN/m}$
2. Live load from slab C- D/ 2C-4A
 $= \text{live load of wardrobe} \times (L_x/ 2)$
 $= 2\text{kN/m}^2 \times (2.55\text{m}/ 2)$
 $= 2.55\text{kN/m}$
3. Total live load
 $= 2.025\text{kN/m} + 2.55\text{kN/m}$
 $= 4.58\text{kN/m}$

Total Live Load Diagram



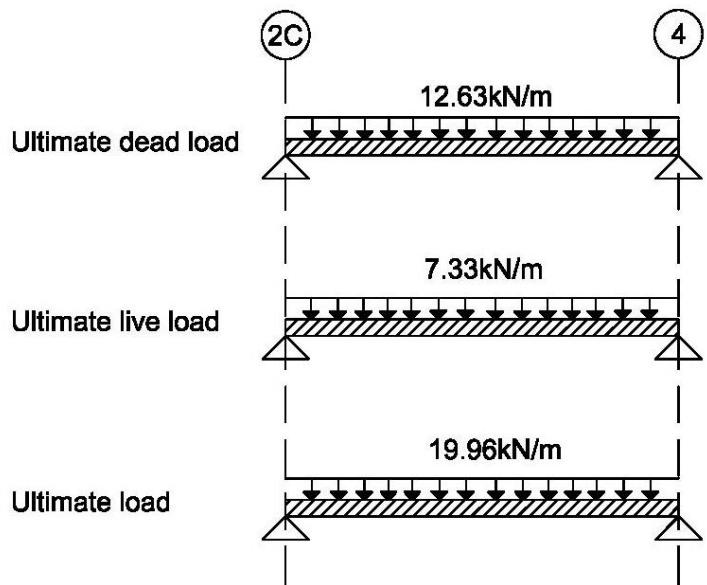
Ultimate Load

Dead load factor= 1.4

Live load factor= 1.6

1. Ultimate dead load
 $= 9.02\text{kN/m} \times 1.4$
 $= 12.63\text{kN/m}$
2. Ultimate live load
 $= 4.58\text{kN/m} \times 1.6$
 $= 7.33\text{kN/m}$
3. Ultimate load
 $= 12.63\text{kN/m} + 7.33\text{kN/m}$
 $= 19.96\text{kN/m}$

Ultimate Load Diagram



Reaction

The ultimate load (UDL) is converted into point load before resolving the reaction forces of the beam C/ 2C- 4.

Ultimate load

$$= 19.96 \text{ kN/m} \times 2.46 \text{ m} = 49.10 \text{ kN}$$

Assuming $\sum M = 0$,

$$(49.10 \text{ kN} \times 1.23 \text{ m}) - (R_b \times 2.46 \text{ m}) = 0$$

$$60.393 \text{ kNm} - 2.46 R_b = 0$$

$$-2.46 R_b = -60.393 \text{ kNm}$$

$$R_b = 60.393 \text{ kNm} / 2.46 \text{ m}$$

$$R_b = 24.55 \text{ kN}$$

Assuming $\sum F = 0$,

$$49.10 \text{ kN} - R_a - R_b = 0$$

$$49.10 \text{ kN} - 24.55 \text{ kN} - R_a = 0$$

$$R_a = 24.55 \text{ kN}$$

Shear force diagram

At point 2C, 24.55kN of R_a is acting upwards.

From 2C to 4, there is a UDL of 19.96kN/m acting downwards, therefore

$$19.96 \text{ kN/m} \times 2.46 \text{ m} = 49.1016 \text{ kN}$$

$$24.55 \text{ kN} - 49.1016 \text{ kN} = -24.55 \text{ kN}$$

At point 4, another 24.55kN of R_b acting upwards, thus making the beam balance.

Bending moment diagram

Positive area – negative area in shear force diagram

(+ve)

$$= (1/2) \times 24.55 \times (2.46/2)$$

$$= (1/2) \times 24.55 \times 1.23$$

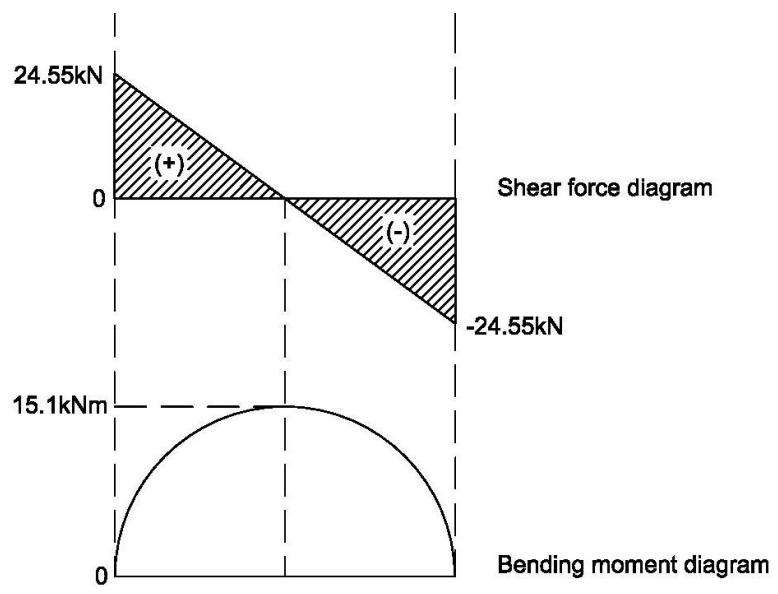
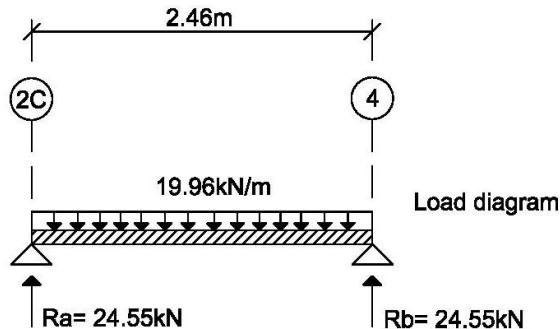
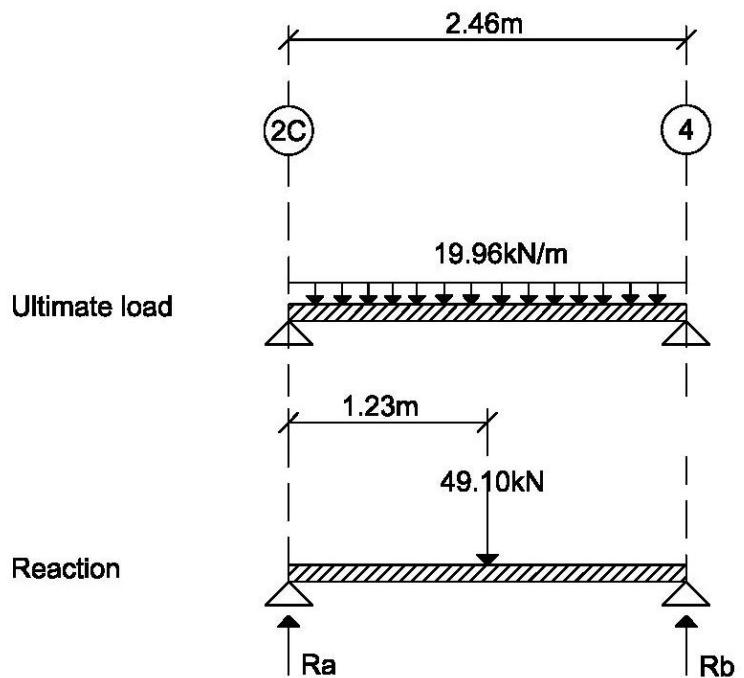
$$= 15.1$$

(-ve)

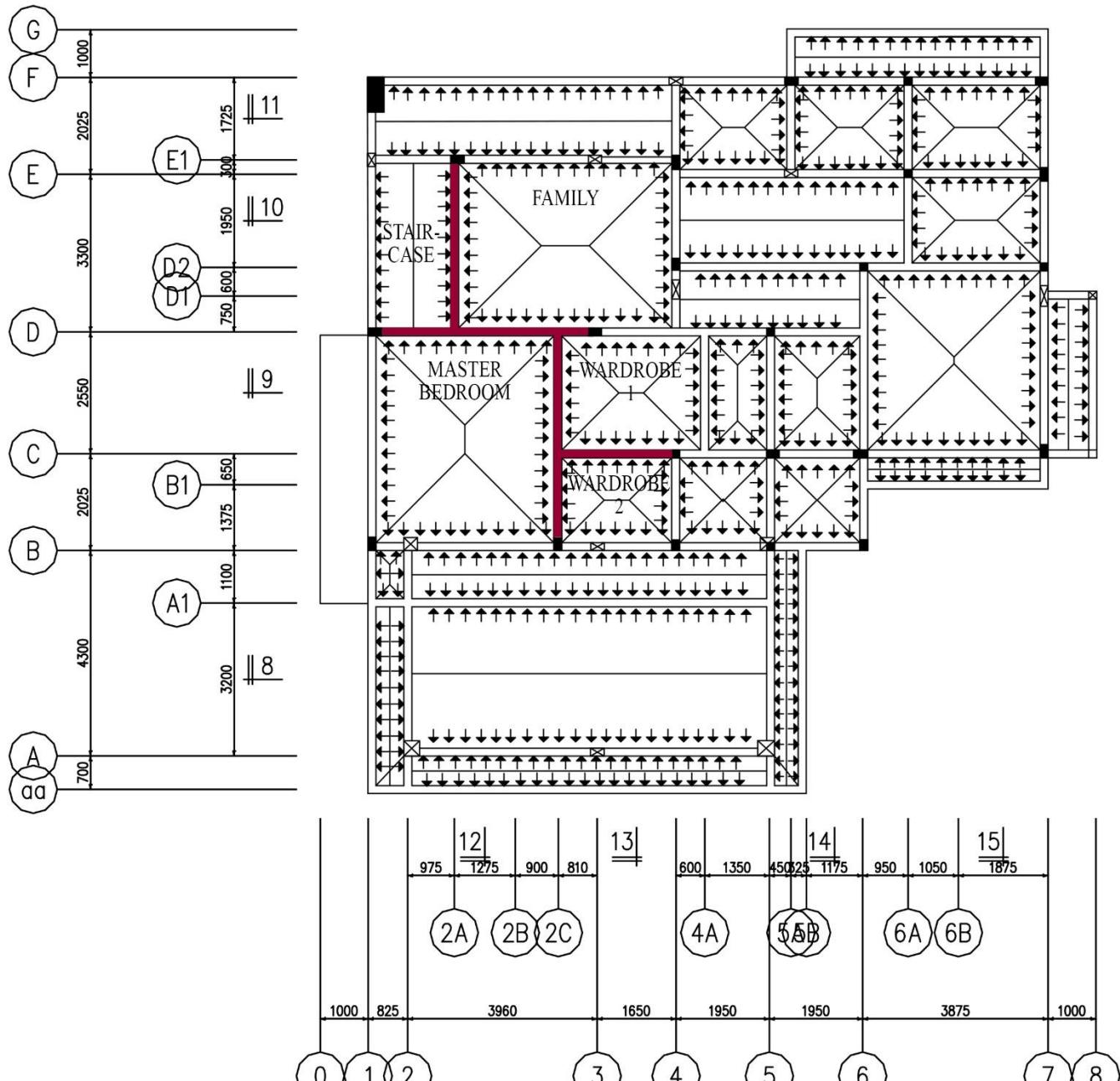
$$= (1/2) \times (-24.55) \times (2.46/2)$$

$$= (1/2) \times (-24.55) \times 1.23$$

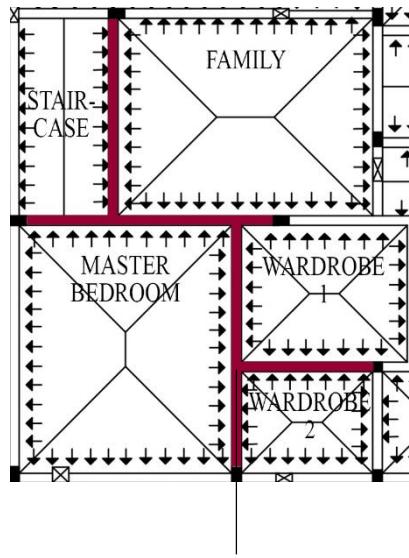
$$= -15.1$$



Analysis on beam 2C/ B-D



LOAD DISTRIBUTION DIAGRAM- FIRST FLOOR
(NTS)

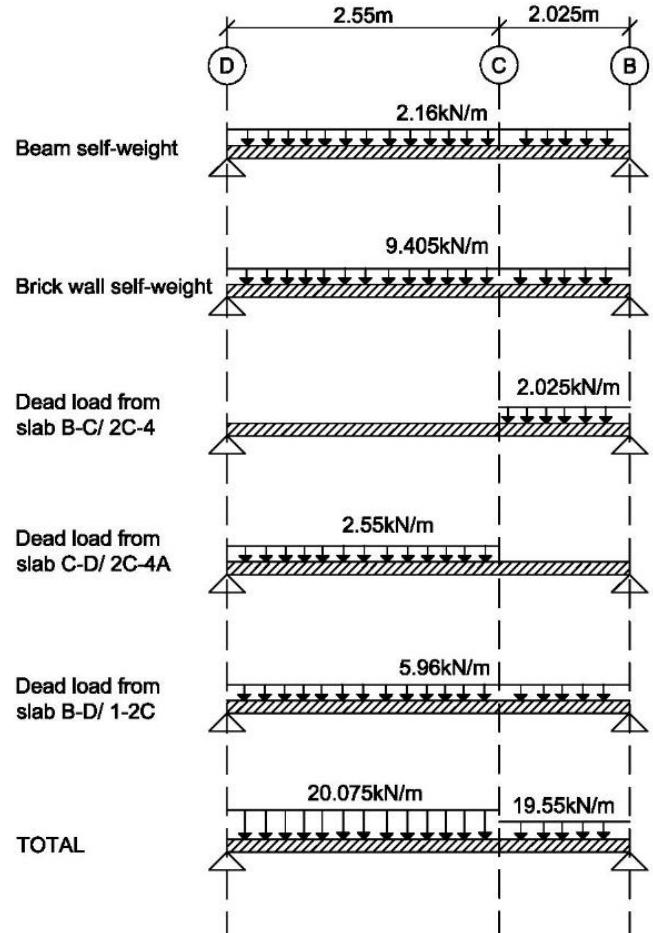


Beam 2C/ B- D (loads from wardrobe 1, wardrobe 2 and master bedroom are acting on it)

Dead loads acting on beam 2C/ B- D

1. Slab self-weight
= Slab thickness x concrete density
= $0.125\text{m} \times 24\text{Kn/m}^3$
= 3kN/m^2
2. Beam self-weight
= Beam size x concrete density
= $(0.15\text{m} \times 0.6\text{m}) \times 24\text{Kn/m}^3$
= 2.16kN/m
3. Brick wall self-weight
= Wall height x thickness x density
= $3.3\text{m} \times 0.15\text{m} \times 19\text{Kn/m}^3$
= 9.405kN/m
4. Dead load from the slab B- C/ 2C-4
= $3\text{kN/m}^2 \times (L_x/2) \times (2/3)$
= $3\text{kN/m}^2 \times (2.025/2) \times (2/3)$
= 2.025kN/m
5. Dead load from the slab C- D/ 2C-4A
= $3\text{kN/m}^2 \times (L_x/2) \times (2/3)$
= $3\text{kN/m}^2 \times (2.55/2) \times (2/3)$
= 2.55kN/m
6. Dead load from the slab B- D/ 1-2C
= $3\text{kN/m}^2 \times (L_x/2)$
= $3\text{kN/m}^2 \times (3.975/2)$
= 5.96kN/m

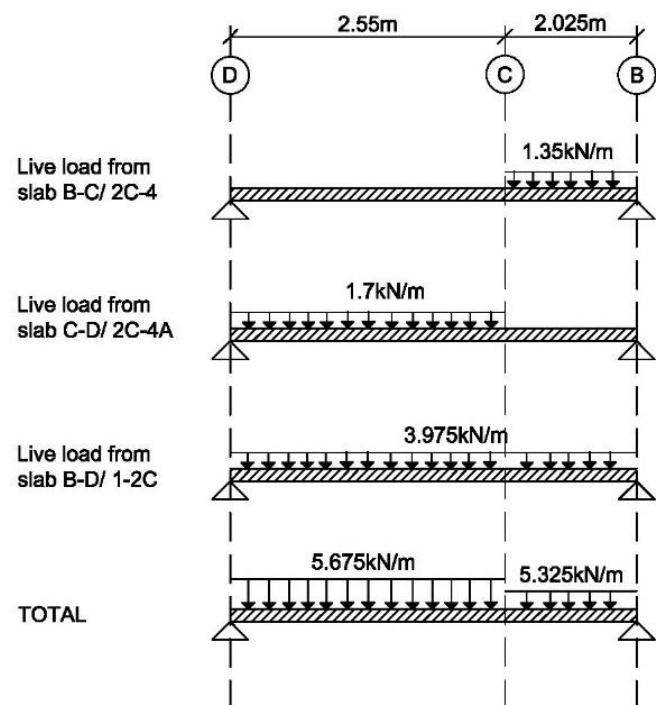
Total Dead Load Diagram



Live loads acting on beam 2C/ B- D

1. Live load from slab B- C/ 2C-4
 $= \text{live load of wardrobe } 2 \times (L_x/ 2) \times (2/3)$
 $= 2\text{kN/m}^2 \times (2.025\text{m}/ 2) \times (2/3)$
 $= 1.35\text{kN/m}$
2. Live load from slab C- D/ 2C-4A
 $= \text{live load of wardrobe } 1 \times (L_x/ 2) \times (2/3)$
 $= 2\text{kN/m}^2 \times (2.55\text{m}/ 2) \times (2/3)$
 $= 1.7\text{kN/m}$
3. Live load from slab B- D/ 1-2C
 $= \text{live load of master bedroom } \times (L_x/ 2)$
 $= 2\text{kN/m}^2 \times (3.975\text{m}/ 2)$
 $= 3.975\text{kN/m}$

Total Live Load Diagram



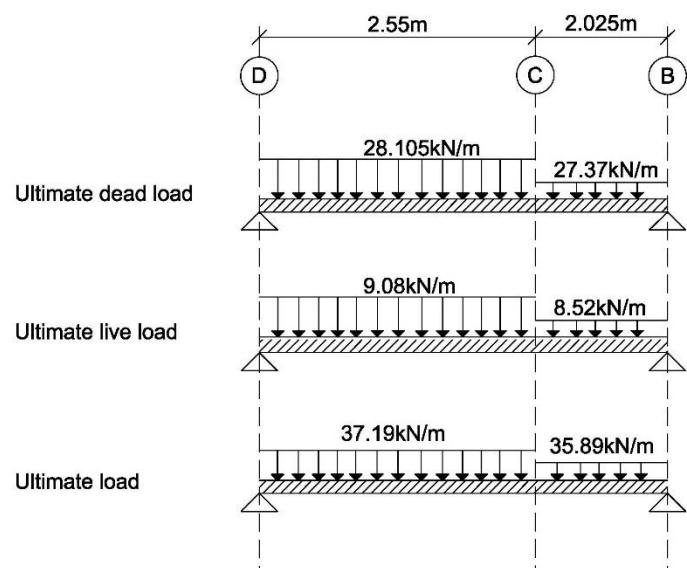
Ultimate Load

Dead load factor= 1.4

Live load factor= 1.6

1. Ultimate dead load at B- C
 $= 19.55\text{kN/m} \times 1.4$
 $= 27.37\text{kN/m}$
 Ultimate dead load at C- D
 $= 20.075\text{kN/m} \times 1.4$
 $= 28.105\text{kN/m}$
2. Ultimate live load at B- C
 $= 5.325\text{kN/m} \times 1.6$
 $= 8.52\text{kN/m}$
 Ultimate live load at C- D
 $= 5.675\text{kN/m} \times 1.6$
 $= 9.08\text{kN/m}$
3. Ultimate load at B- C
 $= 27.37\text{kN/m} + 8.52\text{kN/m}$
 $= 35.89\text{kN/m}$
 Ultimate load at C- D
 $= 28.105\text{kN/m} + 9.08\text{kN/m}$
 $= 37.19\text{kN/m}$

Ultimate Load Diagram



Reaction

The ultimate load (UDL) is converted into point load before resolving the reaction forces of the beam 2C/ B- D.

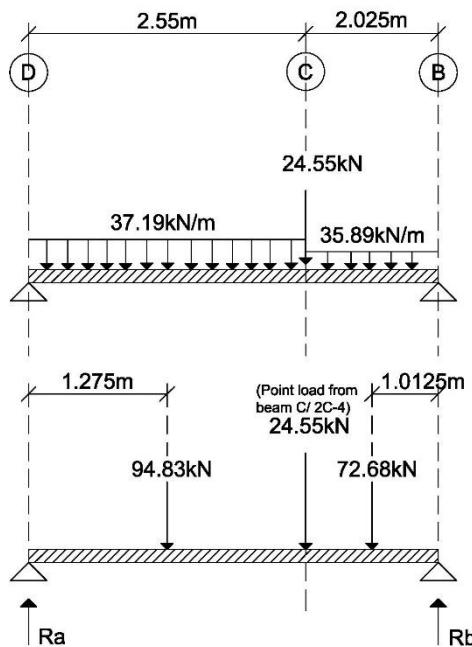
Ultimate load at B- C

$$= 35.89\text{kN/m} \times 2.025\text{m} = 72.68\text{kN}$$

Ultimate load at C- D

$$= 37.19\text{kN/m} \times 2.55\text{m} = 94.83\text{kN}$$

Reaction force, R_a of beam C/ 2C-4 acting on this beam is taken as the point load which is 24.55kN.



Assuming $\sum M = 0$,

$$(94.83\text{kN} \times 1.275\text{m}) + (24.55\text{kN} \times 2.55\text{m}) + (72.68\text{kN} \times 3.5625\text{m}) - (R_b \times 4.575\text{m}) = 0$$

$$120.91\text{kNm} + 65.60\text{kNm} + 258.92\text{kNm} - 4.575R_b = 0$$

$$442.43\text{kNm} - 4.575R_b = 0$$

$$-4.575R_b = -442.43\text{kNm}$$

$$R_b = 442.43\text{kNm} / 4.575\text{m}$$

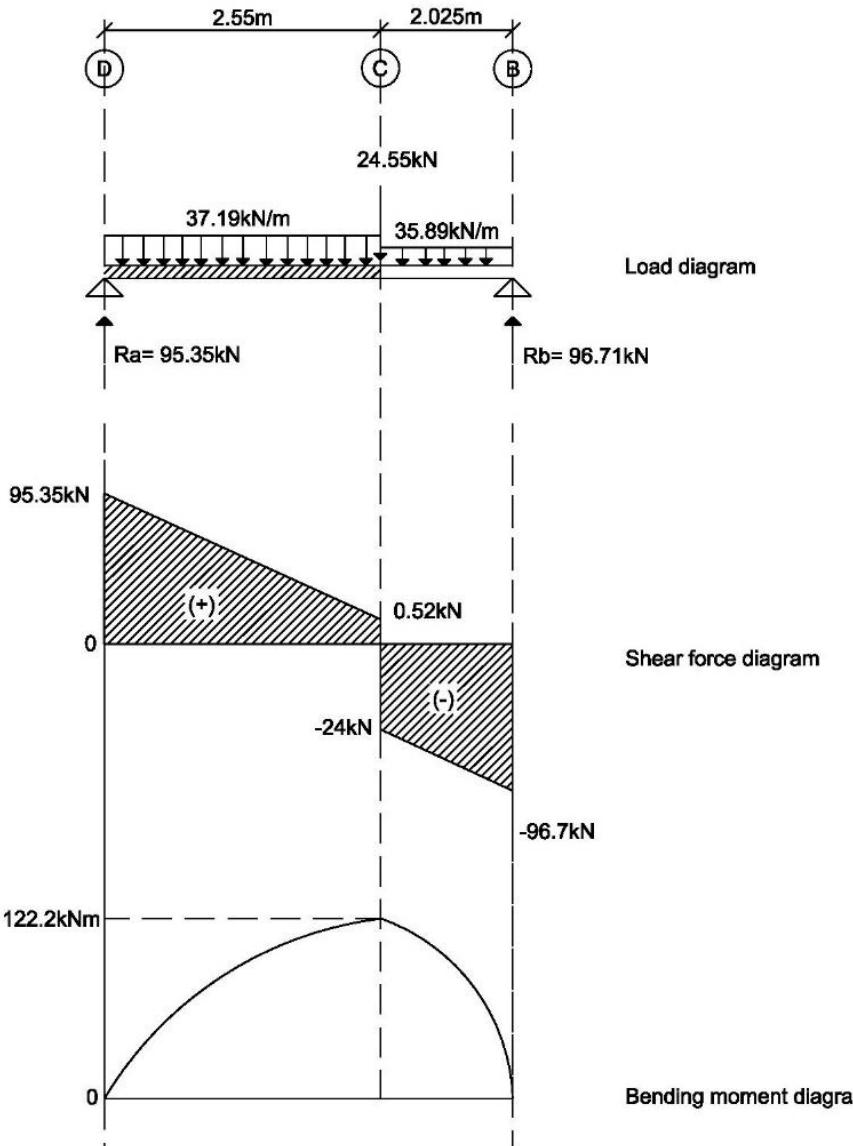
$$R_b = 96.71\text{kN}$$

Assuming $\sum F = 0$,

$$94.83\text{kN} + 24.55\text{kN} + 72.68\text{kN} - R_a - R_b = 0$$

$$192.06\text{kN} - 96.71\text{kN} - R_a = 0$$

$$R_a = 95.35\text{kN}$$



Shear force diagram

At point D, 95.35kN of R_a is acting upwards.

From D to C, there is a UDL of 37.19kN/m acting downwards, therefore

$$37.19\text{kN/m} \times 2.55\text{m} = 94.8345\text{kN}$$

$$95.35\text{kN} - 94.8345\text{kN} = 0.52\text{kN}$$

At point C, there is a point load of 24.55kN (R_a of beam C/ 2C-4) acting downwards, therefore

$$0.52\text{kN} - 24.55\text{kN} = -24\text{kN}$$

From C to B, there is a UDL of 35.89kN/m acting downwards, therefore

$$35.89\text{kN/m} \times 2.025\text{m} = 76.677\text{kN}$$

$$-24\text{kN} - 76.677\text{kN} = -96.68\text{kN} \approx -96.7\text{kN}$$

Which is then resolved by R_b of 96.71kN that is acting upwards.

Bending moment diagram

Bending moment diagram

Positive area – negative area in shear force diagram

(+ve)

$$= (1/2) \times (95.35 + 0.52) \times 2.55$$

$$= (1/2) \times 95.87 \times 2.55$$

$$= 122.23 \approx 122.2$$

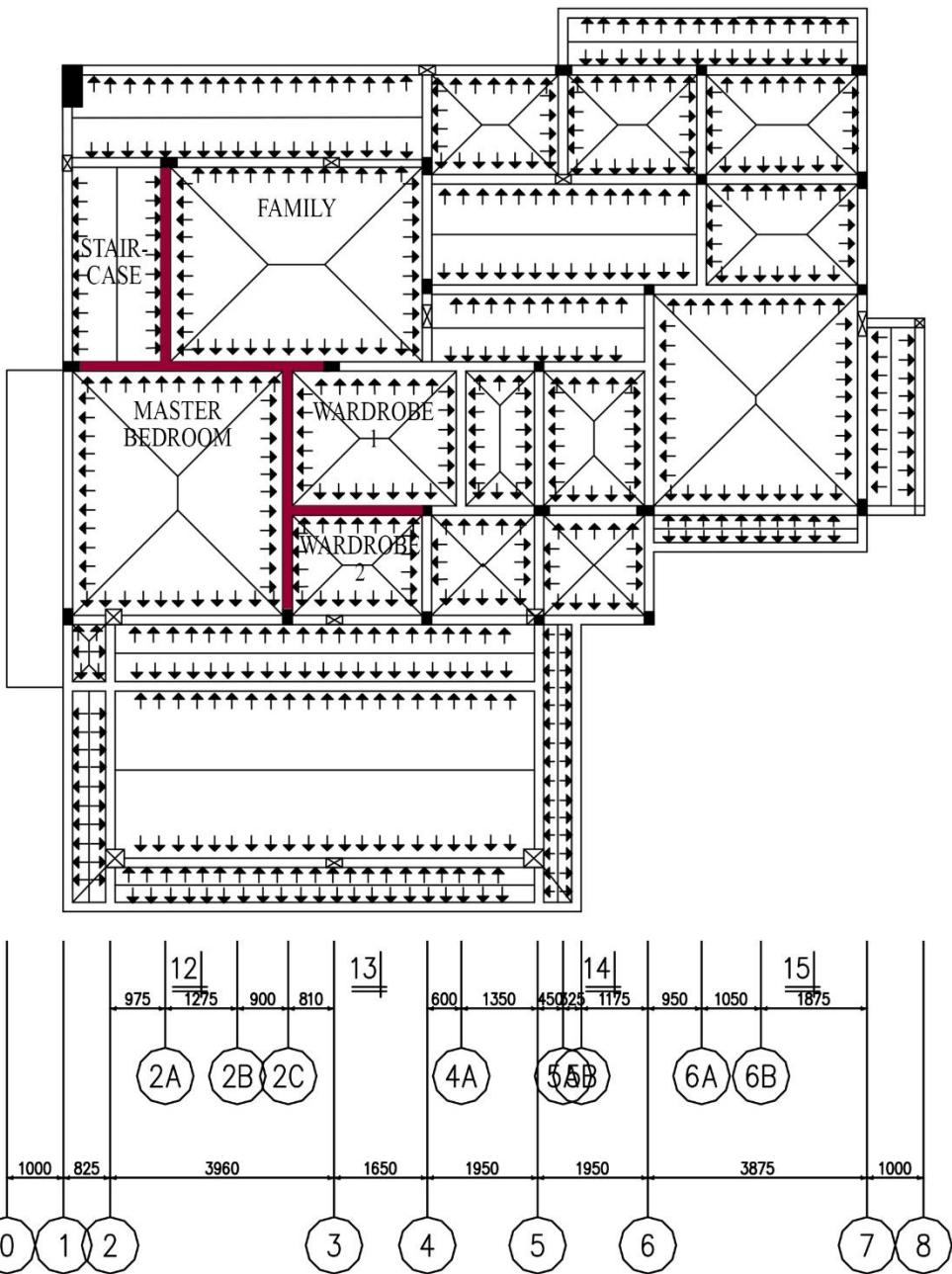
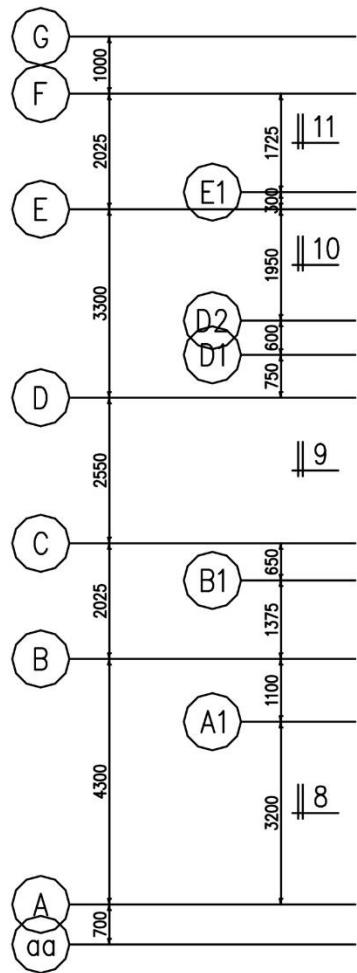
(-ve)

$$= (1/2) \times [(-24) + (-96.7)] \times 2.025$$

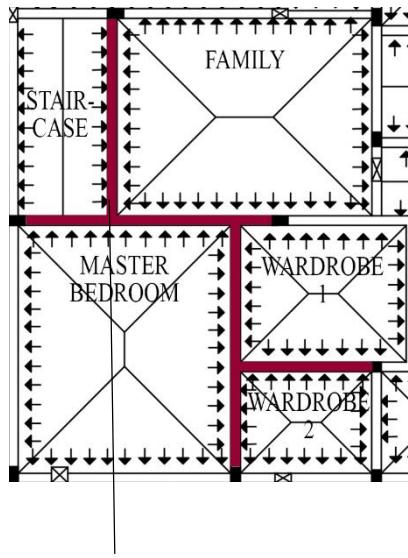
$$= (1/2) \times 120.7 \times 2.025$$

$$= 122.21 \approx -122.2$$

Analysis on beam 2A/ D-E1



LOAD DISTRIBUTION DIAGRAM- FIRST FLOOR
(NTS)



Beam 2A/ D- E1 (loads from staircase and family room are acting on it).

Dead loads acting on beam 2A/ D- E1

1. Slab self-weight

$$= \text{Slab thickness} \times \text{concrete density}$$

$$= 0.125\text{m} \times 24\text{Kn/m}^3$$

$$= 3\text{kN/m}^2$$
2. Beam self-weight

$$= \text{Beam size} \times \text{concrete density}$$

$$= (0.15\text{m} \times 0.6\text{m}) \times 24\text{Kn/m}^3$$

$$= 2.16\text{kN/m}$$
3. Brick wall self-weight

$$= \text{Wall height} \times \text{thickness} \times \text{density}$$

$$= 3.3\text{m} \times 0.15\text{m} \times 19\text{Kn/m}^3$$

$$= 9.405\text{kN/m}$$
4. Dead load from the slab D- E1/ 1-2A

$$= 3\text{kN/m}^2 \times (L_x/2)$$

$$= 3\text{kN/m}^2 \times (1.8/2)$$

$$= 2.7\text{kN/m}$$
5. Dead load from the slab D- E1/ 2A-4

$$= 3\text{kN/m}^2 \times (L_x/2) \times (2/3)$$

$$= 3\text{kN/m}^2 \times (3.6/2) \times (2/3)$$

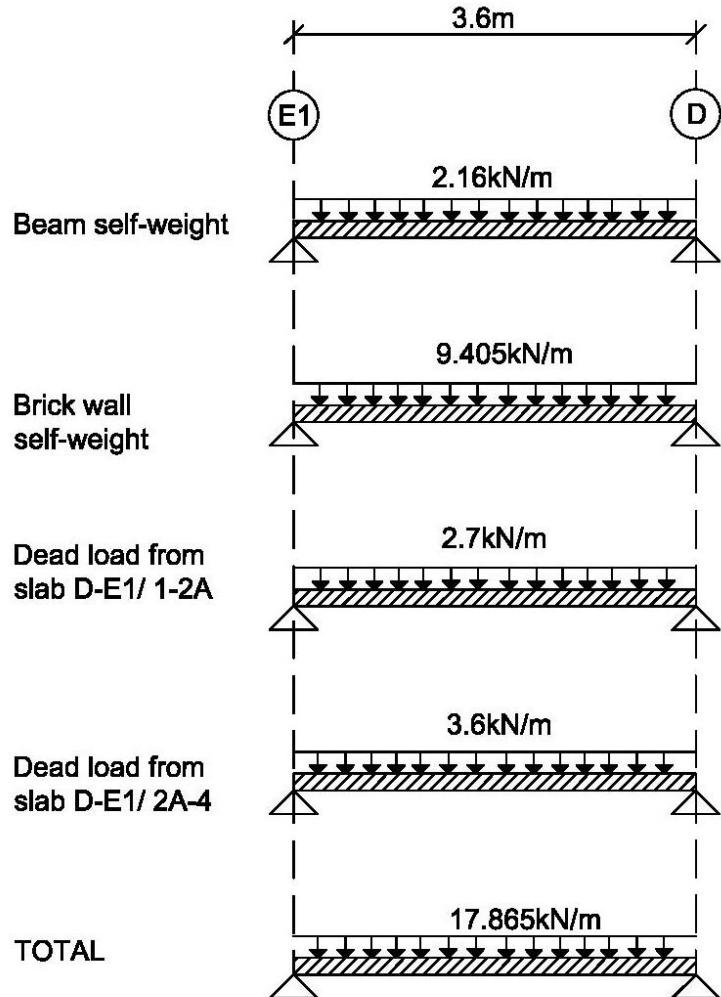
$$= 3.6\text{kN/m}$$
6. Total dead load

$$= 2.16\text{kN/m} + 9.405\text{kN/m} + 2.7\text{kN/m}$$

$$+ 3.6\text{kN/m}$$

$$= 17.865\text{kN/m}$$

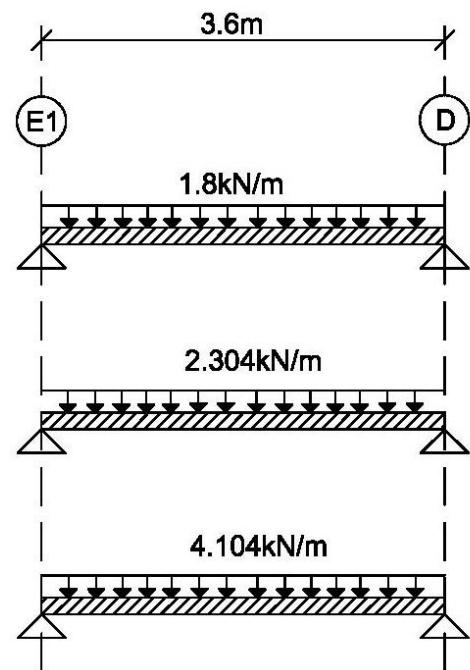
Total Dead Load Diagram



Live loads acting on beam 2A/ D- E1

1. Live load from slab D- E1/ 1-2A
 $= \text{live load of staircase} \times (L_x/ 2)$
 $= 2\text{kN/m}^2 \times (1.8\text{m}/ 2)$
 $= 1.8\text{kN/m}$
2. Live load from slab D- E1/ 2A-4
 $= \text{live load of family room} \times (L_x/ 2) \times (2/3)$
 $= 1.92\text{kN/m}^2 \times (3.6\text{m}/ 2) \times (2/3)$
 $= 2.304\text{kN/m}$
3. Total live load
 $= 1.8\text{kN/m} + 2.304\text{kN/m}$
 $= 4.104\text{kN/m}$

Total Live Load Diagram



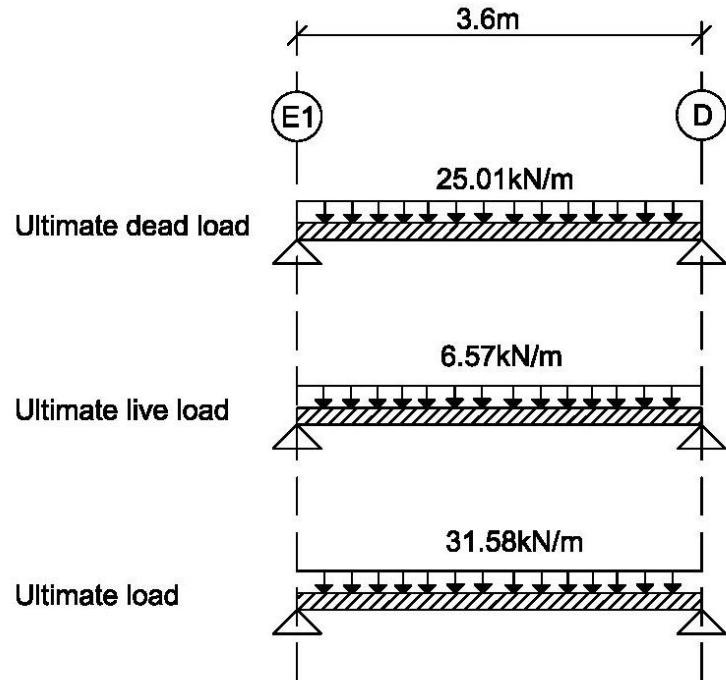
Ultimate Load

Dead load factor= 1.4

Live load factor= 1.6

4. Ultimate dead load
 $= 17.865\text{kN/m} \times 1.4$
 $= 25.01\text{kN/m}$
5. Ultimate live load
 $= 4.104\text{kN/m} \times 1.6$
 $= 6.57\text{kN/m}$
6. Ultimate load
 $= 25.01\text{kN/m} + 6.57\text{kN/m}$
 $= 31.58\text{kN/m}$

Ultimate Load Diagram



Reaction

The ultimate load (UDL) is converted into point load before resolving the reaction forces of the beam 2A/ D- E1.

Ultimate load

$$= 31.58 \text{ kN/m} \times 3.6 \text{ m} = 113.69 \text{ kN}$$

Assuming $\sum M = 0$,

$$(113.69 \text{ kN} \times 1.8 \text{ m}) - (R_b \times 3.6 \text{ m}) = 0$$

$$204.64 \text{ kNm} - 3.6R_b = 0$$

$$-3.6R_b = -204.64 \text{ kNm}$$

$$R_b = 204.64 \text{ kNm} / 3.6 \text{ m}$$

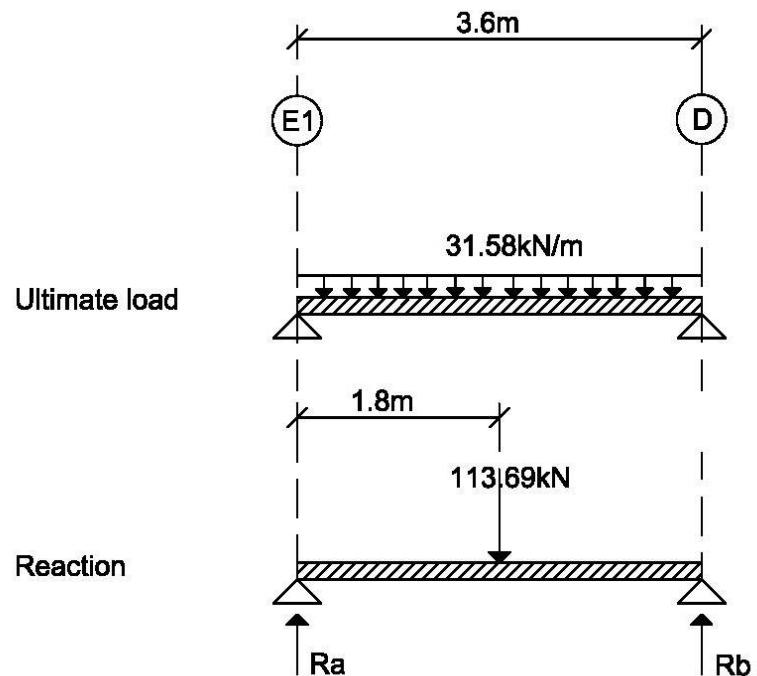
$$R_b = 56.85 \text{ kN}$$

Assuming $\sum F = 0$,

$$113.69 \text{ kN} - R_a - R_b = 0$$

$$113.69 \text{ kN} - 56.85 \text{ kN} - R_a = 0$$

$$R_a = 56.84 \text{ kN}$$



Shear force diagram

At point E1, 56.84kN of R_a is acting upwards.

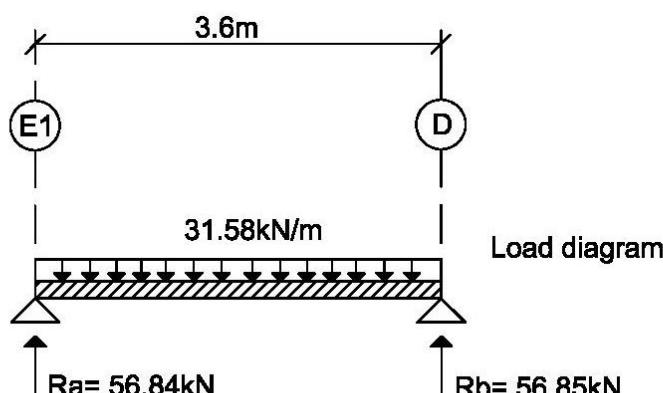
From E1 to D, there is a UDL of 31.58kN/m acting downwards, therefore

$$31.58 \text{ kN/m} \times 3.6 \text{ m} = 113.688 \text{ kN}$$

$$56.84 \text{ kN} - 113.688 \text{ kN} = -56.848 \text{ kN}$$

At point D, another 56.85kN of R_b acting upwards,

thus making the beam balance.



Bending moment diagram

Positive area – negative area in shear force diagram

(+ve)

$$= (1/2) \times 56.84 \times (3.6/2)$$

$$= (1/2) \times 56.84 \times 1.8$$

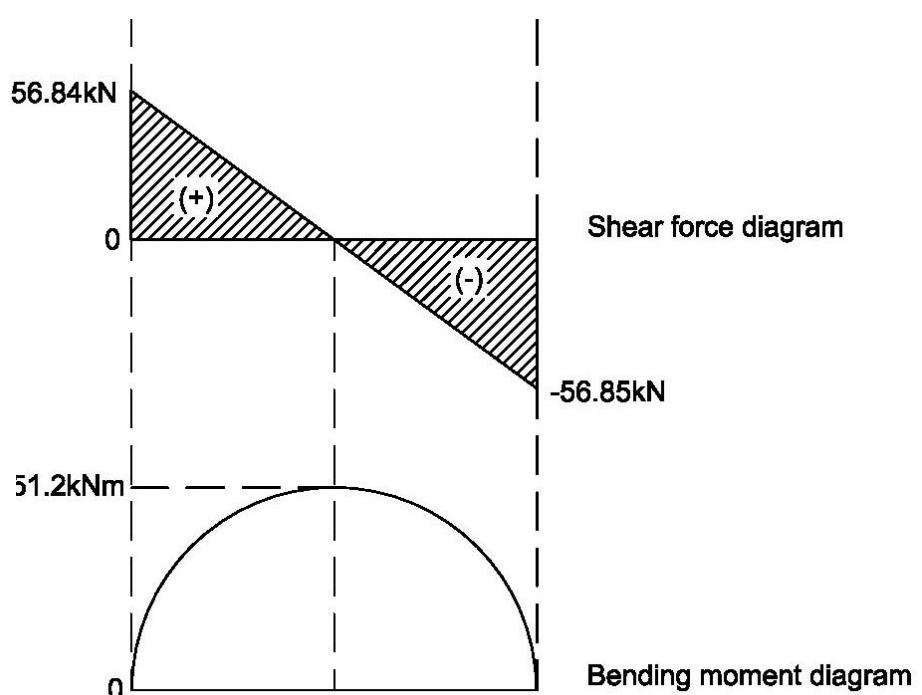
$$= 51.156 \approx 51.2$$

(-ve)

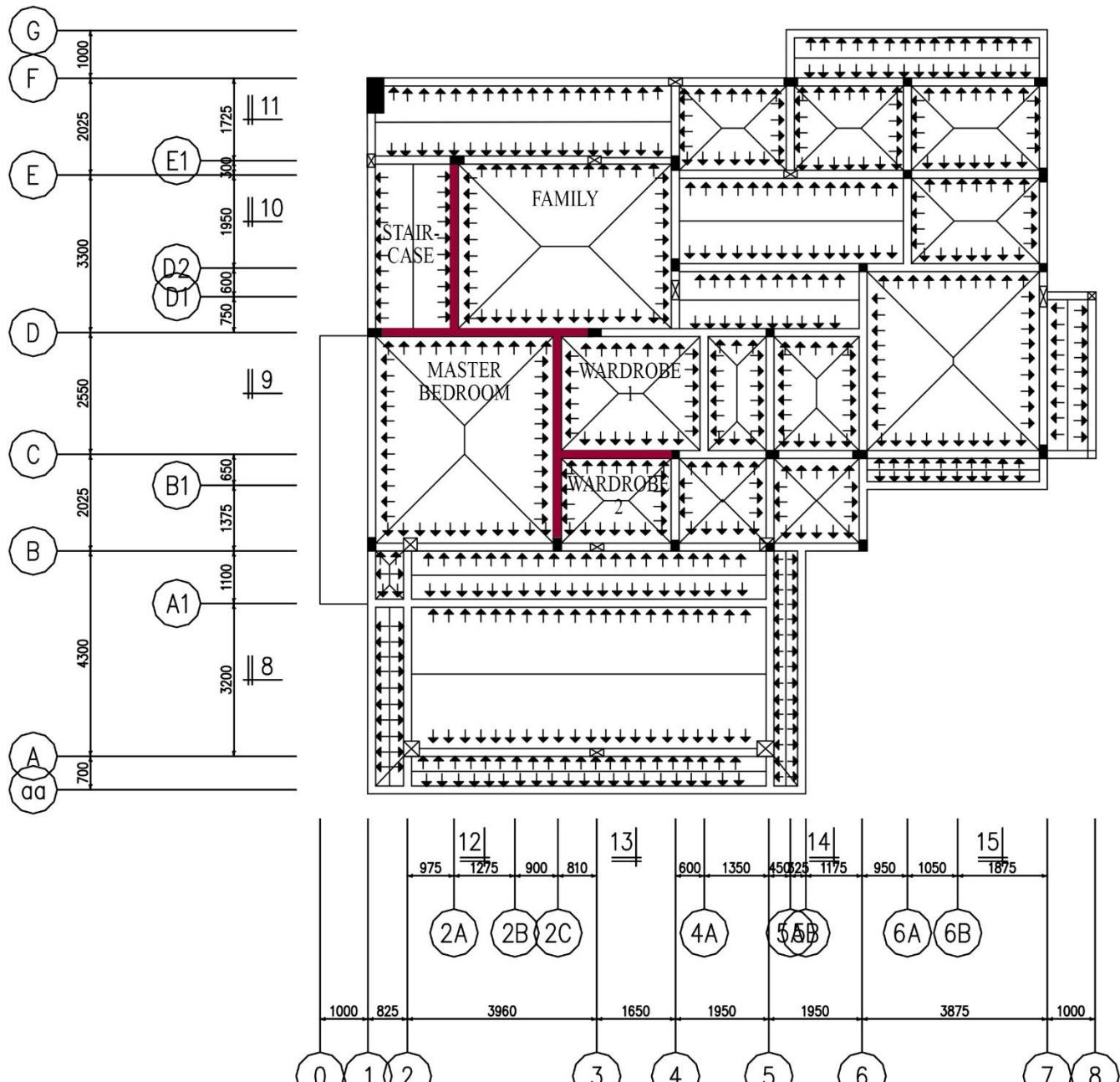
$$= (1/2) \times (-56.85) \times (3.6/2)$$

$$= (1/2) \times (-56.85) \times 1.8$$

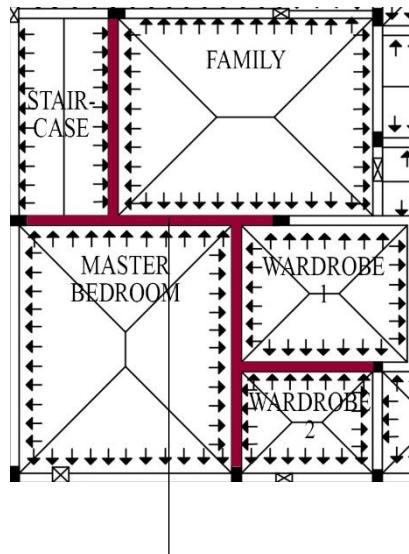
$$= -51.165 \approx -51.2$$



Analysis on beam D/ 1-3



LOAD DISTRIBUTION DIAGRAM- FIRST FLOOR
(NTS)

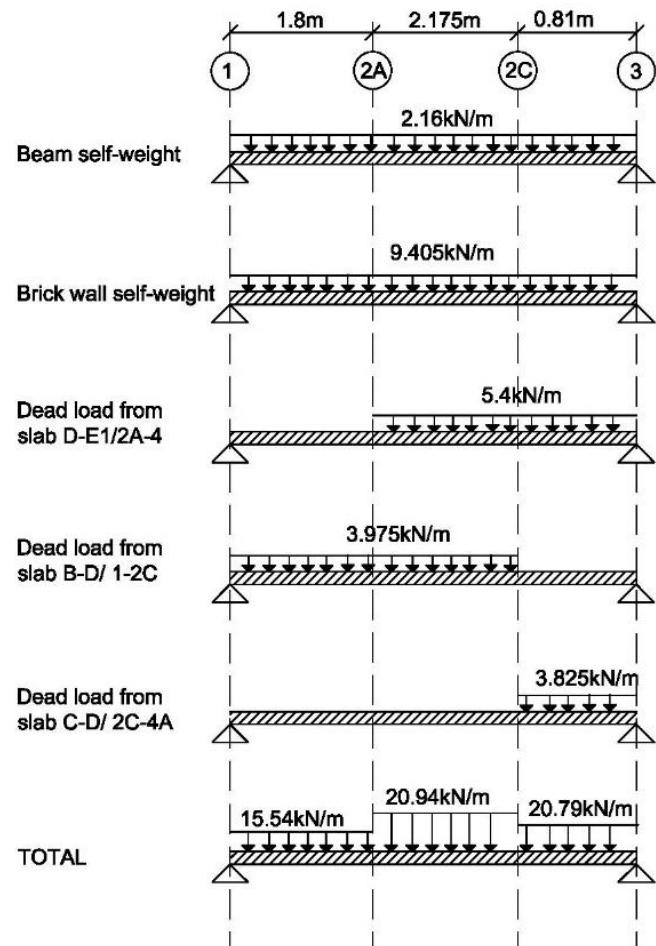


Beam D/ 1-3 (loads from wardrobe 1, family room and master bedroom are acting on it)

Dead loads acting on beam D/ 1-3

1. Slab self-weight
 $= \text{Slab thickness} \times \text{concrete density}$
 $= 0.125\text{m} \times 24\text{Kn/m}^3$
 $= 3\text{kN/m}^2$
2. Beam self-weight
 $= \text{Beam size} \times \text{concrete density}$
 $= (0.15\text{m} \times 0.6\text{m}) \times 24\text{Kn/m}^3$
 $= 2.16\text{kN/m}$
3. Brick wall self-weight
 $= \text{Wall height} \times \text{thickness} \times \text{density}$
 $= 3.3\text{m} \times 0.15\text{m} \times 19\text{Kn/m}^3$
 $= 9.405\text{kN/m}$
4. Dead load from the slab D- E1/ 2A-4
 $= 3\text{kN/m}^2 \times (L_x/2)$
 $= 3\text{kN/m}^2 \times (3.6/2)$
 $= 5.4\text{kN/m}$
5. Dead load from the slab B- D/ 1-2C
 $= 3\text{kN/m}^2 \times (L_x/2) \times (2/3)$
 $= 3\text{kN/m}^2 \times (3.975/2) \times (2/3)$
 $= 3.975\text{kN/m}$
6. Dead load from the slab C- D/ 2C-4A
 $= 3\text{kN/m}^2 \times (L_x/2)$
 $= 3\text{kN/m}^2 \times (2.55/2)$
 $= 3.825\text{kN/m}$

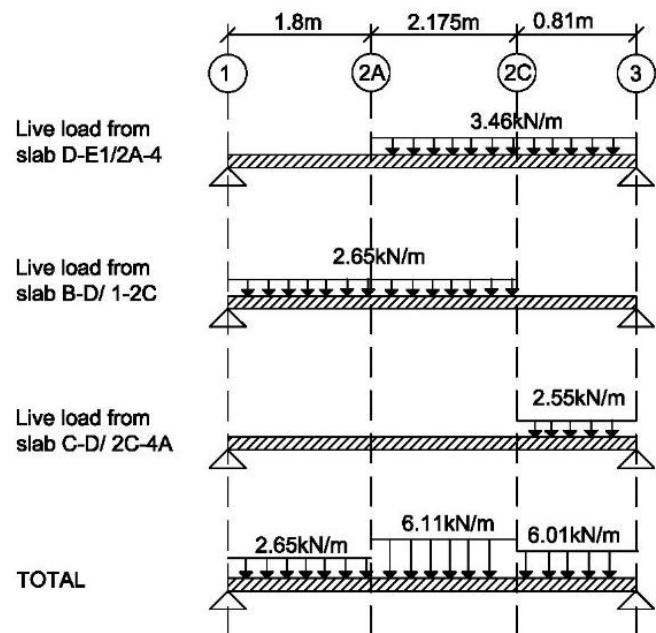
Total Dead Load Diagram



Live loads acting on beam D/ 1-3

1. Live load from slab D- E1/ 2A-4
 $= \text{live load of family room } x (L_x / 2)$
 $= 1.92 \text{ kN/m}^2 \times (3.6 \text{ m} / 2)$
 $= 3.46 \text{ kN/m}$
2. Live load from slab B- D/ 1-2C
 $= \text{live load of master bedroom } x (L_x / 2) \times (2/3)$
 $= 2 \text{ kN/m}^2 \times (3.975 \text{ m} / 2) \times (2/3)$
 $= 2.65 \text{ kN/m}$
3. Live load from slab C- D/ 2C-4A
 $= \text{live load of wardrobe 1 } x (L_x / 2)$
 $= 2 \text{ kN/m}^2 \times (2.55 \text{ m} / 2)$
 $= 2.55 \text{ kN/m}$

Total Live Load Diagram



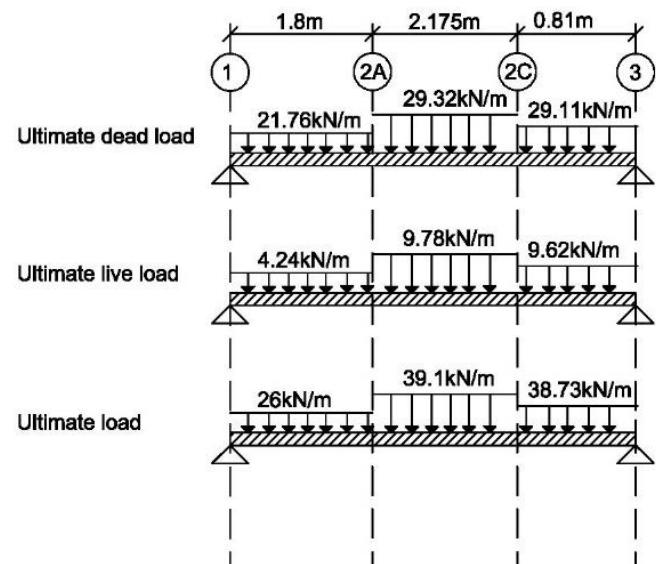
Ultimate Load

Dead load factor= 1.4

Live load factor= 1.6

1. Ultimate dead load at 1- 2A
 $= 15.54 \text{ kN/m} \times 1.4$
 $= 21.76 \text{ kN/m}$
 Ultimate dead load at 2A- 2C
 $= 20.94 \text{ kN/m} \times 1.4$
 $= 29.32 \text{ kN/m}$
 Ultimate dead load at 2C- 3
 $= 20.79 \text{ kN/m} \times 1.4$
 $= 29.11 \text{ kN/m}$
2. Ultimate live load at 1- 2A
 $= 2.65 \text{ kN/m} \times 1.6$
 $= 4.24 \text{ kN/m}$
 Ultimate live load at 2A- 2C
 $= 6.11 \text{ kN/m} \times 1.6$
 $= 9.78 \text{ kN/m}$
 Ultimate live load at 2C- 3
 $= 6.01 \text{ kN/m} \times 1.6$
 $= 9.62 \text{ kN/m}$
3. Ultimate load at 1- 2A
 $= 21.76 \text{ kN/m} + 4.24 \text{ kN/m}$
 $= 26 \text{ kN/m}$
 Ultimate load at 2A- 2C
 $= 29.32 \text{ kN/m} + 9.78 \text{ kN/m}$
 $= 39.1 \text{ kN/m}$
 Ultimate load at 2C- 3
 $= 29.11 \text{ kN/m} + 9.62 \text{ kN/m}$
 $= 38.73 \text{ kN/m}$

Ultimate Load Diagram



Reaction

The ultimate load (UDL) is converted into point load before resolving the reaction forces of the beam D/1-3.

Ultimate load at 1- 2A

$$= 26\text{kN/m} \times 1.8\text{m} = 46.8\text{kN}$$

Ultimate load at 2A- 2C

$$= 39.1\text{kN/m} \times 2.175\text{m} = 85.04\text{kN}$$

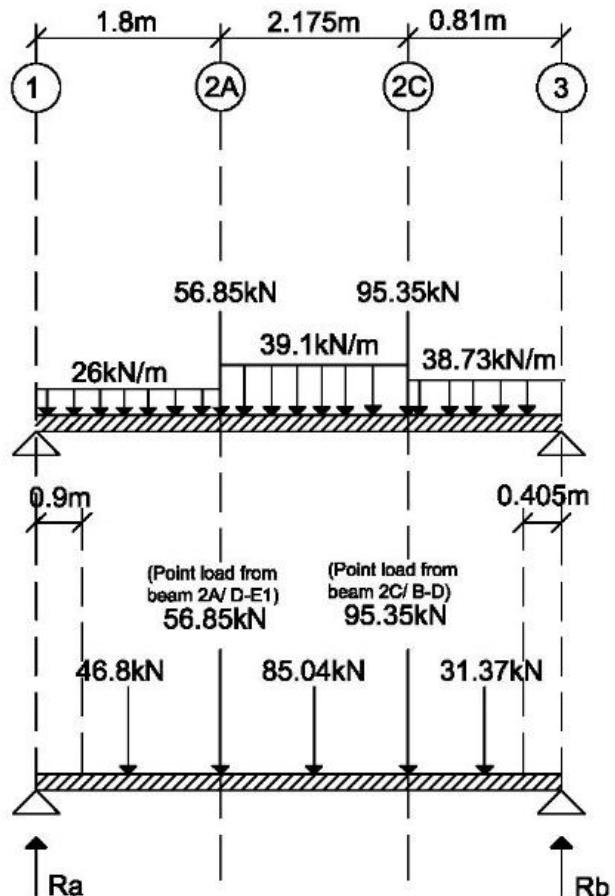
Ultimate load at 2C- 3

$$= 38.73\text{kN/m} \times 0.81\text{m} = 31.37\text{kN}$$

Reaction force, R_b of beam 2A/D- E1 acting on this beam is taken as the point load which is 56.85kN, and also reaction force, R_a of beam 2C/B- D which is 95.35kN.

Ultimate load

Reaction



Assuming $\sum M = 0$,

$$(46.8\text{kN} \times 0.9\text{m}) + (56.85\text{kN} \times 1.8\text{m}) + (85.04\text{kN} \times 2.8875\text{m}) + (95.35\text{kN} \times 3.975\text{m}) + (31.37\text{kN} \times 4.38\text{m}) - (R_b \times 4.785\text{m}) = 0$$

$$42.12\text{kNm} + 102.33\text{kNm} + 245.553\text{kNm} + 379.02\text{kNm} + 137.40\text{kNm} - 4.785R_b = 0$$

$$906.423\text{kNm} - 4.785R_b = 0$$

$$-4.785R_b = -906.423\text{kNm}$$

$$R_b = 906.423\text{kNm} / 4.785\text{m}$$

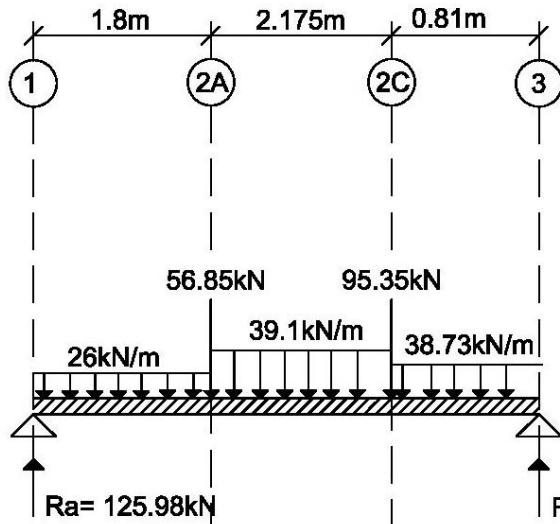
$$R_b = 189.43\text{kN}$$

Assuming $\sum F = 0$,

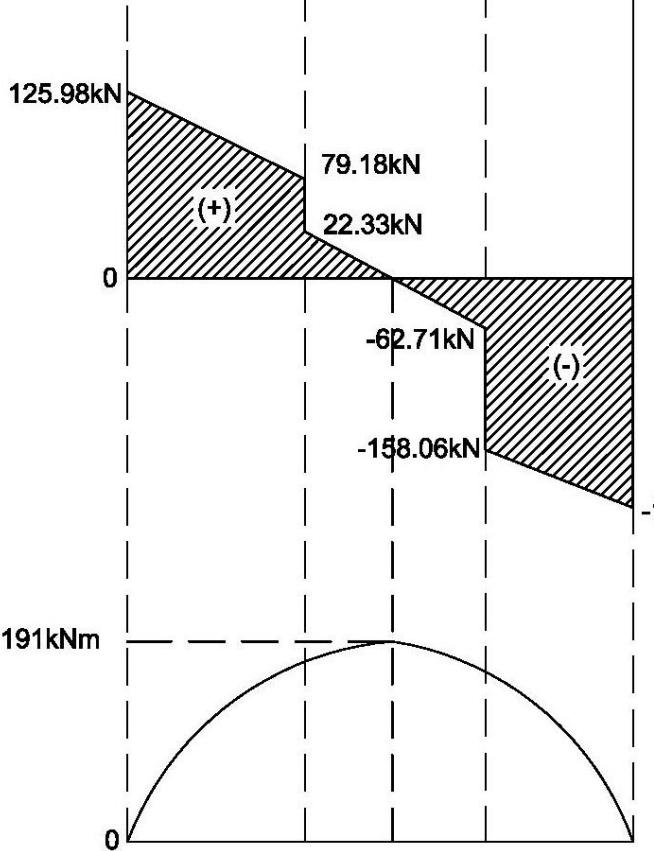
$$46.8\text{kN} + 56.85\text{kN} + 85.04\text{kN} + 95.35\text{kN} + 31.37\text{kN} - R_a - R_b = 0$$

$$315.41\text{kN} - 189.43\text{kN} - R_a = 0$$

$$R_a = 125.98\text{kN}$$



Load diagram



Shear force diagram

Bending moment diagram

Bending moment diagram

Shear force diagram

At point 1, 125.98kN of R_a is acting upwards.

From 1 to 2A, there is a UDL of 26kN/m acting downwards, therefore

$$26\text{kN/m} \times 1.8\text{m} = 46.8\text{kN}$$

$$125.98\text{kN} - 46.8\text{kN} = 79.18\text{kN}$$

At point 2A, there is a point load of 56.85kN (R_b of beam 2A/D-E1) acting downwards, therefore

$$79.18\text{kN} - 56.85\text{kN} = 22.33\text{kN}$$

From 2A to 2C, there is a UDL of 39.1kN/m acting downwards, therefore

$$39.1\text{kN/m} \times 2.175\text{m} =$$

$$85.0425\text{kN}$$

$$22.33\text{kN} - 85.0425\text{kN} =$$

$$-62.7125\text{kN}$$

At point 2C, there is another point load of 95.35kN (R_a of beam 2C/ B- D) acting downwards, therefore,

$$-62.71\text{kN} - 95.35\text{kN} = -158.0625$$

From 2C to 3, there is a UDL of 38.73kN/m acting downwards, therefore

$$38.73\text{kN/m} \times 0.81\text{m} = 31.3713$$

$$-158.0625 - 31.3713 = -189.43$$

Which is then resolved by R_b of 189.43kN that is acting upwards.

Positive area – negative area in shear force diagram

(+ve)

$$= [(1/2) \times (125.98 + 79.18) \times 1.8] + [(1/2) \times 0.57 \times 22.33]$$

$$= 184.644 + 6.36$$

$$= 191.04 \approx 191$$

(-ve)

$$= [(1/2) \times (-62.71) \times (2.175 - 0.57)] + [(1/2) \times (158.06 + 189.43) \times 0.81]$$

$$= 50.32 + 140.73$$

$$= 191.05 \approx 191$$